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3D Face Recognition Under Expressions, Occlusions and Pose Variations
Hassen Drira, Boulbaba Ben Amor, Anuj Srivastava, Mohamed Daoudi, and Rim Slama

Abstract—We propose a novel geometric framework for analyzing 3D faces, with the specific goals of comparing, matching, and averaging their shapes. Here we represent facial surfaces by radial curves emanating from the nose tips and use elastic shape analysis of these curves to develop a Riemannian framework for analyzing shapes of full facial surfaces. This representation, along with the elastic Riemannian metric, seems natural for measuring facial deformations and is robust to challenges such as large facial expressions (especially those with open mouths), large pose variations, missing parts, and partial occlusions due to glasses, hair, etc. This framework is shown to be promising from both — empirical and theoretical — perspectives. In terms of the empirical evaluation, our results match or improve the state-of-the-art methods on three prominent databases: FRGCv2, GavabDB, and Bosphorus, each posing a different type of challenge. From a theoretical perspective, this framework allows for formal statistical inferences, such as the estimation of missing facial parts using PCA on tangent spaces and computing average shapes.

Index Terms—3D face recognition, shape analysis, biometrics, quality control, data restoration.

1 INTRODUCTION

Due to the natural, non-intrusive, and high-throughput nature of face data acquisition, automatic face recognition has many benefits when compared to other biometrics. Accordingly, automated face recognition has received a growing attention within the computer vision community over the past three decades. Amongst different modalities available for face imaging, 3D scanning has a major advantage over 2D color imaging in that nuisance variables, such as illumination and small pose changes, have a relatively smaller influence on the observations. However, 3D scans often suffer from the problem of missing parts due to self occlusions or external occlusions, or some imperfections in the scanning technology. Additionally, variations in face scans due to changes in facial expressions can also degrade face recognition performance. In order to be useful in real-world applications, a 3D face recognition approach should be able to handle these challenges, i.e., it should recognize people despite large facial expressions, occlusions and large pose variations. Some examples of face scans highlighting these issues are illustrated in Fig. 1.

We note that most recent research on 3D face analysis has been directed towards tackling changes in facial expressions while only a relatively modest effort has been spent on handling occlusions and missing parts. Although a few approaches and corresponding results dealing with missing parts have been presented, none, to our knowledge, has been applied systematically to a full real database containing scans with missing parts. In this paper, we present a comprehensive Riemannian framework for analyzing facial shapes, in the process dealing with large expressions, occlusions and missing parts. Additionally, we provide some basic tools for statistical shape analysis of facial surfaces. These tools help us to compute a typical or average shape and measure the intra-class variability of shapes, and will even lead to face atlases in the future.

1.1 Previous Work

The task of recognizing 3D face scans has been approached in many ways, leading to varying levels of successes. We refer the reader to one of many extensive surveys on the topic, e.g. see Bowyer et al. [3]. Below we summarize a smaller subset that is more relevant to our paper.
1. Deformable template-based approaches: There have been several approaches in recent years that rely on deforming facial surfaces into one another, under some chosen criteria, and use quantifications of these deformations as metrics for face recognition. Among these, the ones using non-linear deformations facilitate the local stretching, compression, and bending of surfaces to match each other and are referred to as elastic methods. For instance, Kakadiaris et al. [13] utilize an annotated face model to study geometrical variability across faces. The annotated face model is deformed elastically to fit each face, thus matching different anatomical areas such as the nose, eyes, and mouth. In [25], Passalis et al. use automatic landmarking to estimate the pose and to detect occluded areas. The facial symmetry is used to overcome the challenges of missing data here. Similar approaches, but using manually annotated models, are presented in [31], [17]. For example, [17] uses manual landmarks to develop a thin-plate-spline based matching of facial surfaces. A strong limitation of these approaches is that the extraction of fiducial landmarks needed during learning is either manual or semi-automated, except in [13] where it is fully automated.

2. Local regions/ features approaches: Another common framework, especially for handling expression variability, is based on matching only parts or regions rather than matching full faces. Lee et al. [15] use ratios of distances and angles between eight fiducial points, followed by a SVM classifier. Similarly, Gupta et al. [11] use Euclidean/geodesic distances between anthropometric fiducial points, in conjunction with linear classifiers. As stated earlier, the problem of automated detection of fiducial points is non-trivial and hinders automation of these methods. Gordon [10] argues that curvature descriptors have the potential for higher accuracy in describing surface features and are better suited to describe the properties of faces in areas such as the cheeks, forehead, and chin. These descriptors are also invariant to viewing angles. Li et al. [16] design a feature pooling and ranking scheme in order to collect various types of low-level geometric features, such as curvatures, and rank them according to their sensitivity to facial expressions. Along similar lines, Wang et al. [32] use a signed shape-difference map between two aligned 3D faces as an intermediate representation for shape comparison. McKeon and Russ [19] use a region ensemble approach that is based on Fisherfaces, i.e., face representations are learned using Fisher’s discriminant analysis.

In [12], Huang et al. use a multi-scale Local Binary Pattern (LBP) for a 3D face jointly with shape index. Similarly, Moorthy et al. [20] use Gabor features around automatically detected fiducial points. To avoid passing over deformable parts of faces encompassing discriminative information, Faltemier et al. [9] use 38 face regions that densely cover the face, and fuse scores and decisions after performing ICP on each region. A similar idea is proposed in [29] that uses PCA-LDA for feature extraction, treating the likelihood ratio as a matching score and using the majority voting for face identification. Queirolo et al. [26] use Surface Inter-penetration Measure (SIM) as a similarity measure to match two face images. The authentication score is obtained by combining the SIM values corresponding to the matching of four different face regions: circular and elliptical areas around the nose, forehead, and the entire face region. In [1], the authors use Average Region Models (ARMs) locally to handle the challenges of missing data and expression-related deformations. They manually divide the facial area into several meaningful components and the registration of faces is carried out by separate dense alignments to the corresponding ARMs. A strong limitation of this approach is the need for manual segmentation of a face into parts that can then be analyzed separately.

3. Surface-distance based approaches: There are several papers that utilize distances between points on facial surfaces to define features that are eventually used in recognition. (Some papers call it geodesic distance but, in order to distinguish it from our later use of geodesics on shape spaces of curves and surfaces, we shall call it surface distance.) These papers assume that surface distances are relatively invariant to small changes in facial expressions and, therefore, help generate features that are robust to facial expressions. Bronstein et al. [4] provide a limited experimental illustration of this invariance by comparing changes in surface distances with the Euclidean distances between corresponding points on a canonical face surface. To handle the open mouth problem, they first detect and remove the lip region, and then compute the surface distance in presence of a hole corresponding to the removed part [5]. The assumption of preservation of surface distances under facial expressions motivates several authors to define distance-based features for facial recognition. Samir et al. [28] use the level curves of the surface distance function (from the tip of the nose) as features for face recognition. Since an open mouth affects the shape of some level curves, this method is not able to handle the problem of missing data due to occlusion or pose variations. A similar polar parametrization of the facial surface is proposed in [24] where the authors study local geometric attributes under this parameterization. To deal with the open mouth problem, they modify the parametrization by disconnecting the top and bottom lips. The main limitation of this approach is the need for detecting the lips, as proposed in [5]. Beretti et al. [2] use surface distances to define facial stripes which, in turn, is used as nodes in a graph-based recognition algorithm.
The main limitation of these approaches, apart from the issues resulting from open mouths, is that they assume that surface distances between facial points are preserved within face classes. This is not valid in the case of large expressions. Actually, face expressions result from the stretching or the shrinking of underlying muscles and, consequently, the facial skin is deformed in a non-isometric manner. In other words, facial surfaces are also stretched or compressed locally, beyond a simple bending of parts.

In order to demonstrate this assertion, we placed four markers on a face and tracked the changes in the surface and Euclidean (straight line) distances between the markers under large expressions. Fig. 2 shows some facial expressions leading to a significant shrinking or stretching of the skin surface and, thus, causing both Euclidean and surface distances between these points to change. In one case these distances decrease (from 113 mm to 103 mm for the Euclidean distance, and from 115 mm to 106 mm for the surface distance) while in the other two cases they increase. This clearly shows that large expressions can cause stretching and shrinking of facial surfaces, i.e., the facial deformation is elastic in nature. Hence, the assumption of an isometric deformation of the shape of the face is not strictly valid, especially for large expressions. This also motivates the use of elastic shape analysis in 3D face recognition.

![Image of facial expressions showing distance changes](image.png)

**Fig. 2.** Significant changes in both Euclidean and surface distances under large facial expressions.

### 1.2 Overview of Our Approach

This paper presents a Riemannian framework for 3D facial shape analysis. This framework is based on elastically matching and comparing radial curves emanating from the tip of the nose and it handles several of the problems described above. The main contributions of this paper are:

- It extracts, analyzes, and compares the shapes of radial curves of facial surfaces.
- It develops an elastic shape analysis of 3D faces by extending the elastic shape analysis of curves [30] to 3D facial surfaces.
- To handle occlusions, it introduces an occlusion detection and removal step based on recursive-ICP.
- To handle the missing data, it introduces a restoration step that uses statistical estimation on shape manifolds of curves. Specifically, it uses PCA on tangent spaces of the shape manifold to model the normal curves and uses that model to complete the partially-observed curves.

The different stages and components of our method are laid out in Fig. 3. While some basic steps are common to all application scenarios, there are also some specialized tools suitable only for specific situations. The basic steps that are common to all situations include 3D scan preprocessing (nose tip localization, filling holes, smoothing, face cropping), coarse and fine alignment, radial curve extraction, quality filtering, and elastic shape analysis of curves (Component III and quality module in Component II). This basic setup is evaluated on the FRGCv2 dataset following the standard protocol (see Section 4.2). It is also tested on the GAVAB dataset where, for each subject, four probe images out of nine have large pose variations (see Section 4.3). Some steps are only useful where one anticipates some data occlusion and missing data. These steps include occlusion detection (Component I) and missing data restoration (Component II). In these situations, the full processing includes Components I+II+III to process the given probes. This approach has been evaluated on a subset of the Bosphorus dataset that involves occlusions (see Section 4.4). In the last two experiments, except for the manual detection of nose coordinates, the remaining processing is automatic.

### 2 Radial, Elastic Curves: Motivation

Since an important contribution of this paper is its novel use of radial facial curves studied using elastic shape analysis.

#### 2.1 Motivation for Radial Curves

Why should one use the radial curves emanating from the tip of the nose for representing facial shapes? Firstly, why curves and not other kinds of facial features? Recently, there has been significant progress in the analysis of curves shapes and the resulting algorithms are very sophisticated and efficient [30], [33]. The changes in facial expressions affect different regions of a facial surface differently. For example, during a smile, the top half of the face is relatively unchanged while the lip area changes a lot, and when a person is surprised the effect is often the opposite. If chosen appropriately, curves have the potential to capture regional shapes and that is why their role becomes important. The locality of shapes represented by facial curves is an important reason
for their selection. The next question is: Which facial curves are suitable for recognizing people? Curves on a surface can, in general, be defined either as the level curves of a function or as the streamlines of a gradient field. Ideally, one would like curves that maximally separate inter-class variability from the intra-class variability (typically due to expression changes). The past usage of the level curves (of the surface distance function) has the limitation that each curve goes through different facial regions and that makes it difficult to isolate local variability. Actually, the previous work on shape analysis of facial curves for 3D face recognition was mostly based on level curves [27], [28].

In contrast, the radial curves with the nose tip as origin have a tremendous potential. This is because: (i) the nose is in many ways the focal point of a face. It is relatively easy and efficient to detect the nose tip (compared to other facial parts) and to extract radial curves, with nose tip as the center, in a completely automated fashion. It is much more difficult to automatically extract other types of curves, e.g., those used by sketch artists (cheek contours, forehead profiles, eye boundaries, etc). (ii) Different radial curves pass through different regions and, hence, can be associated with different facial expressions. For instance, differences in the shapes of radial curves in the upper-half of the face can be loosely attributed to the inter-class variability while those for curves passing through the lips and cheeks can largely be due to changes in expressions. This is illustrated in Fig. 4 which shows a neutral face (left), a smiling face (middle), and a surprised face (right). The main difference in the middle face, relative to the left face, lies in the lower part of the face, while for the right face the main differences lie in the top half. (iii) Radial curves have a more universal applicability. The curves used in the past have worked well for some specific tasks, e.g., lip contours in detecting certain expressions, but they have not been as efficient for some other tasks, such as face recognition. In contrast, radial curves capture the full geometry and are applicable to a variety of applications, including facial expression recognition. (iv) In the case of the missing parts and partial occlusion, at least some part of every radial curve is usually available. It is rare to miss a full radial curve. In contrast, it is more common to miss an eye due to occlusion by glasses, the forehead due to hair, or parts of cheeks due to a bad angle for laser reflection. This issue is important in handling the missing data via reconstruction, as shall be described later in this paper. (v) Natural face deformations
are largely (although not exactly) symmetric and, to a limited extent, are radial around the nose. Based on these arguments, we choose a novel geometrical representation of facial surfaces using radial curves that start from the nose tip.

### 2.2 Motivation for Elasticity

Consider the two parameterized curves shown in Fig. 5; call them $\beta_1$ and $\beta_2$. Our task is to automatically match points on these radial curves associated with two different facial expressions. The expression on the left has the mouth open whereas the expression on the right has the mouth closed. In order to compare their shapes, we need to register points across those curves. One would like the correspondence to be such that geometric features match across the curves as well as possible. In other words, the lips should match the lips and the chin should match the chin. Clearly, if we force an arc-length parameterization and match points that are at the same distance from the starting point, then the resulting matching will not be optimal. The points A and B on $\beta_1$ will not match the points $A'$ and $B'$ on $\beta_2$ as they are not placed at the same distances along the curves. For curves, the problem of optimal registration is actually the same as that of optimal re-parameterization. This means that we need to find a re-parameterization function $\gamma(t)$ such that the point $\beta_1(t)$ is registered with the point $\beta_2(\gamma(t))$, for all $t$. The question is how to find an optimal $\gamma$ for an arbitrary $\beta_1$ and $\beta_2$? Keep in mind that the space of all such $\gamma$s is infinite dimensional because it is a space of functions.

As described in [30], this registration is accomplished by solving an optimizing problem using the dynamic programming algorithm, but with an objective function that is developed from a Riemannian metric. The chosen metric, termed an elastic metric, has a special property that the same re-parameterization of two curves does not change the distance between them. This, in turn, enables us to fix the parameterization of one curve arbitrarily and to optimize over the parameterization of the other. This optimization leads to a proper distance (geodesic distance) and an optimal deformation (geodesic) between the shapes of curves. In other words, it results in their elastic comparisons. Please refer to [30] for details.

### 2.3 Automated Extraction of Radial Curves

Each facial surface is represented by an indexed collection of radial curves that are defined and extracted as follows. Let $S$ be a facial surface obtained as an output of the preprocessing step. The reference curve on $S$ is chosen to be the vertical curve after the face has been rotated to the upright position. Then, a radial curve $\beta_\alpha$ is obtained by slicing the facial surface by a plane $P_\alpha$ that has the nose tip as its origin and makes an angle $\alpha$ with the plane containing the reference curve. That is, the intersection of $P_\alpha$ with $S$ gives the radial curve $\beta_\alpha$. We repeat this step to extract radial curves from $S$ at equally-separated angles, resulting in a set of curves that are indexed by the angle $\alpha$. Fig. 6 shows an example of this process.

If needed, we can approximately reconstruct $S$ from these radial curves according to $S \approx \cup_\alpha \beta_\alpha = \cup_\alpha \{ S \cap P_\alpha \}$. In the later experiments, we have used 40 curves to represent a surface. Using these curves, we will demonstrate that the elastic framework is well suited to modeling of deformations associated with changes in facial expressions and for handling missing data.

In our experiments, the probe face is first rigidly aligned to the gallery face using the ICP algorithm. In this step, it is useful but not critical to accurately find the nose tip on the probe face. As long as there is a sufficient number of distinct regions available on the probe face, this alignment can be performed. Next, after the alignment, the radial curves on the probe model are extracted using the plane $P_\alpha$ passing through the nose tip of the gallery model at an angle $\alpha$ with the vertical. This is an important point in that only the nose tip of the gallery and a good alignment between gallery-probe is needed to extract good quality curves. Even if some parts of the probe...
face are missing, including its nose region, this process can still be performed. To demonstrate this point, we take session #0405d222, from the FRGCv2 dataset, in which some parts of the nose are missing and are filled using a linear interpolation filter (top row of Fig. 7). The leftmost panel shows the hole-filled probe face, the next panel shows the gallery face, the third panel shows its registration with the gallery face and extracted curves on the gallery face. The last panel shows the extracted curves for the probe face. As shown there, the alignment of the gallery face with the probe face is good despite a linear interpolation of the missing points. Then, we use the gallery nose coordinates to extract radial curves on the probe surface. The gallery face in this example belongs to the same person under the same expression. In the second row, we show an example where the two faces belong to the same person but represent different expressions/pose. Finally, in the last row we show a case where the probe and the gallery faces belong to different persons. Since the curve extraction on the probe face is based on the gallery nose coordinates which belongs to another person, the curves may be shifted in this nose region. However, this small inaccuracy in curve extraction is actually helpful since it increases the inter-class distances and improves the biometric performance.

![Fig. 7. Curves extraction on a probe face after its rigid alignment with a gallery face. In (a), the nose region of the probe is missing and filled using linear interpolation. The probe and gallery faces are from the same class for (a) and (b), while they are from different classes for (c).](image)

2.4 Curve Quality Filter

In situations involving non-frontal 3D scans, some curves may be partially hidden due to self occlusion. The use of these curves in face recognition can severely degrade the recognition performance and, therefore, they should be identified and discarded. We introduce a quality filter that uses the continuity and the length of a curve to detect such curves. To pass the quality filter, a curve should be one continuous piece and have a certain minimum length, say of, 70mm. The discontinuity or the shortness of a curve results either from missing data or large noise.

We show two examples of this idea in Fig. 8 where we display the original scans, the extracted curves, and then the action of the quality filter on these curves. Once the quality filter is applied and the high-quality curves retained, we can perform face recognition procedure using only the remaining curves. That is, the comparison is based only on curves that have passed the quality filter. Let \( \beta \) denotes a facial curve, we define the boolean function \( \text{quality}(\beta) = 1 \) if \( \beta \) passes the quality filter and \( \text{quality}(\beta) = 0 \) otherwise. Recall that during the pre-processing step, there is a provision for filling holes. Sometimes the missing parts are too large to be faithfully filled using linear interpolation. For this reason, we need the quality filter that will isolate and remove curves associated with those parts.

3 Shape Analysis of Facial Surfaces

In this section we will start by summarizing a recent work in elastic shape analysis of curves and extend it to shape analysis of facial surfaces.

3.1 Background on the Shapes of Curves

Let \( \beta : I \rightarrow \mathbb{R}^3 \), represent a parameterized curve on the face, where \( I = [0, 1] \). To analyze the shape of \( \beta \), we shall represent it mathematically using the square-root velocity function (SRVF) \([30]\), denoted by \( q(t) = \frac{\dot{\beta}(t)}{\sqrt{|\dot{\beta}(t)|}} \); \( q(t) \) is a special function of \( \beta \) that simplifies computations under elastic metric. More precisely, as shown in \([30]\), an elastic metric for comparing shapes of curves becomes the simple \( L^2 \)-metric under the SRVF representation. (A similar metric and representation for curves was also developed by Younes et
al. [33] but it only applies to planar curves and not to facial curves). This point is very important as it simplifies the analysis of curves, under the elastic metric, to the standard functional analysis. Furthermore, under $L^2$-metric, the re-parametrization group acts by isometries on the manifold of $q$ functions, which is not the case for the original curve $\beta$. To elaborate on the last point, let $q$ be the SRVF of a curve $\beta$. Then, the SRVF of a re-parametrized curve $\beta \circ \gamma$ is given by $\sqrt{\gamma}(q \circ \gamma)$. Here $\gamma : I \to I$ is a re-parametrization function and let $\Gamma$ be the set of all such functions. Now, if $q_1$ and $q_2$ are SRVFs of two curves $\beta_1$ and $\beta_2$, respectively, then it is easy to show that under the $L^2$ norm, $\|q_1 - q_2\| = \|\sqrt{\gamma_1}(q_1 \circ \gamma) - \sqrt{\gamma_2}(q_2 \circ \gamma)\|$, for all $\gamma \in \Gamma$, while $\|\beta_1 - \beta_2\| \neq \|\beta_1 \circ \gamma - (\beta_2 \circ \gamma)\|$ in general. This is one more reason why SRVF is a better representation of curves than $\beta$ for shape analysis.

Define the pre-shape space of such curves: $\mathcal{C} = \{q : I \to \mathbb{R}^3 | \|q\| = 1\} \subset L^2(I, \mathbb{R}^3)$, where $\|\cdot\|$ implies the $L^2$ norm. With the $L^2$ metric on its tangent spaces, $\mathcal{C}$ becomes a Riemannian manifold. Also, since the elements of $\mathcal{C}$ have a unit $L^2$ norm, $\mathcal{C}$ is a hypersphere in the Hilbert space $L^2(I, \mathbb{R}^3)$. Furthermore, the geodesic path between any two points $q_1, q_2 \in \mathcal{C}$ is given by the great circle, $\psi : [0, 1] \to \mathcal{C}$, where

$$
\psi(\tau) = \frac{1}{\sin(\theta)} (\sin((1 - \tau)\theta)q_1 + \sin(\theta \tau)q_2), \quad (1)
$$

and the geodesic length is $\theta = d_c(q_1, q_2) = \cos^{-1}(\langle q_1, q_2 \rangle)$.

In order to study shapes of curves, one should identify all rotations and re-parametrizations of a curve as an equivalence class. Define the equivalence class of $q$ as: $[q] = \text{closure}([\gamma(t)]) : O \in \text{SO}(3), \gamma \in \Gamma$. The set of such equivalence classes, denoted by $\mathcal{S} = \{[q] | q \in \mathcal{C}\}$ is called the shape space of open curves in $\mathbb{R}^3$. As described in [30], $\mathcal{S}$ is a metric space with the metric inherited from the larger space $\mathcal{C}$. To obtain geodesics and geodesic distances between elements of $\mathcal{S}$, one needs to solve the optimization problem:

$$
(O^*, \gamma^*) = \arg\min_{(O, \gamma) \in \text{SO}(3) \times \Gamma} d_c(q_1, \sqrt{\gamma}O(q_2 \circ \gamma)). \quad (2)
$$

For a fixed $O$ in $\text{SO}(3)$, the optimization over $\Gamma$ is done using the dynamic programming algorithm while, for a fixed $\gamma \in \Gamma$, the optimization over $\text{SO}(3)$ is performed using SVD. By iterating between these two, we can reach a solution for the joint optimization problem. Let $q_3(t) = \sqrt{\gamma^*(t)}O^*q_2(\gamma^*(t))$ be the optimal element of $[q_2]$, associated with the optimal rotation $O^*$ and re-parametrization $\gamma^*$ of the second curve, then the geodesic distance between $[q_1]$ and $[q_2]$ in $\mathcal{S}$ is $d_s([q_1], [q_2]) = d_c(q_1, q_3)$ and the geodesic is given by Eqn. 1, with $[q_2]$ replaced by $q_3$.

### 3.2 Shape Metric for Facial Surfaces

Now we extend the framework from radial curves to full facial surfaces. A facial surface $S$ is represented by an indexed collection of radial curves, indexed by the $n$ uniform angles $\mathcal{A} = \{0, \frac{2\pi}{n}, \frac{4\pi}{n}, \ldots, 2\pi(n-1)\}$. Thus, the shape of a facial surface can be represented as an element of the set $\mathcal{S}^n$. The indexing provides a correspondence between curves across faces. For example, the curve at an angle $\alpha$ on a probe face is compared with the curve at the same angle on a gallery face. Thus, the distance between two facial surfaces is $d_s : \mathcal{S}^n \times \mathcal{S}^n \to \mathbb{R}_{\geq 0}$ given by $d_s(S^1, S^2) = \frac{1}{n} \sum_{\alpha \in \mathcal{A}} d_s([q^1_\alpha], [q^2_\alpha])$. Here, $q^i_\alpha$ denotes the SRVF of the radial curve $\beta^i_\alpha$ on the $i^{th}$ facial surface. The distance $d_s$ is computed by the following algorithm.

**Input:** Facial surfaces $S_1$ and $S_2$.

**Output:** The distance $d_s$.

For $i \leftarrow 1 \text{ to } 2$ do

for $\alpha \leftarrow 0 \text{ to } 2\pi$ do

Extract the curve $\beta^*_\alpha$.

if $\text{quality}(\beta^*_1) = 1$ and $\text{quality}(\beta^*_2) = 1$ then

Compute the optimal rotation and re-parameterization alignment $O^*$ and $\gamma^*_\alpha$ using Eqn. 2.

set $q^*_\alpha(t) = \sqrt{\gamma^*_\alpha}(t)O^*q^*_\alpha(\gamma^*_\alpha(t))$.

compute

$$
d_s([q^1_\alpha], [q^2_\alpha]) = \cos^{-1}(\langle q^1_\alpha, q^2_\alpha \rangle).
$$

end

Compute $d_s = \frac{1}{n} \sum_{\alpha \in \mathcal{A}} d_s([q^1_\alpha], [q^2_\alpha])$, where $n$ is the number of valid pairs of curves.

end

**Algorithm 1:** Elastic distance computation.

Since we have deformations (geodesic paths) between corresponding curves, we can combine these deformations to obtain deformations between full facial surfaces. In fact, these full deformations can be shown to be formal geodesic paths between faces, when represented as elements of $\mathcal{S}^n$. Shown in Fig. 9 are examples of some geodesic paths between source and target faces. The three top rows illustrate paths between faces of different subjects, and are termed inter-class geodesics whereas the remaining rows illustrate paths between faces of the same person conveying different expressions, and are termed intra-class geodesics.

These geodesics provide a tangible benefit, beyond the current algorithms that provide some kind of a similarity score for analyzing faces. In addition to their interpretation as optimal deformations under the chosen metric, the geodesics can also be used for computing the mean shape and measuring the shape covariance of a set of faces, as illustrated later. To demonstrate the quality of this deformation, we compare it qualitatively for faces with the deformation obtained using a linear interpolation between registered points under an ICP registration of points, in Fig. 10. The three rows show, respectively, a geodesic path in the shape space, the corresponding path in the pre-shape space, and a path using ICP. Algorithm 1
is used to calculate the geodesic path in the shape space. In other words, the optimal matching (reparameterization) between curves is established and, thus, anatomical points well matched across the two surfaces. The upper lips match the upper lips, for instance, and this helps produce a natural opening of the mouth as illustrated in the top row in Fig. 10. However, the optimal matching is not established yet when the geodesic is calculated in the pre-shape space. This results in an unnatural deformation along the geodesic in the mouth area.

3.3 Computation of the Mean Shape

As mentioned above, an important advantage of our Riemannian approach over many past papers is its ability to compute summary statistics of a set of faces. For example, one can use the notion of Karcher mean [14] to define an average face that can serve as a representative face of a group of faces. To calculate a Karcher mean of facial surfaces \( \{ S^1, ..., S^k \} \) in \( S^n \), we define an objective function: \( \mathcal{V} : S^n \to \mathbb{R}, \mathcal{V}(S) = \sum_{i=1}^{k} d_S(S^i, S)^2 \). The Karcher mean is then defined by: 

\[
\tilde{S} = \arg \min_{S \in S^n} \mathcal{V}(S).
\]

The algorithm for computing Karcher mean is a standard one, see e.g. [8], and is not repeated here to save space. This minimizer may not be unique and, in practice, one can pick any one of those solutions as the mean face. This mean has a nice geometrical interpretation: \( \tilde{S} \) is an element of \( S^n \) that has the smallest total (squared) deformation from all given facial surfaces \( \{ S^1, ..., S^k \} \). An example of a Karcher mean face for eight faces belonging to different people is shown in Fig. 11.

3.4 Completion of Partially-Obscured Curves

Earlier we have introduced a filtering step that finds and removes curves with missing parts. Although this step is effective in handling some missing parts, it may not be sufficient when parts of a face are missing due to external occlusions, such as glasses and hair. In the case of external occlusions, the majority of radial curves could have hidden parts that should be predicted before using these curves. This problem is more challenging than self-occlusion because, in addition to the missing parts, we can also have parts of the occluding object(s) in the scan. In a non-cooperative situation, where the acquisition is unconstrained, there is a high probability for this kind of occlusion to occur. Once we detect points that belong to the face and points that belong to the occluding object, we first remove the occluding object and use a statistical model in the shape space of radial curves to complete the broken curves. This replaces the parts of face that have been occluded using information from the visible part and the training data.

The core of this problem, in our representation of facial surfaces by curves, is to take a partial facial curve and predict its completion. The sources of information available for this prediction are: (1) the current
(partially observed) curve and (2) several (complete) training curves at the same angle that are extracted from full faces. The basic idea is to develop a sparse model for the curve from the training curves and use that to complete the observed curve. To keep the model simple, we use the PCA of the training data, in an appropriate vector space, to form an orthogonal basis representing training shapes. Then, this basis is used to estimate the coefficients of the observed curve and the coefficients help reconstruct the full curve. Since the shape space of curve $S$ is nonlinear, we use the tangent space $T_{\mu}(S)$, where $\mu$ is the mean of the training shapes, to perform PCA. Let $\alpha$ denote the angular index of the observed curve, and let $q_{\alpha}^1, q_{\alpha}^2, \ldots, q_{\alpha}^k$ be the SRVF s of the curves taken from the training faces at that angle. As described earlier, we can compute the sample Karcher mean of the training shapes, to perform PCA. Let $\mu$ denote the mean of the training shapes, as discussed earlier. A PCA of the tangent vectors $\{v_i\}$ leads to the principal basis vectors $u_{1,\alpha}, u_{2,\alpha}, \ldots, u_{J,\alpha}$, where $J$ represents the number of significant basis elements.

Now returning to the problem of completing a partially-occluded curve, let us assume that this curve is observed for parameter value $t$ in $[0, \tau] \subset [0, 1]$. In other words, the SRVF of this curve $q(t)$ is known for $t \in [0, \tau]$ and unknown for $t > \tau$. Then, we can estimate the coefficients of $q$ under the chosen basis according to $c_{j,\alpha} = \langle q_{\alpha}, u_{j,\alpha} \rangle \approx \int_0^\tau \langle q(t), u_{j,\alpha}(t) \rangle \, dt$, and estimate the SRVF of the full curve according to

$$
\hat{q}_\alpha(t) = \sum_{j=1}^J c_{j,\alpha} u_{j,\alpha}(t), \quad t \in [0, 1].
$$

We present three examples of this procedure in Fig. 12, with each face corrupted by an external occlusion as shown in column (a). The detection and removal of occluded parts is performed as described in the previous section, and the result of that step is shown in column (b). Finally, the curves passing through the missing parts are restored and shown in (c).

In order to evaluate this reconstruction step, we have compared the restored surface (shown in the top row of Fig. 12) with the complete neutral face of that class, as shown in Fig. 13. The small values of both absolute deviation and signed deviation, between the restored face and the corresponding face in the gallery, demonstrate the success of the restoration process.

In the remainder of this paper, we will apply this comprehensive framework for 3D face recognition using a variety of well known and challenging datasets.

**4 EXPERIMENTAL RESULTS**

In the following we provide a comparative performance analysis of our method with other state-of-the-art solutions, using three datasets: the FRGC v2.0 dataset, the GavabDB, and the Bosphorus dataset.

**4.1 Data Preprocessing**

Since the raw data contains a number of imperfections, such as holes, spikes, and include some undesired parts, such as clothes, neck, ears and hair, the data pre-processing step is very important and non-trivial. As illustrated in Fig. 14, this step includes the following items:

- The hole-filling filter identifies and fills holes in input meshes. The holes are created either because of the absorption of laser in dark areas, such as eyebrows and mustaches, or self-occlusion or...
open mouths. They are identified in the input mesh by locating boundary edges, linking them together into loops, and then triangulating the resulting loops.

- A cropping filter cuts and returns parts of the mesh inside an Euclidean sphere of radius $75\text{mm}$ centered at the nose tip, in order to discard as much hair as possible. The nose tip is automatically detected for frontal scans and manually annotated for scans with occlusions and large pose variation.

- A smoothing filter reduces high frequency components (spikes) in the mesh, improves the shapes of cells, and evenly distributes the vertices on a facial mesh.

We have used functions provided in the VTK (www.vtk.org) library to develop these filters.

### 4.2 Comparative Evaluation on the FRGCv2 Dataset

For the first evaluation we use the FRGCv2 dataset in which the scans have been manually clustered into three categories: neutral expression, small expression, and large expression. The gallery consists of the first scans for each subject in the database, and the remaining scans make up the probe faces. This dataset was automatically preprocessed as described in the Section 4.1. Fig. 15 shows Cumulative Matching Curves (CMCs) of our method under this protocol for the three cases: neutral vs. neutral, neutral vs. non-neutral and neutral vs. all. Note that this method results in $97.7\%$ rank-1 recognition rate in the case of neutral vs. all. In the difficult scenario of neutral vs. expressions, the rank-1 recognition rate is $96.8\%$, which represents a high performance, while in the simpler case of neutral vs. neutral the rate is $99.2\%$.

A comparison of recognition performance of our method with several state-of-the-art results is presented in Table 1. This time, in order to keep the comparisons fair, we kept all the 466 scans in the gallery. Notice that our method achieved a $97\%$ rank-1 recognition which is close to the highest published results on this dataset [29], [26], [9]. Since the scans in FRGCv2 are all frontal, the ability of region-based algorithms, such as [9], [26], to deal with the missing parts is not tested in this dataset. For that end, one would need a systematic evaluation on a dataset with the missing data issues, e.g. the GavabDB. The best recognition score on FRGCv2 is reported by Spreeuw et al. [29] which uses an intrinsic coordinate system based on the vertical symmetry plane through the nose. The missing data due to pose variation and occlusion challenges will be a challenge there as well.

In order to evaluate the performance of the proposed approach in the verification scenario, the Receiver Operating Characteristic (ROC) curves for the ROC III mask of FRGCv2 and "all-versus-all" are plotted in Fig. 16. For comparison, Table 2 shows the verification results at false acceptance rate (FAR) of 0.1 percent for several methods. For the standard protocol testings, the ROC III mask of FRGCv2, we obtain the verification rates of around $97\%$, which is comparable to the best published results. In the all-versus-all experiment, our method provides $93.96\%$ VR at $0.1\%$ FAR, which is among the best rates in the table [26], [29], [32]. Note that these approaches are applied to FRGCv2 only. Since scans in FRGCv2 are mostly frontal and have high quality, many methods are able to provide good performance. It is, thus, important to evaluate a method in other situations where the data quality is not as good. In the next two sections, we will consider those situations with the GavabDB involving the pose variation and the Bosphorus dataset involving the occlusion challenge.

### 4.3 Evaluation on the GavabDB Dataset

Since GavabDB [21] has many noisy 3D face scans under large facial expressions, we will use that database to help evaluate our framework. This database consists of the Minolta Vi-700 laser range scans from 61 subjects – 45 male and 16 female – all of them Caucasian. Each subject was scanned nine times from different angles and under different facial expressions.

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**Fig. 14.** The different steps of preprocessing: acquisition, filling holes, cropping and smoothing

**Fig. 15.** The CMC curves of our approach for the following scenario: neutral vs. neutral, neutral vs. expressions and neutral vs. all.
TABLE 1
Comparison of rank-1 scores on the FRGCv2 dataset with the state-of-the-art results.

<table>
<thead>
<tr>
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</thead>
<tbody>
<tr>
<td></td>
<td>99%</td>
<td>98.3%</td>
<td>97%</td>
<td>94.1%</td>
<td>98.4%</td>
<td>97.2%</td>
<td>97%</td>
<td>97%</td>
</tr>
</tbody>
</table>

TABLE 2
Comparison of verification rates at FAR=0.1% on the FRGCv2 dataset with state-of-the-art results (the ROC III mask and the All vs. All scenario).

<table>
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<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>ROC III</td>
<td>97%</td>
<td>94.8%</td>
<td>96.6%</td>
<td>94.6%</td>
<td>98.4%</td>
<td>98.13%</td>
<td>93.96%</td>
</tr>
<tr>
<td>All vs. All</td>
<td>93.2%</td>
<td>81.2%</td>
<td>96.5%</td>
<td>94.6%</td>
<td>98.4%</td>
<td>98.13%</td>
<td>93.96%</td>
</tr>
</tbody>
</table>

Fig. 16. The ROC curves of our approach for the following scenario: All vs. All and the ROC III mask.

(six with the neutral expression and three with non-neutral expressions). The neutral scans include several frontal scans – one scan while looking up (+35 degree), one scan while looking down (-35 degree), one scan from the right side (+90 degree), and one from the left side (-90 degree). The non-neutral scans include cases of a smile, a laugh, and an arbitrary expression chosen freely by the subject. We point out that in these experiments the nose tips in profile faces have been annotated manually.

One of the two frontal scans with the neutral expression for each person is taken as a gallery model, and the remaining are used as probes. Table 3 compares the results of our method with the previously published results following the same protocol. As noted, our approach provides the highest recognition rate for faces with non-neutral expressions (94.54%). This robustness comes from the use of radial, elastic curves since: (1) each curve represents a feature that characterizes local geometry and, (2) the elastic matching is able to establish a correspondence with the correct alignment of anatomical facial features across curves.

Fig. 17 illustrates examples of correct and incorrect matches for some probe faces. In each case we show a pair of faces with the probe shown on the left and the top ranked gallery face shown on the right. These pictures also exhibit examples of the variability in facial expressions of the scans included in the probe dataset. As far as faces with the neutral expressions are concerned, the recognition accuracy naturally depends on their pose. The performance decreases for scans from the left or right sides because more parts are occluded in those scans. However, for pose variations up to 35 degrees the performance is still high (100% for looking up and 98.36% for looking down). Fig. 17 (top row) shows examples of successful matches for up and down looking faces and unsuccessful matches for sideways scans.

Table 3 provides an exhaustive summary of results obtained using GavabDB; our method outperforms the majority of other approaches in terms of the recognition rate. Note that there is no prior result in the literature on 3D face recognition using sideway-scans from this database. Although our method works well on common faces with a range of pose variations within 35 degrees, it can potentially fail when a large part of the nose is missing, as it can cause an incorrect alignment between the probe and the gallery. This situation occurs if the face is partially occluded by external objects such as glasses, hair, etc. To solve this problem, we first restore the data missing due to occlusion.

4.4 3D Face Recognition on the Bosphorus Dataset: Recognition Under External Occlusion

In this section we will use components I (occlusion detection and removal) and II (missing data restora-
Fig. 18. Gradual removal of occluding parts in a face scan using Recursive-ICP.

In the case of faces with external occlusion, we first restore them and then apply the recognition procedure. That is, we detect and remove the occluded part, and recover the missing part resulting in a full face that can be compared with a gallery face using the metric $d_S$. The recovery is performed using the tangent PCA analysis and Gaussian models, as described in Section 3.4. In order to evaluate our approach, we perform this automatic procedure on the Bosphorus database [1]. We point out that for this dataset the nose tip coordinates are already provided. The Bosphorus database is suitable for this evaluation as it contains scans of 60 men and 45 women, 105 subjects in total, in various poses, expressions and in the presence of external occlusions (eyeglasses, hand, hair). The majority of the subjects are aged between 25 and 35. The number of total face scans is 4652; at least 54 scans each are available for most of the subjects, while there are only 31 scans each for 34 of them. The interesting part is that for each subject there are four scans with occluded parts. These occlusions refer to (i) mouth occlusion by hand, (ii) eyeglasses, (iii) occlusion of the face with hair, and (iv) occlusion of the left eye and forehead regions by hands. Fig. 19 shows sample images from the Bosphorus 3D database illustrating a full scan on the left and the remaining scans with typical occlusions.

We pursued the same evaluation protocol used in the previously published papers: a neutral scan for each person is taken to form a gallery dataset of size 105 and the probe set contains 381 scans that have occlusions. The training is performed using other sessions so that the training and test data are disjoint. The rank-1 recognition rate is reported in Fig. 20 for different approaches depending upon the type of occlusion. As these results show the process of restoring occluded parts significantly increases the accuracy of recognition. The rank-1 recognition rate is 78.63% when we remove the occluded parts and apply the recognition algorithm using the remaining parts, as described in Section 2.4. However, if we

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<tbody>
<tr>
<td>Neutral</td>
<td>96.67%</td>
<td>90.16%</td>
<td>72%</td>
<td>-</td>
<td>100%</td>
</tr>
<tr>
<td>Expressive</td>
<td>93.33%</td>
<td>77.5%</td>
<td>72%</td>
<td>-</td>
<td>94.54%</td>
</tr>
<tr>
<td>Neutral+expressive</td>
<td>94.68%</td>
<td>-</td>
<td>78%</td>
<td>-</td>
<td>95.9%</td>
</tr>
<tr>
<td>Rotated looking down</td>
<td>-</td>
<td>-</td>
<td>85.3%</td>
<td>-</td>
<td>100%</td>
</tr>
<tr>
<td>Rotated looking up</td>
<td>-</td>
<td>-</td>
<td>88.6%</td>
<td>-</td>
<td>98.36%</td>
</tr>
<tr>
<td>Overall</td>
<td>-</td>
<td>-</td>
<td>98%</td>
<td>81.67%</td>
<td>96.99%</td>
</tr>
<tr>
<td>Scans from right side</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>70.49%</td>
</tr>
<tr>
<td>Scans from left side</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>86.89%</td>
</tr>
</tbody>
</table>
perform restoration, the recognition rate is improved to 87.06%. Clearly, this improvement in performance is due to the estimation of missing parts on curves. These parts, that include important shape data, were not considered by the algorithm described earlier. Even if the part added with restoration introduces some error, it still allows us to use the shapes of the partially observed curves. Furthermore, during restoration, the shape of the partially observed curve is conserved as much as possible.

Examples of 3D faces recognized by our approach are shown in Fig. 12, along with different steps of the algorithm. The faces in the two bottom rows are examples of incorrectly recognized faces by our algorithm without restoration (as described earlier), but after the restoration step, they are correctly recognized. Aluz et al [1] reported a 93.69% rank-1 recognition rate overall for this database using the same protocol that we have described above. While this reported performance is very good, their processing has some manual components. Actually, the authors partition the face manually and fuse the scores for matching different parts of the face together. In order to compare with Colombo et al. [6], we reduce the probe dataset to 360 by discarding bad quality scans as Colombo et al. [6] did. Our method outperforms their approach with an overall performance of 89.25%, although individually our performance is worse in the case of occlusion by hair. It is difficult, in this case, to completely overcome face occlusion. Therefore, during the restoration step, our algorithm tries to keep majority of parts. This leads to a deformation in the shape of curves and, hence, affects the recognition accuracy. We present some examples of unrecognized faces in the case of occlusion by hair in Fig. 21. In this instance, the removal of curves passing through occlusion is better than restoring them as illustrated in Fig. 20.

5 Discussion

In order to study the performance of the proposed approach in presence of different challenges, we have presented experimental results using three well-known 3D face databases. We have obtained competitive results relative to the state of the art for 3D face recognition in presence of large expressions, non-frontal views and occlusions. As listed in Table 4, our fully automatic results obtained on the FRGCv2 are near the top. Table 4 also reports the computational time of our approach and some state of the art methods on the FRGCv2 dataset. For each approach, we report the time needed for preprocessing and/or feature extraction in the first column. In the second column we report the time needed to compare two faces. The third column is the sum of the two previous computation times for each approach. In the last column, we report the accuracy (recognition rate on FRGCv2) of different approaches. Regarding computational efficiency, parallel techniques can also be exploited to improve performance of our approach since the computation of curve distances, preprocessing, etc, are independent tasks.

Table 4: Comparative study of time implementations and recognition accuracy on FRGCGv2 of the proposed approach with state-of-the-art.

<table>
<thead>
<tr>
<th>Approach</th>
<th>preprocessing (s)</th>
<th>Face matching (s)</th>
<th>Comparison time (s)</th>
<th>Accuracy (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Wong et al. [32]</td>
<td>1.48</td>
<td>0.65</td>
<td>2.2</td>
<td>98.3%</td>
</tr>
<tr>
<td>Suppakom [29]</td>
<td>2.5</td>
<td>1</td>
<td>11</td>
<td>99%</td>
</tr>
<tr>
<td>This work</td>
<td>6.18</td>
<td>1.27</td>
<td>7.45</td>
<td>97%</td>
</tr>
<tr>
<td>Faltemier et al. [9]</td>
<td>7.52</td>
<td>2.4</td>
<td>9.92</td>
<td>97.2%</td>
</tr>
<tr>
<td>Faltemier et al. [13]</td>
<td>1.5</td>
<td>17000</td>
<td>15</td>
<td>97%</td>
</tr>
<tr>
<td>Faes et al. [11]</td>
<td>1</td>
<td>2</td>
<td>3</td>
<td>97%</td>
</tr>
<tr>
<td>Berrett et al. [2]</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>94.1%</td>
</tr>
<tr>
<td>Queirolo et al. [26]</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>98.4%</td>
</tr>
</tbody>
</table>

In the case of GavabDB and Bosphorus, the nose tip was manually annotated for non frontal and occluded faces. In the future, we hope to develop automatic nose tip detection methods for non frontal views and for faces that have undergone occlusion.

6 Conclusion

In this paper we have presented a framework for a statistical shape analysis of facial surfaces. We have also presented results on 3D face recognition designed to handle variations of facial expression, pose variations and occlusions between gallery and probe scans. This method has several properties that make it appropriate for 3D face recognition in non-cooperative scenarios. Firstly, to handle pose variation and missing data, we have proposed a local representation by using a curve representation of a 3D face and a quality filter for selecting curves. Secondly, to handle variations in facial expressions, we have proposed an elastic shape analysis of 3D faces. Lastly, in the presence of occlusion, we have proposed to remove the occluded parts then to recover only the missing data on the 3D scan using statistical shape models. That is, we have constructed a low dimensional shape subspace for each element of the indexed collection of curves.
and then represent a curve (with missing data) as a linear combination of its basis elements.

ACKNOWLEDGEMENTS
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REFERENCES


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**Fig. 20.** Recognition results on the Bosphorus database and comparison with state-of-the-art approaches.


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