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# When do textbooks matter for achievement? Evidence from African primary schools 

Maria Kuecken* Marie-Anne Valfort ${ }^{\dagger}$

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#### Abstract

Using a within-student analysis, we find no average impact of textbook access (ownership or sharing) on primary school achievement. Instead, it is only for students with high socioeconomic status that one form of textbook access - sharing - has a positive impact. Keywords: Textbooks, Educational quality, Sub-Saharan Africa, SACMEQ JEL: A12, I21, N37


[^0]
## 1 Introduction

Improving access to textbooks via ownership or sharing seems an obvious way to increase student achievement in African countries where resources are particularly limited. Retrospective studies of both Francophone and Anglophone African countries find significant positive correlations between access to textbooks and student test scores in both reading and mathematics. ${ }^{1}$ However, such analyses are at risk from bias due to omitted variables that may influence both textbook access and educational outcomes. Alternatively, randomized experiments have allowed researchers to avoid such endogeneity biases and isolate the impact of schooling inputs on learning outcomes. Glewwe, Kremer and Moulin (2009) analyze the only randomized experiment conducted in Africa that focuses on the impact of textbook access, specifically sharing, on pupils' achievement. They find that, due in part to overly-ambitious curricula not suited for the average student, textbook sharing in Kenya improves test scores only for those students who were already high achievers prior to the intervention. ${ }^{2}$

Our paper aims to improve upon this result in two ways. First, we do not restrict our attention to the impact of textbook sharing alone. Instead, we expand our analysis to include textbook ownership as these two forms of textbook access are expected to create differential effects. For instance, Frölich and Michaelowa (2011) demonstrate, based on African data, that textbook sharing is associated with positive externalities (notably through knowledge sharing) which simple textbook ownership does not allow. Second, instead of relying on only one African country, we cover eleven Sub-Saharan African countries from the second round of the Southern and Eastern African Consortium for Monitoring Educational Quality (SACMEQ) survey from 2005. ${ }^{3}$ Our identification strategy treats endogeneity through a within-student analysis (across subject rather than across time). Doing so ensures that there are no unobserved student characteristics which are correlated with both textbook access and

[^1]achievement, at least when these unobservables remain constant across subjects. ${ }^{4}$ Moreover, with a rich set of controls at the teacher level, we mitigate the possibility of unobserved teacher characteristics being correlated with both textbook access and test scores.

## 2 Data

The SACMEQ II survey administers questionnaires and standardized reading and mathematics examinations to both students and teachers to compare cross-country achievement in the final year of primary school. We measure achievement with the scores obtained by students on standardized tests in reading and mathematics. For textbook access we use an indicator variable which is equal to 1 if a student has access to a textbook in mathematics or reading (whether via ownership or sharing) and 0 if a student has no access to a textbook. We then disaggregate this variable into two dummies: one that is equal to 1 if a student owns a textbook (and 0 if a student has no access to a textbook) and another that is is equal to 1 if a student shares a textbook (and 0 if a student has no access to a textbook). We do so in order to examine the potentially different effects of textbook ownership versus sharing.

Glewwe, Kremer and Moulin (2009) find that textbook access in Kenya improves test scores only for those students who were already high achievers before receiving textbook access. Yet, socioeconomic status is known to be an excellent predictor of academic ability. In Sub-Saharan Africa for instance, Lee, Zuze and Ross (2005) find that a pupil with a high SES strongly outperforms her low SES counterparts. We therefore test, later in the analysis, whether textbook access may make a significant difference only for students from the most privileged backgrounds. We do so by interacting our indicators for textbook access with student socioeconomic status, a proxy derived from an average of 14 home possessions (a newspaper, magazine, radio, television, VCR, cassette, telephone, refrigerator, car, motorcycle, bicycle, water, electricity, and table) present in each student's household.

When we run the within-student analysis, we need control only for the variables that vary across subjects. Regarding teachers, we account for sex (using an indicator for females), age, and highest level of academic qualification obtained (with dummy variables for primary, junior secondary, senior secondary, and A-level/tertiary). To control for characteristics related to teaching competency and practices, we use the raw teacher test scores in math and reading

[^2](with maximum scores of 41 and 47 respectively) as well as the frequency with which they correct homework (never, sometimes, always), importance they assign to encouraging their students (not important, of some importance, very important), and frequency with which they assess their students (no test, once per year, once per term, 2-3 times per term, 2-3 times per month, once or more per week). Additionally, we include a set of dummy variables for the presence of specific classroom resources (such as writing board, chalk, wall chart, cupboard or locker, one or more bookshelves, classroom library or book corner, teacher table, and teacher chair). Summary statistics for all variables can be found in Table A1.

## 3 Empirical strategy and results

Because, for each student, SACMEQ reports pairs of test scores in both math and reading, we are able to exploit these matched pairs by running a within-student analysis similar to Dee (2007), Aslam and Kingdon (2011) and Cho (2012). This analysis allows us to control for student fixed effects that are constant across subjects. Moreover, thanks to a comprehensive set of controls at the teacher level, this approach reduces the possibility that unobserved teacher characteristics are correlated with both a student's textbook access and their test scores. We begin with Equation (1):

$$
\begin{equation*}
Y_{i j}=a_{i}+b \cdot \mathrm{BOOK}_{i j}+c \cdot \mathrm{MATH}+\mathbf{X}_{\mathbf{j}}^{\prime} \cdot d+\epsilon_{i j} \tag{1}
\end{equation*}
$$

where $Y_{i j}$ represents the test score for student $i$ in subject $j$. We run three estimations in which the coefficient $b$ associated with BOOK stands for the impact of textbook access, ownership, or sharing on the score of student $i$. We control for student $\left(a_{i}\right)$ and subject (MATH) fixed effects, as well as for a vector of teacher traits $\left(\mathbf{X}_{\mathbf{j}}^{\prime}\right)$. Finally, we include the mean-zero error term $\left(\epsilon_{i j}\right)$ and cluster standard errors at the school level to account for the undoubtedly similar variation amongst students from the same school. Table 1 presents the OLS estimates of Equation (1). We observe that neither textbook access, textbook ownership nor textbook sharing has a significant impact on students' achievement. These results hold if we distinguish between the impact of textbook access in math versus reading. (Results available upon request).

However, it is possible that textbook access makes a significant difference only for students from the most privileged backgrounds due to severe constraints faced by poor students (such as hindered cognitive development, sporadic enrollment, low parent and teacher expectations,
and - particularly relevant for textbooks - elitist curriculum biases). ${ }^{5}$ We test for this possibility by adding to Equation (1) an interaction term between the indicators capturing textbook access and student SES, as proxied by average level of home possessions:

$$
\begin{equation*}
Y_{i j}=a_{i}+b \cdot \mathrm{BOOK}_{i j}+c \cdot \mathrm{BOOK}_{i j}^{*} \mathrm{SES}_{i}+d \cdot \mathrm{MATH}+\mathbf{X}_{\mathbf{j}}^{\prime} \cdot e+\epsilon_{i j} \tag{2}
\end{equation*}
$$

Here, the coefficient of the interaction term $\mathrm{BOOK}_{i j}^{*} \mathrm{SES}_{i}$ captures the differential impact of each textbook measure (access, ownership, or sharing) on a student's test score according to their level of home possessions. We test which percentile of SES is significant by running a Wald test. ${ }^{6}$ If we consider the $71^{\text {st }}$ percentile of home possessions for example, this Wald test consists of computing whether the sum of the coefficient of BOOK and the level of home possessions corresponding to the $71^{\text {st }}$ percentile (0.5) multiplied by the coefficient of BOOK*SES is significantly different from 0 .

OLS estimates of Equation (2) are reported in Table 2. They demonstrate that is it only for students belonging to the $71^{\text {st }}$ percentile of SES and above that one form of textbook access, textbook sharing, has a positive impact on achievement. The alternative textbook measures (access and ownership) have no effect at any level of student SES. This set of results holds if we distinguish between the impact of textbook access in math versus reading. (Results available upon request). In terms of magnitude, textbook sharing increases student test scores by a maximum of 0.20 standard deviations (the marginal effect obtained for students in the uppermost percentile of the SES distribution). When compared to other types of educational interventions, this impact is equivalent to that found from merit-based school vouchers (Kremer and Holla (2009)).

## 4 Conclusion

Relying on a within-student analysis, this paper aims to improve upon the representativeness of the results from Glewwe, Kremer and Moulin (2009) by (i) analyzing the impact of textbook ownership in addition to sharing and (ii) covering eleven Sub-Saharan African countries instead of one (Kenya). Our findings are consistent with theirs. We find no average impact of textbooks on student test scores although we identify a positive impact for a certain margin of students - those at the top of the socioeconomic distribution. Moreover,

[^3]this impact arises solely from textbook sharing. This result is consistent with the fact that sharing is associated with positive externalities via knowledge transfers, an effect that simple textbook ownership does not produce (see Frölich and Michaelowa (2011)).

## 5 Acknowledgements

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## 6 Tables

Table 1: Textbook access, ownership, or sharing and test scores: OLS results

|  | Dep. var.: Test scores |  |  |
| :---: | :---: | :---: | :---: |
|  | (1) | (2) | (3) |
| Student has access to a textbook | 0.790 (2.818) |  |  |
| Student owns a textbook |  | -2.163 (5.387) |  |
| Student shares a textbook |  |  | 3.060 (3.542) |
| Math | -3.152* (1.720) | -5.223* (2.722) | 0.597 (2.335) |
| Teacher gender (female) | 2.511 (2.356) | 1.667 (3.634) | 4.290 (3.522) |
| Teacher age | 0.219 (0.156) | 0.134 (0.207) | 0.206 (0.204) |
| Teacher qualification (junior secondary) | -3.741 (3.920) | -1.813 (5.728) | -7.771 (5.305) |
| Teacher qualification (senior secondary) | -3.846 (3.797) | -3.759 (5.712) | -5.937 (6.137) |
| Teacher qualification (A-level/tertiary) | -3.261 (4.504) | -3.654 (6.896) | -8.223 (6.893) |
| Teacher test score | 0.541*** (0.178) | 0.548* (0.286) | $0.527^{* *}$ (0.245) |
| Frequency of correcting homework | 1.810 (3.188) | 0.475 (4.588) | 6.814 (4.798) |
| Importance of encouraging students | 0.834 (2.074) | 1.364 (3.129) | 0.710 (2.907) |
| Frequency of assessing students | -0.388 (1.006) | -0.017 (1.709) | -0.606 (1.379) |
| Teacher has a writing board | 1.848 (11.666) | 6.522 (15.033) | 3.876 (11.805) |
| Teacher has chalk | -1.584 (5.984) | -0.499 (7.508) | -6.671 (7.786) |
| Teacher has a wall chart | -0.483 (2.684) | 0.953 (4.392) | -2.224 (3.842) |
| Teacher has a cupboard | -1.429 (3.287) | -1.543 (4.633) | -0.968 (4.713) |
| Teacher has bookshelves | 4.601 (3.198) | 8.507** (4.190) | 3.170 (5.130) |
| Teacher has a class library | $6.936 * *(3.159)$ | 7.004 (4.771) | 3.022 (4.000) |
| Teacher has a table | 1.031 (3.510) | -1.667 (5.353) | 2.929 (5.171) |
| Teacher has a chair | -2.752 (3.519) | -2.089 (5.164) | -1.603 (5.116) |
| Student fixed effects | Yes | Yes | Yes |
| $R^{2}$ | 0.888 | 0.921 | 0.898 |
| Observations | 68,197 | 37,626 | 38,060 |

Notes: This table reports OLS estimates for test scores. See main text for an explanation of controls. Standard errors are clustered at the school level. ${ }^{*},{ }^{* *}$ and ${ }^{* * *}$ indicate significance at the 10,5 and $1 \%$ levels.

Table 2: Textbook access, ownership, or sharing according to SES level and test scores:

## OLS results

|  | Dep. var.: Test scores |  |  |
| :---: | :---: | :---: | :---: |
|  | (1) | (2) | (3) |
| Student has access to a textbook | -0.575 (4.814) |  |  |
| Student owns a textbook |  | 5.772 (10.355) |  |
| Student shares a textbook |  |  | -3.533 (5.658) |
| Student has access to a textbook*Home possession | 4.371 (11.351) |  |  |
| Student owns a textbook*Home possession |  | -22.192 (21.200) |  |
| Student shares a textbook*Home possession |  |  | 22.453 (14.476) |
| Math | -3.154* (1.720) | -5.180* (2.702) | 0.638 (2.337) |
| Teacher gender (female) | 2.506 (2.356) | 1.680 (3.617) | 4.273 (3.519) |
| Teacher age | 0.220 (0.156) | 0.133 (0.207) | 0.209 (0.204) |
| Teacher qualification (junior secondary) | -3.737 (3.920) | -1.850 (5.731) | -7.729 (5.300) |
| Teacher qualification (senior secondary) | -3.838 (3.795) | -3.826 (5.710) | -5.875 (6.123) |
| Teacher qualification (A-level/tertiary) | -3.257 (4.505) | -3.634 (6.891) | -8.125 (6.896) |
| Teacher test score | 0.540*** (0.178) | 0.554* (0.284) | 0.522** (0.244) |
| Frequency of correcting homework | 1.794 (3.178) | 0.589 (4.563) | 6.800 (4.791) |
| Importance of encouraging students | 0.835 (2.074) | 1.385 (3.129) | 0.746 (2.895) |
| Frequency of assessing students | -0.389 (1.006) | -0.030 (1.708) | -0.626 (1.381) |
| Teacher has a writing board | 1.847 (11.677) | 6.775 (14.943) | 4.058 (11.864) |
| Teacher has chalk | -1.560 (5.983) | -0.645 (7.473) | -6.557 (7.767) |
| Teacher has a wall chart | -0.488 (2.683) | 0.959 (4.396) | -2.261 (3.830) |
| Teacher has a cupboard | -1.421 (3.286) | -1.568 (4.595) | -0.913 (4.711) |
| Teacher has bookshelves | 4.605 (3.199) | 8.524** (4.182) | 3.268 (5.116) |
| Teacher has a class library | $6.942^{* *}(3.160)$ | 6.980 (4.780) | 3.025 (3.989) |
| Teacher has a table | 1.020 (3.512) | -1.647 (5.345) | 2.846 (5.170) |
| Teacher has a chair | -2.757 (3.518) | -2.154 (5.159) | -1.698 (5.087) |
| Wald test p-value (Textbook $+0.5($ Textbook*Home poss.) $=0$ ) | 0.6256 | 0.3209 | 0.0870 |
| Wald test p-value (Textbook +0.57 (Textbook*Home poss.) $=0$ ) | 0.6124 | 0.2490 | 0.0740 |
| Wald test p-value (Textbook $+0.64($ Textbook*Home poss.) $=0$ ) | 0.6102 | 0.2185 | 0.0696 |
| Wald test p-value (Textbook +0.71 (Textbook*Home poss.) $=0$ ) | 0.6130 | 0.2076 | 0.0689 |
| Wald test p-value (Textbook +0.79 (Textbook*Home poss.) $=0$ ) | 0.6176 | 0.2055 | 0.0698 |
| Wald test p-value (Textbook +0.86 (Textbook*Home poss.) $=0$ ) | 0.6228 | 0.2073 | 0.0715 |
| Wald test p-value (Textbook +0.93 (Textbook*Home poss.) $=0$ ) | 0.6279 | 0.2107 | 0.0734 |
| Wald test p-value (Textbook +1 (Textbook*Home poss.) $=0$ ) | 0.6326 | 0.2147 | 0.0755 |
| Student fixed effects | Yes | Yes | Yes |
| $R^{2}$ | 0.888 | 0.921 | 0.898 |
| Observations | 68,197 | 37,626 | 38,060 |

Notes: This table reports OLS estimates for test scores. See main text for an explanation of controls. Standard errors are clustered at the school level. ${ }^{*}$, ${ }^{* *}$ and ${ }^{* * *}$ indicate significance at the 10,5 and $1 \%$ levels.
Table A1: Summary statistics

|  | Mean | Standard Deviation | Observations |  | Mean | Standard Deviation | Observations |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Panel A: Dependent variable |  |  | Teacher has a wall chart | 0.61 | 0.49 | 2,659 |
| Student math score | 494.04 | 92.26 | 36,829 | Teacher has a cupboard | 0.41 | 0.49 | 2,659 |
| Student reading score | 498.36 | 96.58 | 37,062 | Teacher has bookshelves | 0.27 | 0.44 | 2,659 |
|  | Panel B: Student and subject-specific characteristics |  |  | Teacher has a class library | 0.40 | 0.49 | 2,659 |
| Student has access to a math textbook | 0.88 | 0.33 | 37,062 | Teacher has a table | 0.69 | 0.46 | 2,659 |
| Student has access to a reading textbook | 0.89 | 0.31 | 37,062 | Teacher has a chair | 0.70 | 0.46 | 2,659 |
| Student owns a math textbook | 0.78 | 0.41 | 21,049 |  | Pane | E: Reading teacher | racteristics |
| Student owns a reading textbook | 0.79 | 0.40 | 19,631 | Gender (female) | 0.53 | 0.50 | 2,713 |
| Student shares a math textbook | 0.78 | 0.42 | 20,589 | Age | 35.36 | 8.24 | 2,747 |
| Student shares a reading textbook | 0.81 | 0.39 | 21,458 | Qualification (primary) | 0.12 | 0.32 | 2,747 |
|  | Panel C: Student-specific characteristics |  |  | Qualification (junior secondary) | 0.20 | 0.40 | 2,747 |
| Student home possession | 0.37 | 0.24 | 37,062 | Qualification (senior secondary) | 0.47 | 0.50 | 2,747 |
|  | Panel D: Math teacher characteristics |  |  | Qualification (A-level/tertiary secondary) | 0.21 | 0.41 | 2,747 |
| Gender (female) | 0.46 | 0.50 | 2,644 | Test score | 30.75 | 5.66 | 2,729 |
| Age | 35.38 | 8.13 | 2,679 | Frequency of correcting homework | 2.55 | 0.37 | 2,656 |
| Qualification (primary) | 0.11 | 0.31 | 2,679 | Importance of encouraging students | 2.76 | 0.48 | 2,747 |
| Qualification (junior secondary) | 0.21 | 0.41 | 2,679 | Frequency of assessing students | 5.28 | 0.90 | 2,747 |
| Qualification (senior secondary) | 0.50 | 0.50 | 2,679 | Teacher has a writing board | 0.94 | 0.23 | 2,731 |
| Qualification (A-level/tertiary secondary) | 0.19 | 0.39 | 2,679 | Teacher has chalk | 0.94 | 0.24 | 2,731 |
| Test score | 25.75 | 6.84 | 2,625 | Teacher has a wall chart | 0.60 | 0.49 | 2,731 |
| Frequency of correcting homework | 2.65 | 0.34 | 2,657 | Teacher has a cupboard | 0.40 | 0.49 | 2,731 |
| Importance of encouraging students | 2.77 | 0.47 | 2,646 | Teacher has bookshelves | 0.27 | 0.44 | 2,731 |
| Frequency of assessing students | 4.88 | 0.91 | 2,660 | Teacher has a class library | 0.43 | 0.49 | 2,731 |
| Teacher has a writing board | 0.94 | 0.24 | 2,659 | Teacher has a table | 0.69 | 0.46 | 2,731 |
| Teacher has chalk | 0.93 | 0.25 | 2,659 | Teacher has a chair | 0.70 | 0.46 | 2,731 |







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[^1]:    ${ }^{1}$ For evidence that is both recent and comprehensive, see Fehrler, Michaelowa and Wechtler (2009).
    ${ }^{2}$ This finding contrasts with the results by Jamison, Searle, Galda and Heyneman (1981). Relying on a randomized experiment in Nicaragua, these authors show that allocating a textbook to each student improves mathematics test scores by one-third of a standard deviation on average. This diverging conclusion may be due to the fact that the curriculum is less ambitious in Nicaragua than in Kenya. Moreover, the average student in Nicaragua is better off than her Kenyan counterpart. Because she faces lower barriers to learning, textbook access may have a greater positive impact on her achievement. The same reasoning applies to Hungi (2008) who shows that textbook ownership positively impacts test scores in math and reading in Vietnam as well as to Tan, Lan and Lassibille (1999) who demonstrate that providing teachers with learning materials leads to a significant decline in dropout rates in the Philippines.
    ${ }^{3}$ These include Botswana, Lesotho, Kenya, Malawi, Mozambique, Namibia, Seychelles, Swaziland, Tanzania, Uganda, and Zambia. We are forced to exclude Mauritius and South Africa as they report no test scores for teachers, a crucial control variable.

[^2]:    ${ }^{4}$ To be sure, a student fixed effect approach does not allow us to control for students' subject-specific propensities for achievement. Yet, this potential endogeneity problem is expected to be weak given that our data reveal a very strong correlation (equal to $76 \%$ ) between students' achievements across subjects. This correlation suggests that students' unobserved propensities for achievement are constant across subjects rather than subject-specific.

[^3]:    ${ }^{5}$ See Kuecken and Valfort (2012) for a discussion of these constraints.
    ${ }^{6}$ The levels-to-percentiles conversions are the following: $0\left(1^{\text {st }}\right), 0.07\left(2^{\text {nd }}\right), 0.14\left(13^{\text {th }}\right), 0.21\left(25^{t h}\right), 0.29$ $\left(38^{t h}\right), 0.36\left(52^{\text {nd }}\right), 0.43\left(63^{\text {th }}\right), 0.5\left(71^{\text {st }}\right), 0.57\left(77^{\text {th }}\right), 0.64\left(82^{\text {nd }}\right), 0.71\left(87^{t h}\right), 0.79\left(92^{\text {nd }}\right), 0.86\left(95^{t h}\right), 0.93$ $\left(98^{t h}\right), 1\left(100^{t h}\right)$.

