# Models of growth for system of cities : Back to the simple

#### J. Raimbault<sup>1,2</sup> juste.raimbault@parisgeo.cnrs.fr

<sup>1</sup>UMR CNRS 8504 Géographie-cités <sup>2</sup>UMR-T IFSTTAR 9403 LVMT

CCS 2016 - Amsterdam Session Urban 3 22th September 2016

ション ふゆ アメリア メリア しょうくしゃ

# Modeling Urban Growth

*Growth in Urban Systems : multi-scalar, heterogeneous drivers, bifurcations and path-dependancy* 



Source : Wikipedia

イロト イポト イヨト イヨト

# Spatial Interaction and Urban Growth

Role of spatial interactions in Urban Growth ?

 $\rightarrow$  gravity-based flows influence population growth in a synergetic formulation [Sanders, 1992]

 $\rightarrow$  Simpop models (from Simpop1 to SimpopLocal) [Pumain, 2012] : agent-based approaches ; more recently Marius [Cottineau et al., 2015] closer to system dynamics

 $\rightarrow$  Simple random growth (Gibrat model) becomes quickly complex by adding spatial interaction [Bretagnolle et al., 2000]; refined extension with waves of innovation in [Favaro and Pumain, 2011]

# Research Objective

 $\rightarrow$  Between complex ABM and non-geographical models in economics/physics, what place for simple models of growth in Urban Systems ?

 $\rightarrow$  Modulation of simple mechanisms to check for necessity/sufficiency : multi-modeling in models of simulation

**Research Objective :** Extend Gibrat simple model of growth in system of cities with spatial interactions and feedbacks through physical networks ; Explore systematically and calibrate such families of models

うして ふぼう ふほう ふほう しょう

**Rationale** : extend an interaction model for system of cities by including physical network as an additional carrier of spatial interactions (see [Raimbault, 2016b] for developed theoretical context)

→ Work under Gibrat independence assumptions, i.e.  $Cov[P_i(t), P_j(t)] = 0$ . If  $\vec{P}(t+1) = \mathbf{R} \cdot \vec{P}(t)$  where **R** is also independent, then  $\mathbb{E}\left[\vec{P}(t+1)\right] = \mathbb{E}[\mathbf{R}] \cdot \mathbb{E}\left[\vec{P}\right](t)$ . Consider expectancies only (higher moments computable similarly)

ightarrow With  $ec{\mu}(t) = \mathbb{E}\Big[ec{P}(t)\Big]$ , we generalize this approach by taking  $ec{\mu}(t+1) = f(ec{\mu}(t))$ 

# Model Formulation

Let  $\vec{\mu}(t) = \mathbb{E}\Big[\vec{P}(t)\Big]$  cities population and  $(d_{ij})$  distance matrix Model specified by

$$f(\vec{\mu}) = r_0 \cdot \mathsf{Id} \cdot \vec{\mu} + \mathsf{G} \cdot \mathsf{1} + \mathsf{N}$$

with

▲□▶ ▲□▶ ▲□▶ ▲□▶ ▲□▶ ● ● ●

# Data : stylized facts

Population data for French-cities (Pumain-INED database : 1831-1999)

Non-stationarity of log-returns correlations function of distance



# Data : geographic abstract network

*Physical transportation network abstracted through a geographical shortest path network* 



# Implementation

On the importance of visualization in spatial models : complementary implementations in NetLogo/R/Scala



# Results : model exploration

*Evidence of physical network effects : fit improve through feedback at fixed gravity* 



999

# Results : model calibration

Model calibration using GA on computation grid, with software OpenMole [Reuillon et al., 2013]

Pareto front for full model calibration, objectives MSE and MSE on logs



#### Results : non-stationary model calibration



# Quantifying overfitting : Empirical AIC

Not clear nor well theorized how to deal with overfitting in models of simulation. Intuitive idea : Approximate gain of information by approaching models of simulation by statistical models.

Let  $M_k^* = M_k[\alpha_k^*]$  computational models heuristically fitted to the same dataset. With  $S_k \simeq M_k^*$ , we show that  $\Delta D_{KL}(M_k^*, M_{k'}^*) \simeq \Delta D_{KL}(S_k, S_{k'})$  if fits of  $S_k$  are negligible compared to fit difference between computational models and models have same parameter number.

**Application**  $M_1$ : gravity only model with  $(r_0 = 0.0133, w_G = 1.28e - 4, \gamma_G = 3.82, d_G = 4e12)$ ;  $M_2$ : full model with  $(r_0 = 0.0128, w_G = 1.30e - 4, \gamma_G = 3.80, d_G = 8.4e14, w_N = 0.603, \gamma_N = 1.148, d_N = 7.474)$ Fitting of independent polynomial models  $(\tilde{P}_i(t) = Q \left[ \tilde{P}_i(t-1) \right])$  with 4 and 7 parameters) gives  $\Delta D_{KL} \simeq 19.7 \rightarrow$  fit improvement without overfitting

# Discussion

#### Theoretical and Methodological Implications

 $\rightarrow$  Indirect confirmation of known stylized facts (such as tunnel effect through non-stationary calibration)

 $\rightarrow$  For a better integration of theory, empirical and modeling on network aspects in evolutive urban theories

 $\rightarrow$  Methodology : first steps for empirical AIC in multi-modeling

#### **Further Developments**

 $\rightarrow$  Need to validate the approach on other system/subsystem of cities [Pumain et al., 2015]

 $\rightarrow$  Add Real Network in a static/dynamic way : towards models of co-evolution of cities and network [Raimbault, 2016b]

 $\rightarrow$  Coupling with growth models at other level, as e.g. mesoscopic reaction-diffusion model [Raimbault, 2016a]

# Conclusion

 $\rightarrow$  Simple models of complex systems can have strong explanatory power, and be used to test hypothesis/confront a theory

 $\rightarrow$  Crucial role of interdisciplinarity and integration theory/empirical and qualitative/quantitative

ション ふゆ アメリア メリア しょうくしゃ

- All code and data available at https://github.com/JusteRaimbault/CityNetwork/tree/master/Models /NetworkNecessity/InteractionGibrat

# Reserve slides

# **Reserve Slides**

▲□▶ ▲圖▶ ▲ 臣▶ ▲ 臣▶ ― 臣 … のへぐ

# References I

Bretagnolle, A., Mathian, H., Pumain, D., and Rozenblat, C. (2000). Long-term dynamics of european towns and cities: towards a spatial model of urban growth.

Cybergeo: European Journal of Geography.

- Cottineau, C., Chapron, P., and Reuillon, R. (2015).
  An incremental method for building and evaluating agent-based models of systems of cities.
  - Favaro, J.-M. and Pumain, D. (2011).

Gibrat revisited: An urban growth model incorporating spatial interaction and innovation cycles. *Geographical Analysis*, 43(3):261–286.

# References II

# Pumain, D. (2012).

Multi-agent system modelling for urban systems: The series of simpop models.

In Agent-based models of geographical systems, pages 721–738. Springer.

 Pumain, D., Swerts, E., Cottineau, C., Vacchiani-Marcuzzo, C., Ignazzi, A., Bretagnolle, A., Delisle, F., Cura, R., Lizzi, L., and Baffi, S. (2015).
 Multilevel comparison of large urban systems.
 Cybergeo: European Journal of Geography.

 Raimbault, J. (2016a).
 Calibration of a spatialized urban growth model.
 Working Paper, draft at https://github.com/JusteRaimbault/CityNetwork/tree/master/Docs/Paper

# References III



Raimbault, J. (2016b).

Towards Models Coupling Urban Growth and Transportation Network Growth. First year preliminary memoire. DOI : http://dx.doi.org/10.5281/zenodo.60538. PhD thesis, Université Paris-Diderot - Paris VII.

うして ふぼう ふほう ふほう しょう

Reuillon, R., Leclaire, M., and Rey-Coyrehourcq, S. (2013). Openmole, a workflow engine specifically tailored for the distributed exploration of simulation models.

Future Generation Computer Systems, 29(8):1981–1990.

Sanders, L. (1992). Système de villes et synergétique. Economica.

### Reserve slides

#### Calibration with fixed gravity effects (iterative calibration)



イロト 不得下 イヨト イヨト

æ