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An evolutionary model of urban systems

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An evolutionary model of urban systems*

Denise Pumain

The authors of a recent bibliographical essay (Pumain, Robic, 1996) stressed the degree to which theoretical approaches to urban places are static. When such theories do include time, it is usually only implicitly. The focus of explanation tends to be on structures, and much more rarely on the forms taken by change. No theory of urban systems, and especially not those expressed in geometrical or mathematical models, has so far satisfactorily integrated the urban phenomenon's temporal dimension, in the sense of change over historical time. However effective static interpretations may appear, as explanatory tools they completely overlook what is an essential characteristic of towns and cities, namely their capacity to change and adapt over time. The basic question to be addressed is that of how and why the man in the street is not mistaken to go on describing as 'town' or 'city' objects whose form, content and meaning have changed continuously over the centuries.

It is important to be clear that an evolutionary theory is not the same as an historical theory. The aim is not to consider the whole sweep of urban history, nor to reconstruct the particular contours of urban genesis. The approach is not that of historical study in the sense of exploring the past to seek an 'explanation' in a detailed account of how a place has developed. The objective is not the descriptive one of historical geography, and is instead that of producing a theoretical formalization of urban *evolution*, as the process of the historical transformation of specific entities. The aim is to demonstrate that a geographical object can be interpreted as the particular outcome, from among a set of possible outcomes, of a general dynamic process. In making the simplifications necessary for modelling, the notions of uniqueness and un-repeatability that characterize historical objects are inevitably lost, but it does take into account the non-reversibility of their particular history.

1. Difficulties in static explanations

As their structure is evolving slowly, it is not surprising that explanations for settlement systems have been initially searched in static theories, mainly in the framework of economics. But there is no evidence that an adequate explanation of urban systems could be derived from the principles of general economic theory. Economic theory is missing both the spatial and the evolutionary features which seem indispensable for a real understanding of urban systems.

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1.1 Agglomeration economies and central places

Most urban theorists who have based their work on micro-economic theory explain the spatial clustering of economic agents, assumed to be utility maximisers, by the existence of 'agglomeration economies' or 'economies of scale external to the firm' (Catin, 1994, p. 105). A first difficulty with this is that although these 'agglomeration economies' are frequently invoked they are never actually measured. It can also be pointed out that for decisions about localization to be based on agglomeration economies assumes that the town or city already exists, and the theory gives no explanation for how it developed. Another criticism that can be made of these theories is that they usually assume the town or city exists in isolation: the agents cluster according to their individual interests without there being any necessary relations with other urban places. In order to explain urban systems and to account for their hierarchical structure, the micro-economic theories make the assumption that returns increase with the size of urban centre. For example, Fujita *et al.* (1994) work on the hypothesis that the system optimizes its operation by establishing an equilibrium between supply and demand for services at the mesoscopic level of the city, while individuals optimize their localization by maximizing their utility. This means that the towns and cities which offer the widest range of services will be more attractive, and the influx of migrants will in turn cause an increase in the range of services they can offer. Large cities are thus more attractive and grow faster than smaller ones, but the theory does not explain why differences in city size exist, and why the urban hierarchy acquires a particular form or why this is stable over time.

Central place theory, in its original formulation, is a static theory and it takes for granted the structure it purports to explain. According to this theory, postulating the existence of different levels of goods and services (organized according to how much they are in demand, which determines the different ranges and thresholds of appearance) is the basis for deducing the existence of hierarchical configurations of regularly-spaced urban centres (Beckman and MacPherson, 1970). Several authors, including H. Beguin (1979 and 1988) have introduced stochastic elements in an attempt to bring the stepped hierarchy of the models closer to the linearity actually observed in urban settlement sizes. But no satisfactory explanation has been given of how the link is established between the hierarchy of the different goods and services and the hierarchy of the central places. The concentration of goods of the same order in each central place is postulated but is not demonstrated by the theory. Nor does the theory indicate how the urban hierarchy thus formed is likely to evolve. Christaller's book includes a chapter of suggestions on this subject, but they are not incorporated into his models, which thus remain structural and static.

1.2. Static and equilibrium theories

Urban theories that give a static interpretation are unconvincing because they apply on the level of individuals, that is the agents whose behaviour is formalized in the models, processes which they assume to be universally valid regardless of time and place. They completely disregard the historical nature of the urban object and can thus be said to contradict themselves in that they use the mechanisms of today to try to explain an entity that has been produced over time. If a city were to be built today from scratch applying the principles of these theories it is doubtful that it would be like any known city in either its unique character or its principle of functioning. The present form is the result of a long evolution and cannot correspond to the optimization of a handful of factors at a

particular point in time. The mechanisms developed in micro-economic analysis to explain the concentration of the agents and agglomeration economies make no allowance for the length of time that their action requires.

The problem is that behind all the static explanations for the size and spatial arrangement of urban settlements can be discerned the notion of equilibrium, governed by a determining factor in the form of some force, an 'invisible hand', a statistical constraint. The form of urban networks has thus been 'explained' by the action of contradictory forces working for unification and diversification (Zipf 1949), by the micro-economic theory of markets (whose centrality is the spatial expression of the principle according to Berry 1967), by a principle of maximizing social interaction (Claval 1982) or by a statistical process in which a structure is deduced from a mechanism controlled by a limiting or optimizing principle (entropy maximizing. Curry 1964). All these explanations in fact derive from the same hypothesis, which can be summed up thus: the configurations observed at any given moment are the result of the optimization of a constraining factor, or are the expression of an equilibrium between contradictory actions. Fujita *et al.* (1994) consider as a 'natural rule' (*sic*) that 'at any moment in time, the urban system must be in spatial equilibrium' (p.21). In this recent version, they try to introduce a dynamic element to their model by starting with a static equilibrium model and imagining the shifts in this point of equilibrium over time. Contrary to what is claimed by the authors, such a model does not allow us to understand 'the emergence of a system of cities'.

Long-term observation of the dynamics of urban networks does not supply proof that the dynamics of urban systems are governed by a macroscopic constraining factor, or that what is observed at any given time represents an equilibrium state. On the contrary, what we find are large or gradual changes in the distributions, but without knowing if the forces that are supposed to have produced them have changed. A certain dynamic can thus be identified at work within a geographical distribution. This dynamic is the product of interactions which if they were allowed to operate unhindered over a long enough period might result in an equilibrium that could be modelled. In reality, of course, the form and intensity of the interactions have always changed before this equilibrium can be reached. Imagining that a system's current state corresponds to an equilibrium thus means assuming, if it is to be explained in these terms, a set of interactions which on their own cannot in fact explain the present form (Allen 1991). We are thus forced to take the view that the configuration observed and the transformations it experiences must be explained by a single theory. With the same theory it must be possible to explain the structure of the system *and* the changes occurring in it.

The somewhat tautological hypothesis used by economists to justify the concentration of economic activities in urban centres, and which presupposes the existence of agglomeration economies, does not appear to me to be necessary to explain the differences in the size and evolution of towns and cities. An evolutionary theory can account for these without having to accept the idea that large cities are more productive and more efficient in economic terms than small ones in order to explain the existence of urban networks in their present form. Indeed, the greater economic efficiency of large urban centres, if this is actually proved to be the case (Rousseau, Prudhomme 1993), and thus the existence of agglomeration economies, could be as much the *consequence* as the *cause* of their success.

2. Dynamic models of urban growth

With the creation of historical and comparative data bases (Bairoch 1996) a large volume of observations relating to change in urban systems is now available. Early efforts to incorporate this material into a theory involved the transfer of dynamical models from the 'pure' sciences of mathematics, statistics, physics and chemistry. However simplistic these models may be, they have a valuable filtering role. By making possible the comparison between urban dynamics and the dynamics of other systems they have helped to identify a number of specific aspects of urban evolution and thus contributed to the development of more sophisticated modelling.

Many models present merely a simplified description of urban systems in terms of sets of population centres characterized by their number of inhabitants. Although this simplification is extremely crude it is not meaningless given that 'demographic size' is the variable which best expresses a wide range of functional properties of towns and cities. Population size is a correlate for many quantitative descriptors, such as the number of jobs, firms or homes, but also for qualitative descriptors such as the diversity or complexity of economic activities and of urban society. It constitutes the main 'dimension' of an urban system, its most important factor of differentiation. (Reiner, Parr, 1980). Knowing the size of a city typically supplies a lot of other information about that city, and can thus be used to make a wide range of fairly accurate predictions. Size presents the additional advantage of being measurable over very long periods in a reasonably straightforward and comparable way, and of keeping a relatively constant significance in terms of the 'success' of the sub-system it represents. The fact of attracting and keeping a certain number of residents was for long taken as the measure of a city's capacity to provide the means of subsistence for this population (through local production and innovation, but also by the extraction of surplus from the countryside or other urban centres, or by imposing its terms in a system of exchanges). For present-day international comparisons in particular, however, this indicator of urban success needs to be completed by an evaluation of living standards and levels of output, as well as by indicators of quality of life and the environment.

For the purposes of the present article we will just use this description of the system in terms of city size for the formal part of the theory. This does not mean that an evolutionary theory has no further extension. It is merely a first stage, and it will in fact be seen that a coherent and formalized conceptualization leads to including far more complex aspects of the definition of an urban system even in this simplified version of the theory.

2.1. Gibrat's model

The simplest alternative to the static point of view is the approach which treats urban systems as the product of a stochastic process distributing population growth between cities. This involves transferring a *statistical model* for the dynamic description of an urban system. In his book on *Les inégalités économiques*, Gibrat demonstrated that when cities are growing at the same average speed but with fluctuations or inequalities of growth, the distribution of the city sizes will consistently take a particular form.

Let there be a set of localities with a certain size distribution (they can even be all the same size at the start of the process) and whose evolution over a long period (several

centuries, for example) is modelled, using a large number of short time periods. It is assumed that in each time period (for example, one year, or ten years) the population P_i of each locality grows on average (though with fluctuations e_j) by an amount dP_i which is proportional to the population P_i (and low in relation to P_i):

$$dP_i = r P_i + e_j$$

This is the same as saying that the proportional rate of change of the population dP_i/P_i (which is the measure usually expressed in % and used to describe and compare the growth of cities and regions) has the same average value for all settlements, whatever their size at the beginning of each time period. If in addition the distribution of these rates between localities is independent from one time period to the next, the growth process it defines will always result in a distribution of settlement sizes that is a lognormal distribution, highly skewed, characterized by a large number of villages and small towns and a geometric decline in the number of cities at the larger sizes. If the rate of growth and its variations are known it is even possible to predict (at a known probability) by how much the size disparity will increase.

With this process the attractiveness of cities does not have to be assumed to increase with their size in order to obtain a highly uneven size distribution, comprising a small number of very large cities (consequently there is no need for a theory like that of agglomeration economies). Also, this model can be 'tested' empirically against the statistical observations of urban growth rates at regular intervals over long periods. It has been confirmed for many different countries and periods (for example Robson 1973, Pumain 1982, de Vries 1984, Guérin-Pace 1993, Moriconi-Ebrard 1993). A more satisfactory 'explanation' for the form of the distribution of city sizes is thus obtained when we view it as resulting from a dynamic process for the distribution of urban growth than simply as the expression of a static equilibrium. Compared with these static interpretations, Gibrat's model is in fact the only one to show why this form of organization is unchanging over time, and to deduce a gradual concentration of the population in increasingly large cities at the top of increasingly skew distributions. The model thus provides an 'explanation' for the gradual differentiation in size between cities that are involved in the same evolution, though with an uneven effect produced by the 'accidental' (or random, in the sense that they are not determined by the model) repetition in some places of incremental increases that are larger or smaller than those experienced by the set of other cities. As a first approximation, then, Gibrat's model provides both a good description of growth in an urban system and an explanation of its hierarchical structure. It can be used for predicting the evolution of city sizes over periods of up to several decades.

However, a theory of urban systems cannot be restricted to the formulation of this purely stochastic model, especially if we want the theory to accommodate the systematic deviations from Gibrat's model that are observed: first, over the long term there is usually a slight positive correlation between urban growth rates and city size, second, they are sometimes temporally autocorrelated, for periods of several decades (Robson 1973, Pumain 1982, Guérin-Pace 1993). Also, the 'primate' cities, the two or three 'metropolises' in the national urban hierarchies, whose size appears 'disproportionate' compared with the rest of the urban system, are in fact agglomerations which have grown systematically faster than the rest of the urban network over several decades. (Moriconi-Ebrard 1993, Pumain, Moriconi-Ebrard 1997). The model has therefore to be

corrected and completed so as to accommodate what in relation to the simple stochastic process appear as 'anomalies' but which are in fact revealing of processes that are specific to the evolution of the urban system. This leads us to an explicit formalization of the relations of interdependence between cities, and thus to shift from a formalization of a *set* of cities to that of a *system* of cities. In the Gibrat model, the notion of interdependence between cities remains implicit and is present only in the hypothesis that the growth rates of cities obey a distribution with the same average and with a given variance: the implication is thus that they belong to the same 'system'. This hypothesis does not appear as such in the statistical model and it is when the model is transferred to cities that it becomes logical to introduce it as expressing the information exchange and competition between cities.

Empirical observation also necessitates consideration of another process which is that of the *selection* of those members of the set of inhabited localities which grow into towns and cities. The dynamics described by Gibrat in fact applies not only to urban places but more generally to the settlement system as a whole. Clearly, however, this dynamics tends to produce not one but two lognormal distributions, characterized by unequal degrees of contrast between the size of their elements. From our perspective, this implies that two subsets of localities have been subject to a long-term 'selection', one for a dynamics of growth, the other for decline, as has been the case for the towns and rural communes in France over the last two hundred years (Pumain 1995, p. 437). The distinction between towns and cities and villages thus leads to incorporating into the evolutionary theory qualitative considerations concerning the functions of settlement centres and as well as the historical change known as the 'urban transition'.

2.2. A dynamics of interdependence

Communication, exchange and interdependence between like entities are properties which appear linked to a geographical definition of the urban concept. For this reason the geographer finds it hard to accept the definition (presented as a 'non-definition!') put forward by H. Beguin (1996), which emphasizes the concept of density but does not satisfactorily articulate the two identifiable levels of urban organization, the city and the city system, and above all fails to integrate the 'ecological' dimension, that is provide an explanation of the urban object that is 'vertical' rather than simply 'spatial' or 'horizontal'. The individual urban place cannot be dissociated from the system of urban places, and exchange of whatever type or form, including therefore long-distance relations, are integral to the urban function and are part of its specificity. According to Henri Raymond (1981), what distinguishes the town and city from other forms of settlement (village, mining centre), which exploit purely local resources drawn from a single site, is the possibility of exploiting a situation, the resources of several different sites. This conception is consistent with the findings of historical and archaeological research regarding the genesis of towns and cities. For P. Bairoch, 'the existence of an urban centre presupposes not only an agricultural surplus but also the means of exchanging this surplus' (1996, p.19).

H. Raymond justifies his definition using the concept of limiting factor borrowed from ecology, which postulates that at any given moment the resources available to a population established in a particular location act as a limit to its development: 'The system of urban habitat is the basic ecological organism which, of all those invented by the human race, can eliminate the most completely the set of limiting factors of a site,

whatever its own resources. Towns and cities have succeeded in overcoming the uncertainties arising from local limiting factors and in controlling these local difficulties, by developing multiple links and forming ever faster networks. Sites that are linked in this way can support a population much larger than was possible on the initial site. This evolution is not finished, and the tool that these towns and cities become is continually being invented' (personal communication, 1995).

The existence of a pattern in the evolution of interdependent urban centres was noticed long ago, for example by J. Reynaud (1841) when he introduced the concept of 'general city system'. B. Berry's (1964) famous phrase 'cities as systems within systems of cities' was a use of systems theory as the framework in which to formalize the relationship between the level of organization and observation formed by the *city*, viewed as a collection of neighbourhoods, institutions and actors linked by systemic relations, and the *city system*, organized on the principles of central place theory. In his book published in 1977, A. Pred stresses the dynamic aspect of the notion of urban system by defining it in extremely general terms as: 'a national or regional set of cities which are interdependent in such a way that any significant change in the economic activities, occupational structure, total income or population of one member city will directly or indirectly bring about some modification in the economic activities, occupational structure, total income, or population of one or more other set members' (p. 13).

Subsequent empirical research on the ways in which urban systems evolve has demonstrated the value of interpreting their dynamic within the framework of self-organization theory. This formalization can be used to refine A. Pred's definition and in particular his notion of 'significant change'. Not all local transformations will affect the other cities in the system. Many of the changes that affect towns and cities over periods of several years or several decades (in urban morphology, in demographic, social and economic structures, ...), though they could be described as 'significant', have no effect on the structure of the system, that is on the form of inter-urban differentiation, because they affect all towns and cities (Pumain, Saint Julien 1978, Sanders 1992). The structure of the system will also not be modified by changes that are particular to a town or city, because they do not last long enough from one period to the next and are mere *fluctuations* which do not alter the relative position of urban centres within the system. A structural change will occur when one of these fluctuations persists and increases to the point that it modifies this position, usually of several cities at the same time, related to the development of a new specialization, for example. In this case there is said to be a *bifurcation* in the history of the system. Most fluctuations have no effect if they occur while the system is on a stable path (Pumain, 1987, Pumain *et al.* 1989). A bifurcation may also be the result of a *perturbation* originating outside the system in question.

2.3. Models based on self-organization theories

Observation of the ways in which interdependent cities evolve has prompted the transfer to geography of models originating in chemistry and physics. The analogy with physical systems, using the dissipative structures concept (Allen 1978) or synergetics (Haken 1977, Sanders, 1992), involves formalizing the dynamics of systems as the product of interactions between microscopic units which together form structures that are detectable at the macroscopic level. The system thus described is 'open': in the case of a physical system this means that it receives an input of 'energy' from the 'exterior' which allows 'self-organization' to occur. When the model is transferred to human systems, this

energy input is assimilated to innovation, or to a trend towards growth of the system, which acts as the 'motor' of its dynamic. Application of the self-organization concept to these systems suggests that the fact that they are structured by a persistent and thus identifiable architecture cannot be explained by the action of a network operator or by any explicit political or economic objective, such as could be described in terms of some constraint to be respected or quantity to be optimized. The structure is in fact the spontaneous product of multiple interactions between many separate agents. Each of these has its own objectives and strategies, but these do not need to be known in detail in order to predict (or simulate) what will be the system's general architecture. In this way the mass of individual decisions can be reduced to a small number of parameters and equations which describe the system's evolution at a macroscopic level: this is in principle possible using the probabilistic models taken from synergetics and self-organization theory, in which a 'master equation' expresses the overall effect of the interactions occurring between the particles whose individual state and position within the system cannot be known (or predicted). The notion of random event is thus linked to the existence of several levels of observation in the system: 'the microscopic phenomena influence the form of the macroscopic phenomenon, while it is the latter's law which unifies the microscopic phenomena, or, in other words, subjects them to its 'point of view'. The particular laws of these two types of phenomena are not usually 'random laws', and these are merely the laws of their interaction' (Bonitzer 1984).

Self-organizing systems are not in a state of equilibrium at any given time; their transformation is the result of internal and external dynamic processes, and their structure is the product of this evolution. Change in urban centres or urban systems takes forms similar to those in the physical theories of self-organization. This combines, on the one hand a stability or slow transformation in the system's structure (the macrogeographical state of the urban system as reflected in the form of the size distribution, the main differentiating factors in the economic activities and social composition of cities ...), on the other, very large fluctuations in the relative position of its elements: at the meso-geographical level this corresponds to the rapid shifts that individual cities make between 'states' of growth, stagnation, contraction; or changes of rank within the size hierarchy over the medium-term; or ten-yearly changes in their socio-economic profiles, which may anticipate, parallel or lag behind, a general transformation (Pumain, Saint-Julien, 1978). The fluctuations (or shifts of the elements from one state to another) are even more apparent if we adopt the most 'microscopic' level of geographical observation, that is, the individuals, households and firms located in the urban centres, on the time scale of one year (residential and professional mobility, creation and demise of companies) or on the time scale of one generation of people being replaced by the next one.

Dynamic models of urban systems have been elaborated in this context whose formalization makes explicit some forms of interdependence between the elements of the system, such as the competition to attract activities or population. Using dynamic models, the evolution of a set of central places can be simulated from the growth rates and movements of population and employment between the urban centres of a region (Allen, Sanglier 1979, White 1977). Other models have simulated the evolution of city sizes from the migrations of individuals between centres (Weidlich, Haag 1988, Sanders 1992). These models have been related to the macroscopic structure of the urban system, for example by demonstrating that under certain hypotheses, the distribution of

city sizes behaves as an attractor for a synergetic dynamic model of interurban migrations (Pumain, Haag 1994).

A general criticism that can be made of dynamic models is that they describe *how* change occurs but not *why* it occurs. If the essential mechanism responsible for the form of the urban system is the competition between its component geographical units to attract and accumulate the product of different resources, and if this competition is made possible by the circulation of information between the units which thus constitute a network, the fact remains that the motor of change is the continuous creation of new products and wealth in the system. Yet the emergence of innovation remains a stumbling block in dynamic modelling, one that even the most sophisticated efforts at simulation have failed to resolve (Allen 1991).

The difficulty experienced by mathematical models to account for creative change, for the consistent transcending of the limits of a dynamic, that is characteristic of social evolutionary processes, is why models based on a biological analogy have been no more successful than those borrowed from physics. The transposition of Lotka-Volterra predator-prey models to the study of competition between regions or cities (Dendrinos and Mullaly 1985, Ianos, 1994) is only possible if attention is limited to the observation of relative variation, in other words if the urban dynamics is reduced to a struggle to secure market shares (the 'technology substitution' model of Marchetti 1986). Yet this overlooks, first that the limiting factor present in the Lotka-Volterra ecological competition models is continually challenged by human societies, second that temporarily abandoned territories can always find a different use during a new cycle of innovation, thereby invalidating the idea of an analogy with the technological substitution between products.

Here can be seen the limitations of analogies from physics and biology when they are transferred to a theory of urban systems. Although models based on physical systems admit two possible processes of change in the structure of the systems, from bifurcation due to the amplification of an internal fluctuation or the irruption of some external perturbation, they have great difficulty accounting for the crucial phenomenon of innovation. Not only is this to a large extent endogenous to urban systems, but the continuous renewal that it induces means that innovation has a fundamental role in the genesis of the system's structure, through the diversification and complexification of its elements. Consequently it seems inappropriate to consider it simply as a fluctuation or external perturbation. The process has received considerable attention from economists seeking to replace general equilibrium theory by an evolutionary approach.

Some authors have also suggested incorporating in the theory not only aspects of physical dynamics but also evolutionary processes based on biological theories. P. Allen (1991) has argued that towns and cities belong to the sorts of systems in which new forms and functionalities are created. The appearance of innovation in the systems is not due to some optimization of their functioning at a given time but results from the practices and 'discoveries' and 'inventions' of non-average individuals. This is in fact a social interpretation of the notion of *diversity* from the biological theory of evolution. The models based on this theory require very powerful computers to simulate the endogenous emergence of innovation. However, it is not certain that social innovation, and the learning and collective processes that it implies, can be modelled in quite the same way as a biological phenomenon. Future models will probably have to include

cognitive processes, both for their role in the appearance and selection of innovation, and as additional regulators in the evolution. It may then be possible to explain why bifurcations or 'chaotic' behaviour are less common in urban systems than in other types of evolutionary systems.

3. From dynamics to evolutionary theory

These various analyses do help to identify the characteristics of an authentic evolutionary theory of urban systems (Pumain, 1997). We do not focus here on the substantial transformations in urban form and economy, which in a legitimate way are the basis for most of urban research agendas (for instance, Bourne, 1995, 1996, Preston, 1994, Braun, 1991). Our objective is to concentrate on the few features which can be considered as remaining general and specific properties of urban systems over time. An evolutionary theory has thus to accept that its object is transformed over time, based on its previous forms but acquiring new properties. The theory must set out the general pattern of these changes, identify their direction, which can then serve as the basis for forecasts. Of course such a theory may be seen as an oversimplification compared to the complexity of real processes of change. It would be premature to claim that a complete formalization is possible, but we can indicate some lines of inquiry which may be of use in its elaboration.

3.1. The notion of urban system

A simple definition of an urban network or city system is that of a sub-set of a settlement system. The latter is made up of all the inhabited localities of the same territory — hamlets, villages, towns and cities — as well as the relations (which can be specified later) that exist between these localities and between them and their surroundings. The fact of being part of the same territory gives a degree of unity to the system's functioning, by providing relatively homogeneous conditions of communication between its elements. The territory is defined here by political and cultural standards, as a contiguous portion of the Earth's surface occupied or controlled by a group. The notion of territory also implies a degree of delimitation (its 'boundaries' limit the intensity of interactions between localities that belong to different territories) which justifies the identification of a 'system'. However, it must be noted that the development of urban systems continues regardless of changes in politically-defined territories. Furthermore, when the forms of politico-administrative organization of particular territories have remained stable over long periods they can give rise to specific variants of the general urban system model. Finally, it is clear that to varying degrees cities, particularly those in the upper reaches of the urban hierarchy, are indifferent to territorial boundaries. Since the range of urban relations is strongly correlated to the size of the centre, the reference territory should be proportionate to the level of the hierarchy being considered. The notion of system applied to urban settlements is thus of ultimately limited value and needs to be replaced by a more suitable metaphor. However, it is useful for the purposes of modelling, so we shall continue to use it with reservations until something better is found.

The timescale of evolutionary change is that in which complexification occurs. Adoption of the evolutionary perspective implies integrating the specific temporalities of cities and the urban system into our definitions of these objects. This is only possible if we adopt a relative concept of geographical space.

3.2. Relative space and geographical entities

Two concepts of space are found in the work of geographers. The more widely used treats space as a physical reference which acts as the setting and framework for the analysis of the human activities distributed within it (Beguin, Thisse 1979). Space thus construed is endowed with straightforward geometrical properties, even though it gives only an approximate and distorted representation of the Earth's surface, as for example in cartographical representations. The other concept defines space on the basis of the relations which exist between localities. Because the distribution of these relations is not homogeneous or isotropic or continuous, representation of the 'relative' space thus produced is not always easy. However, the concept of relative space is essential for understanding the development of what in terms of absolute space are referred to as 'spatial structures', that is detectable and identifiable geographical objects.

Although the theory is still in its infancy, an evolutionary perspective would show how these geographical entities, in the form of villages, areas of jurisdictions, towns, territories, networks, are constructed through the integration over time of relations between localities. Contact and exchange are responsible for the spread and imitation of practices, for producing personal interaction and shared modes of thought and expression. These relations gradually create the similarities which underpin the formation of homogeneous landscapes and regions, as well as the memberships which define the territories and networks. They are at the origin of the accumulations of human and non-human capital which increase the attractivity of some localities. The interlocking of these constructions at different levels is what forms geographical space. A static account of this was given by Philbrick (1957), while a formal analysis has been attempted by C. Grasland (1994). They have yet to be incorporated in a dynamic theory.

3.3. Urban centres construct two spaces

The dynamic models in which cities are formalized as self-organizing systems use the representation of an absolute space as providing a setting for centres that are linked by flows (of goods, people and information) to form a system. Progressing from a dynamic theory to an evolutionary theory requires conceptualizing a relative space, one that is defined by these relations and flows. It then becomes necessary to distinguish the two levels of observation of the urban phenomenon that are the city and the urban system. First, these two levels of observation of the urban phenomenon correspond to two types of territory, with different relational scales. Second, the changes in this relative space are a source of information about the origins and history of the urban systems (Pumain 1995b).

At any given time, the urban system, or more generally the settlement system, is responsible for the articulation of territorial entities on different geographical levels, by establishing links between levels of organization with contrasting space-time dimensions. The settlement system is what makes possible the coexistence of at least two main levels. The first level is that of the village or urban place in its role of *territory of daily activity*. At different periods, the composition of internal journeys has varied widely, depending in particular on the degree of specialization of places for residence, work, commerce, or leisure. The average time devoted to these daily journeys, which has to be added to that of other activities carried out in the day, remains on the whole relatively constant, in the

order of roughly one hour, sometimes between one and two hours. The spatial expansion of the territories of daily life is thus severely limited by the time necessary for internal journeys, the speed of which, particularly in the cities, is itself reduced by high density levels (for example, the average speed of road traffic in Paris today is estimated to be 18 km/h).

The main functions of the daily territory represented by each cluster in the settlement system are habitat and production (of goods and services). In most cases, however, these two main functions are no longer regulated locally. Their evolution is in the main determined elsewhere, in the nodes of the power networks where decision-making occurs. Some of the power centres in these networks are clearly identified, taking the form of a political or administrative capital, the headquarters of a multinational company. More usually, the forms of the flows of goods, services, labour and ideas which are responsible for the functioning of territories of the higher level of organization, on regional, national or even multinational levels, are determined through multiple networks of negotiation, competition and complementarity.

These networks are able to function thanks to the urban system. The forms of circulation which exist in this other level of territorial organization govern the system's spatial structure, as defined by the distance between and size of the urban elements. At this level the distance between the main centres corresponds roughly to the distance that can be travelled in a single day. This length of time is accepted as the average needed for the stages in a journey (Reclus 1895) or for a return trip necessary to conduct fairly frequent negotiations in localities which are not visited every day (Cauvin, Reymond, Schaub 1989), within the networks of exchange which can exist between headquarters and subsidiaries, between large companies and their clients, between a capital and its main administrative relays. Although it is not very precise, this measure of a single day does allow a much larger spatial extension for the territories of control and co-ordination than for those of daily life. For any given transport technology, not only the length of time determining the spacing of centres in a territory, but also the speed of circulation between them, is in general much greater than that possible within each individual centre (Orfeuil 1993, Dupuy 1995).

Definition of a relative space for representing the relational possibilities both within and between urban centres is at the origin of the attention given to fractal geometry for the study of these objects (Arlinghaus 1985, Frankhauser 1993, Batty, Longley 1994). The relational space is strongly organized by density gradients and has a fractal structure. Applied to the description of urban structures, the notion of *fractality* has the advantage of offering a new reference model to replace that of a homogeneous occupation of space as is used for calculating density. Instead it is the direct expression of the anthropological occupation of space, by incorporating the form generated by the experience of centrality in the description of urban objects. The effect of this is that urban densities (buildings, population, activities, journeys ...) do not have a homogeneous spatial distribution but vary systematically depending on their position in relation to one or several centres, following a dilution or fragmentation going from the centre to the periphery. A fractal model is therefore more suitable than the Euclidean model for analyzing the properties of urban systems and for identifying their specific features. The early experiments on urban centres and urban networks have found a good fit for the fractal models at the different levels of analysis (Le Bras 1996). Some authors have also drawn attention to the existence of a clear discontinuity between the fractality

of the internal spaces of towns and cities and that between them (François *et al.* 1995), which would appear to confirm that urban centres induce space-time structuring on two levels. Fractal representation is also an antidote for the shortcomings of the spatial representations of the geometry of urban systems in the Christaller models, which take no account of the differentiation in density that central places create by their presence. According to M.-C. Robic, this 'distorting' of the spatial models of central places, which was given an approximate schematic formalization by W. Isnard, had been noticed by J. Reynaud, who postulated a 'bending of space' in the vicinity of urban centres and lines of transport.

3.4 Towards a theory of the evolution of settlement systems

A conception of the urban system as being responsible for the articulation between two levels of space-time relations implies seeking an alternative to a static formal theory. The present structure of urban systems represents neither a state of equilibrium nor an optimum dictated by some constraint at a particular moment. The spatial configuration of urban centres, their size and spacing, are the product of more or less constant processes whereby towns and cities are *adapted* to modifications in the proportions of space by the speeds of circulation, and an *adjustment* of their internal structure to the forms of social, functional and technical change.

Evolutionary theory situates the present structure of the urban system in the context of the general history of settlement systems. The latter is deeply influenced by the process of the *urban transition*, which is the name used to describe the changes consequent on the shift from an agrarian economy, using mainly local resources, to a manufacturing and service economy, based on long-distance trade. In the countries which had long been settled, as in Europe and Asia, the same sites or settlement nodes have been maintained by the successive economic and political systems that control these territories. The creation of completely new settlements and new towns and cities is an extremely marginal process compared with the overwhelming majority of processes whereby existing centres of habitation are adapted to new functions. In countries which have been more recently settled, a first phase of the change was reflected in a spatial diffusion that followed the advance of settlement and included the establishment of new sites. Once the available territory was fully occupied, however, the forms of evolution became similar to those observed in the countries of long established settlement.

The main dynamic characteristic of urban settlement systems appears to be the *competition* between their elements for the attraction and creation of wealth, by means of exchange, innovation (anticipation) and the adoption (imitation) of innovations. This form of evolution is made possible by the system's high degree of interconnectivity, which enables information to circulate. A change that occurs in one town or city will quickly be copied and adopted in the others. The capacity for adapting to change is linked to the relative position of urban centres in the system in terms of resources, either linked to the site or accumulated, and the relationship which exists between the rate of adoption of change and previous accumulation (as expressed by the size of urban centre) has been demonstrated by many authors from an examination of the process of hierarchical diffusion of innovations within urban systems (Pred 1966 and 1973). In contrast to the restriction of the volume of population and urban activities that occurs in a biological predator-prey model, inter-urban competition is not a zero-sum game and, because it encourages innovation, is continually pushing back the factors that threaten to

limit urban expansion. It is the source of the process of the social division of labour which expresses this impulse and generates new urban specializations, and which must consequently be conceptualized as being endogenous to a model. Competition between urban centres to attract distant resources and the product of innovations leads sooner or later (depending on the speed of communications of the moment), to a process of growth and transformation experienced by all the towns and cities in the territory under review. In the context of this generalized quantitative and qualitative expansion, urbanization is interpreted as a diffusion-expansion process affecting all parts of the urban system. This process is stochastic, made up of small adjustments by which the place of urban centres in the system is continually adapted (or corrected), with each tending to retain the same relative position. This same process explains the system's hierarchical organization as described by Gibrat's model.

The anticipations and imitations performed by the urban agents are non linear processes, however, which can produce bifurcations, that is, modifications to the structure defined by the relative positions of towns in the system. It is for this reason that in periods when systems of settlement are being established, during upheavals in the political organization of territories, or when particularly selective innovations appear, local mutations (rapid growth, crises, decline) can significantly modify the position of towns in the system. Modelling these non-linear interactions requires a more complex dynamic than that employed by Gibrat.

The expansion of urban systems appears not to be a continuous process over time. In the past, the *range of urban interactions* was for long restricted by the very slow speed of communications, thus preventing towns and cities from developing beyond the limits set by the resources in the accessible territories, which were usually limited in extent. Historians have established that even in the wealthiest pre-industrial economies the average urban population did not exceed 10% of the total population (Bairoch 1996). The process of urbanization that began with the earliest towns, some two or three thousand years after the appearance of agriculture (Bairoch 1985), accelerated significantly when the transport revolution opened the way for an extension of the territories and networks that urban centres were able to dominate. The urban transition, which took urbanization levels up to 80% in the industrial nations in little more than a hundred years, could in fact be interpreted as the fairly brutal condensation of a dynamics of inter-urban competition which although it had started long ago had previously been held in check by slow communications. The transformation of economies from an agrarian to manufacturing and then service basis was accompanied by far-reaching modifications in the distribution of settlement, resulting in a pattern of urban centres that was regularly-spaced, and appreciably more hierarchical, contrasted and concentrated than the previous settlement system (see for example maps of the evolution of the European urban system since XVIth century in Bretagnolle, Pumain, Rozenblat, 1998).

The relationship between the form of urban systems and the speed of communications can be illustrated, for example, by showing that the spatial structure of urban systems, as well as their degree of hierarchization, is characterized by variations that reflect the forms of circulation which existed at the time of their creation. For example, the criterion of average distance between towns and the degree of contrast in their size, corresponds to a division not between developed and Third World countries but between countries of the Old World and those where settlement is of more recent origins (Moriconi-Ebrard

1993). As an example, the average space between two urban centres with over 10 000 inhabitants is less than 15 km in China and in Europe, compared with nearly 50 km in North America. Similarly, an index measuring the size of hierarchical contrasts between these urban populations, expressed by the slope of the 'rank-size' distribution, is less than 1 in Europe, over 1.2 in North America, whereas its average value is the same (1.05) in the developed and developing countries.

In addition, all these systems exhibit a long-term trend to more pronounced hierarchical contrasts. This could be explained by the initial advantage consistently obtained by large centres because innovation is diffused hierarchically (a strengthening of the hierarchy from above). But it also occurs systematically as a result of the *time-space convergence*, whereby the largest urban centres are able to short-circuit the clientele of the smaller centres that occupy an intermediary position, also inducing a 'simplification from the bottom' of the urban hierarchy. The most frequently observed deviation from the Gibrat model, a correlation between urban growth and city size, can thus be incorporated into an evolutionary urban theory in which towns and cities are responsible for articulating two types of relational spaces situated on two different time scales and which take into account the historical trend, based on technological progress, to a contraction of geographical space, as measured by journey time.

The construction over time of an increasingly hierarchical settlement system, marked by growing contrasts in the size of its elements, is thus a consequence not of the optimal organization of circulations in a territory at a given moment (which disqualifies static explanatory theories such as central place theory and spatial economic equilibrium), but rather of the gradual and historical adaptation of a system originally created for a particular speed of circulation and which has subsequently been transformed through the effect of faster speeds. In the course of this evolution, the system has also enabled societies to free themselves gradually from local ecological dependence, on the resources offered by their particular site, while reducing the hazards and uncertainties that threaten their survival and development, by considerably enlarging the scope for substitution and complementarity of resources, through the ability to draw on those of increasingly distant sites.

With this conception it becomes possible to combine into a unified concept the organizational duality between, first, the hierarchical organization of the urban systems that assure the territorial control and servicing, second their formation of a network for the exercise of various specialist functions. Unlike in central place theory, we do not have to accept *a priori* that there are functions which are differentiated by their threshold of appearance or their range, and which order the urban centres into a hierarchic configuration according to their size and the distance between them. These functions are actually created in the urban centres, they are a result of a process of social and spatial division of labour which produces an increasing complexification of functional levels by transforming the places which already exist.

An evolutionary theory has therefore to take into account what is referred to as *complexity*. The question remains of whether it can be translated into statistical or mathematical models and thus tested? A formalization of the modes of urban evolution would have to combine a process of systematized growth like that of Gibrat's model, a competition between urban centres to attract resources and innovations over increasingly extended spatial ranges, and a growing complexification of urban activities and social

structures consistent with specific historical trends, which are very difficult to model using the classic modelling methods, such as dynamic models based on differential equations. Computer simulation methods like that of multiagent systems alone appear to have the capacity to combine in a single model the number of elementary theoretical propositions (rules) that are necessary for even a very basic description of the evolution of an urban system (Bura *et al.*, 1996).

Conclusion

A fundamental link between the city and communication was established by J. Remy and L. Voyé, who defined urbanization as 'a process which integrates spatial mobility into daily life' (1992, p.7). We have defined the essential function* of an urban system in a particular territory as being that of articulating two forms which relate societies to their environment, or two modes of production of geographical space, each possessing its own speed of circulation and hence its specific scale of geographical organization. More than for other social systems, the similarities in the specific organization of urban systems, their universal structure in varied geographical milieus, economic systems and socio-political organizations, cannot be explained without reference to this shared territorial function, and without relating it also to the transcultural but historical processes of the urban transition and the time-space convergence. Urban systems in their present form are the result of these two processes, which have produced a far-reaching transformation of the practical forms of their main function, of what in terms of spatial organization has been their constant meaning, which is to articulate the territories of daily life and the networks of authority. Ultimately, therefore, urban systems can be said to have the function of reducing local uncertainty by establishing the connectedness of places, achieving this continuous adaptation through changes in the size of the two types of territory.

As an alternative to the intractable logical problems of static urban theories, our solution is to conceptualize the urban system as a form of adaptation to the change that is generated by human societies, an invention whose technical nature is usually not apparent in the collective representations, and which is the product of historical self-organization processes. The evolutionary specificity of urban systems is to be sought in at least three related processes: in the *urban transition*, which transforms virtually all urban systems through the *expansion, concentration and diversification of a set of settlements whose original function was the agricultural use of a territory*; in the *connected, mutually informed and competitive* character of the network that human agencies form when densities increase or when urban centres develop (surplus extraction, distribution, exchange); and lastly in the fact that this network is a *spatial and historical object*, rooted in a territory which in anthropological terms does not maintain the same spatial properties over time. The systematic variation in the range of urban relations, the *time-space convergence*, is an essential process — it is this which differentiates the dynamic of urban systems from that of other dynamic systems and restores to the theory of urban systems its specifically geographical dimension. The evolutionary concept also means taking into account the creative potential of urban centres, given that flows of innovation and the creation of new wealth are the only effective explanations for continued urbanization.

An evolutionary conception necessitates a fundamental revision of our representations and methods of analyzing change in geographical space. A key regulator — perhaps the

key regulator — of the size of territorial entities is the *range of spatial interactions*. It is important that this be measured in terms that are socially significant, that is in time rather than in kilometres. It is this time-space measure which will define the geographical entities that are no longer fixed and made immutable by topographical markers or political boundaries, but evolutionary, expanding within the earth-space framework. If we want to construct an evolutionary theory of these objects, it is necessary to examine at an interval of time the same object in a geographical delimitation which corresponds to the range of its present interactions. Consider two examples: if an urban place is defined as a portion of the earth-space in which relations are structured by a centre which can be reached in under an hour, the surface that entity covered in 1950 would be roughly double what it was in 1800, and roughly the double of the 1950 figure in 1990. Examination of this object, which in the relational space-time would be consistently defined as a 'town' or 'city', is unlikely to reveal the pattern of growth followed by decline in the central area and continuous growth in peripheral districts ever further (physically) from the centre, as proclaimed by the theorists of 'counterurbanisation' (for a critical review see Davies, 1994) and whose forms have been well described by the specialists of periurbanisation. On the contrary, the likelihood is that the town or city defined in an evolutionary way will be found to present a sustained trend to growth, compared with its periphery. Similarly, many of the debates over the 'urban exodus' to smaller local spaces could also be interpreted as extensions, in the light of the extension of the spatial range of interactions.

These notions of evolutionary spatial entities can also help geographers to improve their contribution to certain questions of forecasting: regarding the nature of the post-urban transition, that is about the future evolution of urban systems, the increasing speed of inter-urban circulation and the extension of relational networks leave no doubt about the continuing trend to concentration: in a space-time that is smaller in relation to the space-context, an urban network comprising fewer urban places is the transformed equivalent of the earlier urban network. Finally, an evolutionary perspective invites us to take a different view of what are assumed to be the optimal forms in regional planning: the same mechanisms of change may have produced slightly different forms of urban system (for example, French or Romanian centralized network as compared with the networks found in the Rhineland), which constitute so many *varieties* that are equally viable and not interchangeable with each other, with the capacity of adapting to the changes that are occurring without their structures necessarily becoming more similar. There is no optimal urban system, there are just systems which continue to adapt.

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