A convenient truth between-subject random incentives and preferences towards risk and time

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IRISK Seminar, December 2021

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Introduction

Real incentives

Economists have access to

- revealed preferences: no control
 - impossibility to identify all the possible factors impacting the decisions
 - impossibility to identify causality
 - impossibility to address non-existing contexts
- stated preferences: not incentivized
 - respondents may not respond seriously
 - respondents may give socially-desirable answers

Experimental economists design incentivized choices in controlled environments

- experimentalists design and manipulate the choice environment
- subjects are incentivized to provide sincere answers

	Incentives	Control		
Revealed preferences	\checkmark			
Stated preferences		\checkmark		
Economic experiments	\checkmark	\checkmark		

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Economic experiments	✓	\checkmark

The random incentive system: motivation

More often than not, we ask more than one question...

- in order to address consistency (e.g. Allais paradoxes)
- because repetition changes the choice situation (e.g. repeated games)
- in order to reduce the average time cost of data collection (recruiting and instructing subjects is a high fixed cost)

However, incentivizing all the choices

- can create wealth effects
- can create portfolio effects
- can be costly

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The random incentive system consists in randomly selecting one option that is payed

If the questions consist in categorical answers: one of the questions is selected and the chosen option is payed

If the questions consist in continuous answers (e.g. WTP, probability, indifference)

- the continuous answer is approximated by a series of questions, grouped in a list
- the Becker DeGroot Marschak (BDM) procedure can be used
 - a subject bids b for a good G
 - a random number v is generated
 - if $b \ge v$ the subject must buy the good for v
 - if b < v the subject does not pay and does not get the good

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Between-subject random incentives

Even with the random incentive system, experimentalists are constrained by the magnitude of the choice consequences e.g. the maximum outcome in the Holt and Laury (2002) task is \$3.85

This is problematic because

- real economic decisions involve larger consequences
- the literature has reported magnitude effects
 - for risk preferences (?, ?)
 - for time preferences (?)

A solution consists in considering larger consequences, and applying the random incentive system only to a fraction π of subjects

- Each subject has a probability π to be selected
- If the subject is selected, one of her choice is payed

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A distinction introduced by ?

	Number of choices		
Selection probability π	1	> 1	
0	hypothetical		
$0 < \pi < 1$	BRIS	HRIS	
$\pi = 1$	IS	WRIS	

What we do

We focus on the selection probability π

We measure the impact of π on risk and time preferences

	Number of choices		
Selection probability π	1	> 1	
0	hypothetical		
$0 < \pi < 1$	BRIS	HRIS	
$\pi = 1$	IS	WRIS	

Contributions

- an empirical answer to a question frequently asked by referees
- some insights about preferences towards risk and time

Modeling risk and time preferences

Under risk, choice objects are lotteries, i.e. probability distributions over outcomes Under the model of rational choice, Expected Utility (EU), a lottery $(x_1, p_1; ...; x_k, p_k)$ is valued

 $\Sigma_i p_i u(x_i)$

EU assumes

- reduction of compound lotteries for $P = (x_1, p_1; ...; x_k, q_k)$, $R = (x_1, r_1; ...; x_k, r_k)$ and $\lambda \in [0, 1]$, $\lambda P + (1 - \lambda)R$ is the lottery $(x_1, \lambda p_1 + (1 - \lambda)r_1; ...; x_k, \lambda p_k + (1 - \lambda)r_k)$
- **independence**: for any three lotteries P, Q and R and $\lambda \in [0, 1]$, $P \succ Q \Leftrightarrow \lambda P + (1 - \lambda)R \succ \lambda Q + (1 - \lambda)R$

Risk preferences: behavioral approach

• Violation of independence Allais' paradoxes challenge the independence axiom

Common ratio effect

 $P = (90,1) \ Q = (100,0.9;0)$ and $\lambda = 0.1$

 $90 \succ (100, 0.9; 0)$ but $(90, 0.1; 0) \prec (100, 0.09; 0)$

• Editing According to Prospect Theory (?) Subjects do not always reduce compound lotteries, $\lambda P + (1 - \lambda)R$ vs $\lambda Q + (1 - \lambda)R$ is treated as P vs Q • Violation of independence Allais' paradoxes challenge the independence axiom

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According to Prospect Theory (?) Subjects do not always reduce compound lotteries, $\lambda P + (1 - \lambda)R \text{ vs } \lambda Q + (1 - \lambda)R \text{ is treated as } P \text{ vs } Q$ For inter-temporal choice, objects are streams of dated outcomes Under the model of rational choice, discounted utility (DU), a lottery $(x_1, t_1; ...; x_k, t_k)$ is valued

 $\Sigma_i D(t_i) u(x_i)$ with $D(t_i) = e^{-\rho t_i}$

DU assumes that

- future outcomes are received for sure
- discounting is exponential

Time preferences: behavioral approach

Many anomalies have been listed ?

- non constant discounting
- gain loss asymmetry
- magnitude effect
- sub additivity

The most documented one is present bias

$$(x,0) \succ (y,t)$$
 but $(x,\Delta) \prec (y,t+\Delta)$

that is accommodated by non-exponential discount functions

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When risk and time are combined, the usual framework is that objects of choice are lotteries over streams of outcomes $[(x_{1,1}, t_1; \ldots; x_{1,k}, t_k), p_1; \ldots; (x_{m,1}, t_1; \ldots; x_{m,k}, t_k), p_m]$ is valued

 $\sum_i p_i [\sum_j D(t_j) u(x_{i,j})]$

DEU assumes that

- the utility of risk is the same as the utility of time
- discounting under certainty is the same as discounting under uncertainty

- A "recent" literature questions DEU (e.g. Epper and Fehr Duda, 2018)
 - the utility for risk is not the utility for time (e.g. ?) the former is concave, whereas the latter is close to linear
 - discounting under certainty is not discounting under risk (e.g. ?)
 - more patience is observed under risk
 - If present bias is due to a "certainty effect", then it should be reduced when both the present and the future are risky (?)

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The possible impact of π

Dilution

According to ?

- the expected reward of the decision must exceed the decision cost
- otherwise, errors are increased, as well as deviations from the predictions of rational models
- Random incentive systems decrease (delude) expected value of the reward through $% \left({{{\left({{{\left({{{\left({{{c}} \right)}} \right.} \right.} \right.} \right.}}} \right)$
 - the number of choices (in WRIS)
 - the selection probability π (in HRIS)

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- ullet risk aversion should increase when π increases
- ullet impatience should decrease when π increases

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The random incentive system creates a meta lottery over choices Consider two binary choices: P_1 vs Q_1 and P_2 vs Q_2

• With WRIS and reduction, the two choices are into one choice between four lotteries

 $(P_1, 0.5; P_2, 0.5)$ $(P_1, 0.5; Q_2, 0.5)$ $(Q_1, 0.5; P_2, 0.5)$ $(Q_1, 0.5; Q_2, 0.5)$

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 $(P_1, 0.5\pi; P_2, 0.5\pi; 0)$ $(P_1, 0.5\pi; Q_2, 0.5\pi; 0)$ $(Q_1, 0.5\pi; P_2, 0.5\pi; 0)$ $(Q_1, 0.5\pi; Q_2, 0.5\pi; 0)$ $(Q_1, 0.5\pi; Q_2, 0.5\pi; 0)$

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Preferences measured under RIS are valid if the independence axiom holds, or if subject isolate choices

Available studies on WRIS concluded that the subjects isolate choices (?, ?) \Rightarrow WRIS is valid, even though the independence axiom is violated

In the present study, we do not address the validity of WRIS, we assume that subjects isolate each choice from the series of choices

However, subjects may (easily) compound each lottery with the selection probability π

A binary choices: P vs Q would be turned into $(P, \pi; 0)$ vs $(Q, \pi; 0)$

In this case, according to the common ratio effect, we should observe more risk taking when $\pi < 1$

- We consider the possible impact of π on inter-temporal choices
 A binary choices: P vs Q would be turned into (P,π;0) vs (Q,π;0)
- If subject do not isolate from time choices from π we should observe:
 - less impatience when $\pi < 1$
 - less present bias when $\pi < 1$

A series of hypothesis

	for risk	for time
compounding	more risk taking for $0 < \pi < 1$ than for $\pi = 1$	more patience for $0 < \pi < 1$ than for $\pi = 1$
compounding		less present bias for $0<\pi<1$ than for $\pi=1$
dilution	more risk taking and more errors for $\pi < 1$ than for $\pi = 1$	more impatience and more errors for $\pi < 1$ than for $\pi = 1$
dilution	more inverse S for $\pi < 1$ than for $\pi = 1$	more present bias and more errors for $\pi < 1$ than for $\pi = 1$
isolation	no difference	no difference

Table: Hypothesis about the impact of ρ on risk and time preferences

The experiment

Measuring risk and time preferences

The stimuli we consider

- four certainty equivalents $ce \sim (x, p; y)$
- four sooner equivalents (se, t) \sim (x, t + au)

Risk				Time	
×	у	р	x	τ	t
80	0	0.25	80	3	0
80	0	0.50	80	6	0
80	0	0.75	80	12	0
100	20	0.5	80	6	6

The indifferences are elicited using four steps of bisection: this gives a precision of ± 2.5 euros.

Advertising: these stimuli

- have been used in ELIPSS survey: 2000 respondents representative of French population, with about 200 questions about socio-economic, health and food behavior
- should be included in CONSTANCE cohort: 20,000 respondents representative of French population, with additional question and matching with health data

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The display



L'option A vous donne 75% de chance de gagner 80€ et 25% de chance de gagner 0€.

L'option B vous donne 40€ de façon certaine.



Vous devez choisir entre l'option A ou l'option B. Cliquez sur l'option que vous préférez puis validez.

L'option A est un montant de 80€ que vous recevrez dans 3 mois.

L'option B est un montant de 40€ que vous recevrez demain.



- risk and time measurements are made in a within-subject design
- ullet treatments related to π are made in a between-subject design

	0	0.1	0.5	1	Total
n	84	81	88	82	335
Expected gain	0	6üŸŒ	30üŸŒ	60üŸŒ	

Procedure

- Subjects recruited from the INSEAD Lab
- Zoom sessions ran in March and April 2021 between 13 and 20 participants
 - instructions made by the experimenter, using a beamer
 - all the subjects from a given session belong to the same treatment
- Implementation of the incentives
 - a lottery played probability π to determine if WRIS applies
 - a lottery with probability 0.5 determines if the selected choice deals with risk or time
 - a lottery choses among the four stimuli *S* for which an indifference has been measured.
 - for the given stimuli, a value v is chosen in $\{5, \ldots, 75\}$,
 - if v is larger than the indifference value, the subject receives v
 - otherwise, she receives S

The results

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Risk data



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	(80,0.25;0)	(80,0.5;0)	(80,0.75;0)	(100, 0.5; 20)
0 vs 0.1	0.016	< 0.001	0.0012	0.03
0.1 vs 0.5	0.57	0.740	0.61	0.58
0.5 vs 1	0.81	0.37	0.11	0.98
Anova ($\pi \in \{0, 0.1, 0.5, 1\}$)	0.063	0.041	0.005	0.001
Anova $(\pi \in \{0.1, 0.5, 1\})$	0.71	0.82	0.31	0.31
BF $(\pi \in \{0.1, 0.5, 1\})$	0.06	0.05	0.12	0.12

Time data



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	$(se, 0) \sim (80, 3)$	$(se,0)$ \sim $(80,6)$	$(se,0)\sim(80,12)$	$(se,6)$ \sim $(80,12)$
0 vs 0.1	0.90	0.66	0.37	0.81
0.1 vs 0.5	0.79	0.83	0.49	0.38
0.5 vs 1	0.44	0.61	0.73	0.63
Anova $(\pi \in \{0, 0.1, 0.5, 1\})$	0.82	0.91	0.73	0.88
BF $(\pi \in \{0, 0.1, 0.5, 1\})$	0.06	0.05	0.06	0.05

Bayesian ANOVA

- We consider two models M_1 and M_0 with M_0 enforcing the Null
- The Bayes factor is

$$B_{10} = rac{Pr(Data|M_1)}{Pr(Data|M_0)} = rac{1}{B_{01}}$$

- The base factor
 - offers a benchmark to compare the likelihood of the data
 - allows to support the Null
 - allows the analyst to use her own priors

$$\frac{Pr(M_1|Data)}{Pr(M_0|Data)} = B_{10} \frac{Pr(M_0)}{Pr(M_1)}$$

• Rouder et al. (2012) propose "convenient" and "plausible" priors to compute BF in the context of ANOVAs.

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The models

We considered 3 models

- DEU
- Hyperbolic Rank Dependent Utility (HRDU): with probability weighting and quasi-hyperbolic discounting
- Hyperbolic Rank Dependent Utility 2 (HRDU2): with probability weighting and quasi-hyperbolic discounting, and a linear utility for time

	Models		
Model	CE $ce \sim (x, p; y)$	SE (se, t) \sim (x, t + τ)	
DEU	$u^{-1}[p[u(x) - u(y)] + u(y)]$	$u^{-1}[e^{-\rho\tau}u(x)]$	
HRDU	$u^{-1}[w(p)[u(x) - u(y)] + u(y)]$	$u^{-1}\left[\frac{D(t+\tau)}{D(t)}u(x)\right]$	
HRDU2	$u^{-1}[w(p)[u(x) - u(y)] + u(y)]$	$\frac{D(t+ au)}{D(t)}X$	

The specifications

The specification

- Power utility function: $u(x) = x^{\alpha}$
- Prelec (one-parameter) weighting function: $w(p) = e^{-[-log(p)]^{\gamma}}$
- Quasi-hyperbolic discounting

$$D(t) = 1$$
 for $t = 0$
= $\beta e^{-\rho t}$ for $t > 0$

 \bullet Normally distributed errors on CEs and SEs, with different std σ Estimation by (log)likelihood maximization

Capturing treatment effects

The specification

Comparing treatments two-by-two
 For each coefficient θ, we consider that

$$\theta = \theta_0 + \Delta_{0.1-0} \mathbf{1}_{\pi=0.1} + (\Delta_{0.1-0} + \Delta_{0.5-0.1}) \mathbf{1}_{\pi=0.5} + (\Delta_{0.1-0} + \Delta_{0.5-0.1} + \Delta_{1-0.5}) \mathbf{1}_{\pi=0.5}$$
 such that:

$$\Delta_{m-n}=\theta_m-\theta_n$$

 $\bullet\,$ HRIS ws hypothetical and WRIS: treatments $\pi=0.1$ and $\pi=0.5$ are grouped in "HRIS"

$$\theta = \theta_{HRIS} + \Delta_{Hyp} 1_{\pi=0} + \Delta_{Wris} 1_{\pi=1}$$

• Linear effect of π : we focus on case where $\pi > 0$ and we consider that $\theta = \theta_c + s\pi$

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Results: reference treatment

Parameter	DEU	HRDU	HRDU2
α	0.798 (0.046)	0.90 (0.039)	0.90 (0.039)
δ_0	0.054 (0.006)	0.046 (0.005)	0.051 (0.005)
β_0		0.861 (0.023)	0.847 (0.028)
γο		0.671 (0.040)	0.671 (0.039)
σ_0^r	14.65 (2.15)	13.95 (1.948)	13.95 (4.86)
σ_0^t	21.42 (4.96)	20.84 (0.744)	20.84 (3.71)
LL	-7388.14	-7255.68	-7255.68

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Results: treatment effects

Parameter		DEU		HDRDU		HDRDU2	
α	$\alpha_{0.1} - \alpha_0$	-0.239	0.000	-0.164	0.004	-0.164	0.003
	$\alpha_{0.5} - \alpha_{0.1}$	-0.012	0.853	-0.015	0.775	-0.015	0.790
	$\alpha_1 - \alpha_{0.5}$	0.073	0.239	0.041	0.433	0.041	0.472
δ	$\delta_{0.1} - \delta_0$	-0.017	0.020	-0.012	0.060	-0.005	0.476
	$\delta_{0.5} - \delta_{0.1}$	0.002	0.774	0.004	0.495	0.006	0.384
	$\delta_1 - \delta_{0.5}$	0.004	0.569	0.002	0.695	0.000	0.973
β	$\beta_{0.1} - \beta_0$			0.002	0.948	-0.028	0.489
	$\beta_{0.5} - \beta_{0.1}$			0.013	0.586	0.014	0.670
	$\beta_1 - \beta_{0.5}$			0.012	0.631	0.023	0.470
γ	γ _{0.1} - γ ₀			-0.158	0.005	-0.158	0.007
	Yo.5 - Yo.1			-0.001	0.985	-0.001	0.989
	$\gamma_1 - \gamma_{0.5}$			0.070	0.254	0.070	0.351
	$\sigma_{0.1}^r - \sigma_0^r$	2.445	0.076	1.784	0.322	1.784	0.840
σ_0^r	$\sigma_{0.5}^{r} - \sigma_{0.1}^{r}$	-0.084	0.970	-0.111	0.978	-0.111	0.986
	$\sigma_1^r - \sigma_{0.5}^r$	0.128	0.934	0.500	0.942	0.500	0.939
σ_0^t	$\sigma_{0.1}^t - \sigma_0^t$	1.553	0.592	1.324	0.373	1.323	0.872
	$\sigma_{0.5}^t - \sigma_{0.1}^t$	-0.854	0.837	-0.717	0.741	-0.716	0.919
	$\sigma_1^t - \sigma_{0.5}^t$	-0.776	0.776	-0.608	0.736	-0.608	0.927
LL		-7418.426	0.000	-7286.503	0.000	-7286.503	0.000

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Illustration: under DEU



Illustration: under HRDU



Other specifications: HRIS vs hypothetical and WRIS

Parameter		DEU		HRDU		HRDU2	
α	$\alpha_0 - \alpha_{0 < \rho < 1}$	0.245	0.000	0.172	0.000	0.172	0.000
	$\alpha_{0 < \rho < 1} - \alpha_1$	0.067	0.222	0.034	0.462	0.034	0.467
δ	$\delta_{0< ho<1}-\delta_0$	0.016	0.011	0.010	0.077	0.002	0.774
	$\delta_{0< ho<1}-\delta_1$	0.004	0.421	0.004	0.422	0.003	0.605
β	$\beta_0 - \beta_{0 < \rho < 1}$			-0.009	0.725	0.021	0.482
	$\beta_{0< ho<1}-eta_1$			0.018	0.417	0.030	0.301
γ	$\gamma_0 - \gamma_{0 < \rho < 1}$			0.159	0.001	0.159	0.001
	$\gamma_{0< ho<1}-\gamma_{1}$			0.069	0.194	0.069	0.193
σ_0^r	$\sigma_0^r - \sigma_{0 < \rho < 1}^r$	-2.403	0.115	-1.728	0.009	-1.728	0.027
	$\sigma_{0<\rho<1}^r - \sigma_1^r$	0.086	0.966	0.445	0.603	0.445	0.618
σ_0^t	$\sigma_0^t - \sigma_{0 < \rho < 1}^t$	-1.124	0.553	-0.969	0.291	-0.969	0.559
	$\sigma_{0< ho<1}^t-\sigma_1^t$	-1.201	0.316	-0.970	0.495	-0.969	0.346
LL		-7388.823		-7256.445		-7256.445	
		-7418.426	0.000	-7286.503	0.000	-7286.503	0.000

Other specifications: linear effect of π when $\pi > 0$

Parameter		DEU		HDRDU		HDRDU2	
	α	0.070	0.317	0.030	0.601	0.030	0.745
	δ	0.006	0.416	0.007	0.327	0.007	0.487
$slope of \pi$	β			0.028	0.342	0.042	0.360
slope of <i>n</i>	γ			0.077	0.248	0.078	0.549
	σ^r	0.053	0.968	0.449	0.766	0.448	0.963
	σ^t	-1.794	0.044	-1.458	0.400	-1.458	0.886
LL		-5583.121		-5476.502		-5476.50	
		-5585.377	0.34	-5479.01	0.54	-5479.01	0.54

Discussion

We report the first study investigating the impact of the selection probability π on risk and time preferences

for risk:

- a difference between $\pi=0$ and $\pi>0$
- no difference between treatments when $\pi>0$
- for time
 - no impact of π

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- for time
 - ${\scriptstyle \bullet}$ no impact of π

Preliminary conclusion: real incentive matter but subjects isolate from π

Additional findings

- Inverse S probability weighting is
 - more pronounced for $\pi > 0$
 - not due do absence of incentives
- Under DEU, controlling for the time utility using the risk utility may create distortions
 - here it creates the spurious impression that incentives impact discounting
 - another illustration that risk preferences are not time preferences (incentives impact the risk utility but not the time utility)

	for risk	for time
compounding	more risk taking for $0 < \pi < 1$ than for $\pi = 1$	more patience for $0 < \pi < 1$ than for $\pi = 1$
		less present bias for $0 < \pi < 1$ than for $\pi = 1$
dilution	more risk taking and more errors for $\pi < 1$ than for $\pi = 1$	more impatience and more errors for $\pi < 1$ than for $\pi = 1$
	more inverse S for $\pi < 1$ than for $\pi = 1$	more present bias and more errors for $\pi < 1$ than for $\pi = 1$
isolation	no difference	no difference

- The random incentive system creates complexity about
 - how questions are selection
 - how lotteries are played
- In order to avoid this complexity, subject may select the sure outcome more often which would produce
 - more risk aversion
 - more certainty effect, hence more inverse S probability weighting

Thank you!

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