## A convenient truth between-subject random incentives and preferences towards risk and time

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## Introduction

## Real incentives

Economists have access to

- revealed preferences: no control
- impossibility to identify all the possible factors impacting the decisions
- impossibility to identify causality
- impossibility to address non-existing contexts
- stated preferences: not incentivized
- respondents may not respond seriously
- respondents may give socially-desirable answers

Experimental economists design incentivized choices in controlled environments

- experimentalists design and manipulate the choice environment
- subjects are incentivized to provide sincere answers



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Experimental economists design incentivized choices in controlled environments

- experimentalists design and manipulate the choice environment
- subjects are incentivized to provide sincere answers

|  | Incentives | Control |
| :---: | :---: | :---: |
| Revealed preferences | $\checkmark$ |  |
| Stated preferences |  | $\checkmark$ |
| Economic experiments | $\checkmark$ | $\checkmark$ |

## The random incentive system: motivation

More often than not, we ask more than one question...

- in order to address consistency
(e.g. Allais paradoxes)
- because repetition changes the choice situation (e.g. repeated games)
- in order to reduce the average time cost of data collection (recruiting and instructing subjects is a high fixed cost)

However, incentivizing all the choices

- can create wealth effects
- can create portfolio effects
- can be costly


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However, incentivizing all the choices

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The random incentive system consists in randomly selecting one option that is payed

## The random incentive system: principle

If the questions consist in categorical answers:
one of the questions is selected and the chosen option is payed
If the questions consist in continuous answers (e.g. WTP, probability, indifference)

- the continuous answer is approximated by a series of questions, grouped in a list
- the Becker DeGroot Marschak (BDM) procedure can be used
- a subject bids $b$ for a good $G$
- a random number $v$ is generated
- if $b \geq v$ the subject must buy the good for $v$
- if $b<v$ the subject does not pay and does not get the good


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## Between-subject random incentives

Even with the random incentive system, experimentalists are constrained by the magnitude of the choice consequences
e.g. the maximum outcome in the Holt and Laury (2002) task is $\$ 3.85$

This is problematic because

- real economic decisions involve larger consequences
- the literature has reported magnitude effects
- for risk preferences (?, ?)
- for time preferences (?)

A solution consists in considering larger consequences, and applying the random incentive system only to a fraction $\pi$ of subjects

- Each subject has a probability $\pi$ to be selected
- If the subject is selected, one of her choice is payed


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## Vocabulary: RIS, WRIS, BRIS and WRIS

A distinction introduced by?

|  | Number of choices |  |
| :---: | :---: | :---: |
| Selection probability $\pi$ | 1 |  |
| 0 | hypothetical |  |
| $0<\pi<1$ | BRIS | HRIS |
| $\pi=1$ | IS | WRIS |

## What we do

We focus on the selection probability $\pi$
We measure the impact of $\pi$ on risk and time preferences

|  | Number of choices |  |
| :---: | :---: | :---: |
| Selection probability $\pi$ | 1 |  |
| 0 | hypothetical |  |
| $0<\pi<1$ | BRIS | HRIS |
| $\pi=1$ | IS | WRIS |

Contributions

- an empirical answer to a question frequently asked by referees
- some insights about preferences towards risk and time

Modeling risk and time preferences

## Risk preferences: normative approach

Under risk, choice objects are lotteries, i.e. probability distributions over outcomes Under the model of rational choice, Expected Utility (EU), a lottery $\left(x_{1}, p_{1} ; \ldots ; x_{k}, p_{k}\right)$ is valued

$$
\Sigma_{i} p_{i} u\left(x_{i}\right)
$$

EU assumes

- reduction of compound lotteries for $P=\left(x_{1}, p_{1} ; \ldots ; x_{k}, q_{k}\right), R=\left(x_{1}, r_{1} ; \ldots ; x_{k}, r_{k}\right)$ and $\lambda \in[0,1]$, $\lambda P+(1-\lambda) R$ is the lottery $\left(x_{1}, \lambda p_{1}+(1-\lambda) r_{1} ; \ldots ; x_{k}, \lambda p_{k}+(1-\lambda) r_{k}\right)$
- independence: for any three lotteries $P, Q$ and $R$ and $\lambda \in[0,1]$, $P \succ Q \Leftrightarrow \lambda P+(1-\lambda) R \succ \lambda Q+(1-\lambda) R$


## Risk preferences: behavioral approach

- Violation of independence

Allais' paradoxes challenge the independence axiom

| Common ratio effect |
| :---: |
| $P=(90,1) Q=(100,0.9 ; 0)$ and $\lambda=0.1$ |
| $90 \succ(100,0.9 ; 0)$ but $(90,0.1 ; 0) \prec(100,0.09 ; 0)$ |

- Editing

According to Prospect Theory (?)
Subjects do not always reduce compound lotteries,
$\lambda P+(1-\lambda) R$ vs $\lambda Q+(1-\lambda) R$ is treated as $P$ vs $Q$

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Common ratio effect

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According to Prospect Theory (?)
Subjects do not always reduce compound lotteries, $\lambda P+(1-\lambda) R$ vs $\lambda Q+(1-\lambda) R$ is treated as $P$ vs $Q$

## Time preferences: normative approach

For inter-temporal choice, objects are streams of dated outcomes Under the model of rational choice, discounted utility (DU), a lottery $\left(x_{1}, t_{1} ; \ldots ; x_{k}, t_{k}\right)$ is valued

$$
\Sigma_{i} D\left(t_{i}\right) u\left(x_{i}\right) \text { with } D\left(t_{i}\right)=e^{-\rho t_{i}}
$$

DU assumes that

- future outcomes are received for sure
- discounting is exponential


## Time preferences: behavioral approach

Many anomalies have been listed?

- non constant discounting
- gain loss asymmetry
- magnitude effect
- sub additivity

The most documented one is present bias

$$
(x, 0) \succ(y, t) \text { but }(x, \Delta) \prec(y, t+\Delta)
$$

that is accommodated by non-exponential discount functions

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## Risk and time: normative approach

When risk and time are combined, the usual framework is that objects of choice are lotteries over streams of outcomes $\left[\left(x_{1,1}, t_{1} ; \ldots ; x_{1, k}, t_{k}\right), p_{1} ; \ldots ;\left(x_{m, 1}, t_{1} ; \ldots ; x_{m, k}, t_{k}\right), p_{m}\right]$ is valued

$$
\Sigma_{i} p_{i}\left[\Sigma_{j} D\left(t_{j}\right) u\left(x_{i, j}\right)\right]
$$

DEU assumes that

- the utility of risk is the same as the utility of time
- discounting under certainty is the same as discounting under uncertainty


## Risk and time: behavioral approach

A "recent" literature questions DEU (e.g. Epper and Fehr Duda, 2018)

- the utility for risk is not the utility for time (e.g. ?) the former is concave, whereas the latter is close to linear
- discounting under certainty is not discounting under risk (e.g. ?)
- more patience is observed under risk
- If present bias is due to a "certainty effect", then it should be reduced when both the present and the future are risky (?)


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- more patience is observed under risk
- If present bias is due to a "certainty effect", then it should be reduced when both the present and the future are risky (?)

The possible impact of $\pi$

## Dilution

According to ?

- the expected reward of the decision must exceed the decision cost
- otherwise, errors are increased, as well as deviations from the predictions of rational models
Random incentive systems decrease (delude) expected value of the reward through
- the number of choices (in WRIS)
- the selection probability $\pi$ (in HRIS)

$$
\begin{aligned}
& \text { (it seems that) the dilution effect would create a magnitude effect } \\
& \text { - risk aversion should increase when } \pi \text { increases } \\
& \text { - impatience should decrease when } \pi \text { increases }
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(it seems that) the dilution effect would create a magnitude effect
- risk aversion should increase when $\pi$ increases
- impatience should decrease when $\pi$ increases


## Compounding

The random incentive system creates a meta lottery over choices
Consider two binary choices: $P_{1}$ vs $Q_{1}$ and $P_{2}$ vs $Q_{2}$

- With WRIS and reduction, the two choices are into one choice between four lotteries

$$
\begin{aligned}
& \left(P_{1}, 0.5 ; P_{2}, 0.5\right) \\
& \left(P_{1}, 0.5 ; Q_{2}, 0.5\right) \\
& \left(Q_{1}, 0.5 ; P_{2}, 0.5\right) \\
& \left(Q_{1}, 0.5 ; Q_{2}, 0.5\right)
\end{aligned}
$$

- With HRIS and reduction, the two choices are turned into one choice between four lotteries

$$
\begin{aligned}
& \left(P_{1}, 0.5 \pi ; P_{2}, 0.5 \pi ; 0\right) \\
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Preferences measured under RIS are valid if the independence axiom holds, or if subject isolate choices

## Compounding under WRIS and HRIS

Available studies on WRIS concluded that the subjects isolate choices (?, ?) $\Rightarrow$ WRIS is valid, even though the independence axiom is violated In the present study, we do not address the validity of WRIS, we assume that subjects isolate each choice from the series of choices However, subjects may (easily) compound each lottery with the selection probability $\pi$
A binary choices: $P$ vs $Q$ would be turned into $(P, \pi ; 0)$ vs $(Q, \pi ; 0)$ In this case, according to the common ratio effect, we should observe more risk taking when $\pi<1$

## Compounding and time

- We consider the possible impact of $\pi$ on inter-temporal choices A binary choices: $P$ vs $Q$ would be turned into $(P, \pi ; 0)$ vs $(Q, \pi ; 0)$
- If subject do not isolate from time choices from $\pi$ we should observe:
- less impatience when $\pi<1$
- less present bias when $\pi<1$


## A series of hypothesis

|  | for risk | for time |
| :---: | :---: | :---: |
| compounding | more risk taking for $0<\pi<1$ than for $\pi=1$ | more patience for $0<\pi<1$ than for $\pi=1$ |
|  |  | less present bias for $0<\pi<1$ than for $\pi=1$ |
| dilution | more risk taking and more errors for $\pi<1$ than for $\pi=1$ | more impatience and more errors for $\pi<1$ than for $\pi=1$ |
|  | more inverse $S$ for $\pi<1$ than for $\pi=1$ | more present bias and more errors for $\pi<1$ than for $\pi=1$ |
| isolation | no difference | no difference |

Table: Hypothesis about the impact of $\rho$ on risk and time preferences

The experiment

## Measuring risk and time preferences

The stimuli we consider

- four certainty equivalents $c e \sim(x, p ; y)$
- four sooner equivalents $(s e, t) \sim(x, t+\tau)$

| Risk |  |  | Time |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\times$ | y | p | x | $\tau$ | $t$ |
| 80 | 0 | 0.25 | 80 | 3 | 0 |
| 80 | 0 | 0.50 | 80 | 6 | 0 |
| 80 | 0 | 0.75 | 80 | 12 | 0 |
| 100 | 20 | 0.5 | 80 | 6 | 6 |

The indifferences are elicited using four steps of bisection: this gives a precision of $\pm 2.5$ euros.

Advertising: these stimuli

- have been used in ELIPSS survey: 2000 respondents representative of French population, with about 200 questions about socio-economic, health and food behavior
- should be included in CONSTANCE cohort: 20,000 respondents representative of French population, with additional question and matching with health data


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## The display

Voici une nouvelle série de questions dans laquellel'option A a changé.
Vous devez choisir entre l'option A ou l'option B.
Cliquez sur l'option que vous préférez puis validez.

L'option A vous donne 75\% de chance de gagner $80 €$ et $\mathbf{2 5 \%}$ de chance de gagner 0 ©.
L'option B vous donne $40 €$ de façon certaine.


Vous devez choisir entre l'option A ou l'option B. Cliquez sur l'option que vous préférez puis validez.

L'option $A$ est un montant de $80 €$ que vous recevrez dans 3 mois.
L'option B est un montant de $40 €$ que vous recevrez demain.


## The design

- risk and time measurements are made in a within-subject design
- treatments related to $\pi$ are made in a between-subject design

|  | 0 | 0.1 | 0.5 | 1 | Total |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $n$ | 84 | 81 | 88 | 82 | 335 |
| Expected gain | 0 | 6üŸGE | 30üY゙GE | 60üŸCE |  |

## Procedure

- Subjects recruited from the INSEAD Lab
- Zoom sessions ran in March and April 2021 between 13 and 20 participants
- instructions made by the experimenter, using a beamer
- all the subjects from a given session belong to the same treatment
- Implementation of the incentives
- a lottery played probability $\pi$ to determine if WRIS applies
- a lottery with probability 0.5 determines if the selected choice deals with risk or time
- a lottery choses among the four stimuli $S$ for which an indifference has been measured.
- for the given stimuli, a value $v$ is chosen in $\{5, \ldots, 75\}$,
- if $v$ is larger than the indifference value, the subject receives $v$
- otherwise, she receives $S$

The results

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Risk data


## Risk data: tests

|  | $(80,0.25 ; 0)$ | $(80,0.5 ; 0)$ | $(80,0.75 ; 0)$ | $(100,0.5 ; 20)$ |
| :---: | :---: | :---: | :---: | :---: |
| 0 vs 0.1 | 0.016 | $<0.001$ | 0.0012 | 0.03 |
| 0.1 vs 0.5 | 0.57 | 0.740 | 0.61 | 0.58 |
| 0.5 vs 1 | 0.81 | 0.37 | 0.11 | 0.98 |
| Anova $(\pi \in\{0,0.1,0.5,1\})$ | 0.063 | 0.041 | 0.005 | 0.001 |
| Anova $(\pi \in\{0.1,0.5,1\})$ | 0.71 | 0.82 | 0.31 | 0.31 |
| BF $(\pi \in\{0.1,0.5,1\})$ | 0.06 | 0.05 | 0.12 | 0.12 |

## Time data



## Time data: tests

|  | $(s e, 0) \sim(80,3)$ | $(s e, 0) \sim(80,6)$ | $(s e, 0) \sim(80,12)$ | $(s e, 6) \sim(80,12)$ |
| :---: | :---: | :---: | :---: | :---: |
| 0 vs 0.1 | 0.90 | 0.66 | 0.37 | 0.81 |
| 0.1 vs 0.5 | 0.79 | 0.83 | 0.49 | 0.38 |
| 0.5 vs 1 | 0.44 | 0.61 | 0.73 | 0.63 |
| Anova $(\pi \in\{0,0.1,0.5,1\})$ | 0.82 | 0.91 | 0.73 | 0.88 |
| BF $(\pi \in\{0,0.1,0.5,1\})$ | 0.06 | 0.05 | 0.06 | 0.05 |

## Bayesian ANOVA

- We consider two models $M_{1}$ and $M_{0}$ with $M_{0}$ enforcing the Null
- The Bayes factor is

$$
B_{10}=\frac{\operatorname{Pr}\left(\text { Data } \mid M_{1}\right)}{\operatorname{Pr}\left(\text { Data } \mid M_{0}\right)}=\frac{1}{B_{01}}
$$

- The base factor
- offers a benchmark to compare the likelihood of the data
- allows to support the Null
- allows the analyst to use her own priors

$$
\frac{\operatorname{Pr}\left(M_{1} \mid \text { Data }\right)}{\operatorname{Pr}\left(M_{0} \mid \text { Data }\right)}=B_{10} \frac{\operatorname{Pr}\left(M_{0}\right)}{\operatorname{Pr}\left(M_{1}\right)}
$$

- Rouder et al. (2012) propose "convenient" and "plausible" priors to compute BF in the context of ANOVAs.


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## The models

We considered 3 models

- DEU
- Hyperbolic Rank Dependent Utility (HRDU): with probability weighting and quasi-hyperbolic discounting
- Hyperbolic Rank Dependent Utility 2 (HRDU2): with probability weighting and quasi-hyperbolic discounting, and a linear utility for time

|  | Models |  |
| :---: | :---: | :---: |
| Model | CE $c e \sim(x, p ; y)$ | SE $(s e, t) \sim(x, t+\tau)$ |
| DEU | $u^{-1}[p[u(x)-u(y)]+u(y)]$ | $u^{-1}\left[e^{-\rho \tau} u(x)\right]$ |
| HRDU | $u^{-1}[w(p)[u(x)-u(y)]+u(y)]$ | $u^{-1}\left[\frac{D(t+\tau)}{D(t)} u(x)\right]$ |
| HRDU2 | $u^{-1}[w(p)[u(x)-u(y)]+u(y)]$ | $\frac{D(t+\tau)}{D(t)} x$ |

## The specifications

The specification

- Power utility function: $u(x)=x^{\alpha}$
- Prelec (one-parameter) weighting function: $w(p)=e^{-[-\log (p)]^{\gamma}}$
- Quasi-hyperbolic discounting

$$
\begin{aligned}
D(t) & =1 & & \text { for } t=0 \\
& =\beta e^{-\rho t} & & \text { for } t>0
\end{aligned}
$$

- Normally distributed errors on CEs and SEs, with different std $\sigma$ Estimation by (log)likelihood maximization


## Capturing treatment effects

The specification

- Comparing treatments two-by-two For each coefficient $\theta$, we consider that
$\theta=\theta_{0}+\Delta_{0.1-0} 1_{\pi=0.1}+\left(\Delta_{0.1-0}+\Delta_{0.5-0.1}\right) 1_{\pi=0.5}+\left(\Delta_{0.1-0}+\Delta_{0.5-0.1}+\Delta_{1-0.5}\right) 1_{\pi=}$ such that:

$$
\Delta_{m-n}=\theta_{m}-\theta_{n}
$$

- HRIS ws hypothetical and WRIS: treatments $\pi=0.1$ and $\pi=0.5$ are grouped in "HRIS"


## Capturing treatment effects

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$\theta=\theta_{0}+\Delta_{0.1-0} 1_{\pi=0.1}+\left(\Delta_{0.1-0}+\Delta_{0.5-0.1}\right) 1_{\pi=0.5}+\left(\Delta_{0.1-0}+\Delta_{0.5-0.1}+\Delta_{1-0.5}\right) 1_{\pi=}$ such that:

$$
\Delta_{m-n}=\theta_{m}-\theta_{n}
$$

- HRIS ws hypothetical and WRIS: treatments $\pi=0.1$ and $\pi=0.5$ are grouped in "HRIS"

$$
\theta=\theta_{H R I S}+\Delta_{\text {Hyp }} 1_{\pi=0}+\Delta_{\text {Wris }} 1_{\pi=1}
$$

- Linear effect of $\pi$ : we focus on case where $\pi>0$ and we consider that $\theta=\theta_{c}+s \pi$


## Capturing treatment effects

The specification

- Comparing treatments two-by-two For each coefficient $\theta$, we consider that
$\theta=\theta_{0}+\Delta_{0.1-0} 1_{\pi=0.1}+\left(\Delta_{0.1-0}+\Delta_{0.5-0.1}\right) 1_{\pi=0.5}+\left(\Delta_{0.1-0}+\Delta_{0.5-0.1}+\Delta_{1-0.5}\right) 1_{\pi=}$ such that:

$$
\Delta_{m-n}=\theta_{m}-\theta_{n}
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- Linear effect of $\pi$ : we focus on case where $\pi>0$ and we consider that $\theta=\theta_{c}+s \pi$


## Results: reference treatment

| Parameter | DEU | HRDU | HRDU2 |
| :---: | :---: | :---: | :---: |
| $\alpha_{0}$ | $0.798(0.046)$ | $0.90(0.039)$ | $0.90(0.039)$ |
| $\delta_{0}$ | $0.054(0.006)$ | $0.046(0.005)$ | $0.051(0.005)$ |
| $\beta_{0}$ |  | $0.861(0.023)$ | $0.847(0.028)$ |
| $\gamma_{0}$ |  | $0.671(0.040)$ | $0.671(0.039)$ |
| $\sigma_{0}^{r}$ | $14.65(2.15)$ | $13.95(1.948)$ | $13.95(4.86)$ |
| $\sigma_{0}^{t}$ | $21.42(4.96)$ | $20.84(0.744)$ | $20.84(3.71)$ |
| LL | -7388.14 | -7255.68 | -7255.68 |

## Results: treatment effects

| Parameter |  | DEU |  | HDRDU |  | HDRDU2 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\alpha$ | $\alpha_{0.1}-\alpha_{0}$ | -0.239 | 0.000 | -0.164 | 0.004 | -0.164 | 0.003 |
|  | $\alpha_{0.5}-\alpha_{0.1}$ | -0.012 | 0.853 | -0.015 | 0.775 | -0.015 | 0.790 |
|  | $\alpha_{1}-\alpha_{0.5}$ | 0.073 | 0.239 | 0.041 | 0.433 | 0.041 | 0.472 |
| $\delta$ | $\delta_{0.1}-\delta_{0}$ | -0.017 | 0.020 | -0.012 | 0.060 | -0.005 | 0.476 |
|  | $\delta_{0.5}-\delta_{0.1}$ | 0.002 | 0.774 | 0.004 | 0.495 | 0.006 | 0.384 |
|  | $\delta_{1}-\delta_{0.5}$ | 0.004 | 0.569 | 0.002 | 0.695 | 0.000 | 0.973 |
| $\beta$ | $\beta_{0.1}-\beta_{0}$ |  |  | 0.002 | 0.948 | -0.028 | 0.489 |
|  | $\beta_{0.5}-\beta_{0.1}$ |  |  | 0.013 | 0.586 | 0.014 | 0.670 |
|  | $\beta_{1}-\beta_{0.5}$ |  |  | 0.012 | 0.631 | 0.023 | 0.470 |
| $\gamma$ | $\gamma_{0.1}-\gamma_{0}$ |  |  | -0.158 | 0.005 | -0.158 | 0.007 |
|  | $\gamma_{0.5}-\gamma_{0.1}$ |  |  | -0.001 | 0.985 | -0.001 | 0.989 |
|  | $\gamma_{1}-\gamma_{0.5}$ |  |  | 0.070 | 0.254 | 0.070 | 0.351 |
| $\sigma_{0}^{r}$ | $\sigma_{0.1}^{r}-\sigma_{0}^{r}$ | 2.445 | 0.076 | 1.784 | 0.322 | 1.784 | 0.840 |
|  | $\sigma_{0.5}^{r}-\sigma_{0.1}^{r}$ | -0.084 | 0.970 | -0.111 | 0.978 | -0.111 | 0.986 |
|  | $\sigma_{1}^{r}-\sigma_{0.5}^{r}$ | 0.128 | 0.934 | 0.500 | 0.942 | 0.500 | 0.939 |
| $\sigma_{0}^{t}$ | $\sigma_{0.1}^{t}-\sigma_{0}^{t}$ | 1.553 | 0.592 | 1.324 | 0.373 | 1.323 | 0.872 |
|  | $\sigma_{0.5}^{t}-\sigma_{0.1}^{t}$ | -0.854 | 0.837 | -0.717 | 0.741 | -0.716 | 0.919 |
|  | $\sigma_{1}^{t}-\sigma_{0.5}^{t}$ | -0.776 | 0.776 | -0.608 | 0.736 | -0.608 | 0.927 |
|  | LL | -7418.426 | 0.000 | -7286.503 | 0.000 | -7286.503 | 0.000 |

## Illustration: under DEU




## Illustration: under HRDU




## Other specifications: HRIS vs hypothetical and WRIS

| Parameter |  | DEU |  | HRDU |  | HRDU2 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\alpha$ | $\alpha_{0}-\alpha_{0<\rho<1}$ | 0.245 | 0.000 | 0.172 | 0.000 | 0.172 | 0.000 |
|  | $\alpha_{0<\rho<1}-\alpha_{1}$ | 0.067 | 0.222 | 0.034 | 0.462 | 0.034 | 0.467 |
| $\delta$ | $\delta_{0<\rho<1}-\delta_{0}$ | 0.016 | 0.011 | 0.010 | 0.077 | 0.002 | 0.774 |
|  | $\delta_{0<\rho<1}-\delta_{1}$ | 0.004 | 0.421 | 0.004 | 0.422 | 0.003 | 0.605 |
| $\beta$ | $\beta_{0}-\beta_{0<\rho<1}$ |  |  | -0.009 | 0.725 | 0.021 | 0.482 |
|  | $\beta_{0<\rho<1}-\beta_{1}$ |  |  | 0.018 | 0.417 | 0.030 | 0.301 |
| $\gamma$ | $\gamma_{0}-\gamma_{0<\rho<1}$ |  |  | 0.159 | 0.001 | 0.159 | 0.001 |
|  | $\gamma_{0<\rho<1}-\gamma_{1}$ |  |  | 0.069 | 0.194 | 0.069 | 0.193 |
| $\sigma_{0}^{r}$ | $\sigma_{0}^{r}-\sigma_{0<\rho<1}^{r}$ | -2.403 | 0.115 | -1.728 | 0.009 | -1.728 | 0.027 |
|  | $\sigma_{0<\rho<1}^{r}-\sigma_{1}^{r}$ | 0.086 | 0.966 | 0.445 | 0.603 | 0.445 | 0.618 |
| $\sigma_{0}^{t}$ | $\sigma_{0}^{t}-\sigma_{0<\rho<1}^{t}$ | -1.124 | 0.553 | -0.969 | 0.291 | -0.969 | 0.559 |
|  | $\sigma_{0<\rho<1}^{t}-\sigma_{1}^{t}$ | -1.201 | 0.316 | -0.970 | 0.495 | -0.969 | 0.346 |
| LL |  | -7388.823 |  | -7256.445 |  | -7256.445 |  |
|  |  | -7418.426 | 0.000 | -7286.503 | 0.000 | -7286.503 | 0.000 |

## Other specifications: linear effect of $\pi$ when $\pi>0$

| Parameter |  | DEU |  | HDRDU |  | HDRDU2 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| slope of $\pi$ | $\alpha$ | 0.070 | 0.317 | 0.030 | 0.601 | 0.030 | 0.745 |
|  | $\delta$ | 0.006 | 0.416 | 0.007 | 0.327 | 0.007 | 0.487 |
|  | $\beta$ |  |  | 0.028 | 0.342 | 0.042 | 0.360 |
|  | $\gamma$ |  |  | 0.077 | 0.248 | 0.078 | 0.549 |
|  | $\sigma^{r}$ | 0.053 | 0.968 | 0.449 | 0.766 | 0.448 | 0.963 |
|  | $\sigma^{t}$ | -1.794 | $\mathbf{0 . 0 4 4}$ | -1.458 | 0.400 | -1.458 | 0.886 |
| LL |  | -5583.121 |  | -5476.502 |  | -5476.50 |  |
|  |  |  | -5585.377 | 0.34 | -5479.01 | 0.54 | -5479.01 |

# Discussion 

## Main results

We report the first study investigating the impact of the selection probability $\pi$ on risk and time preferences

- for risk:
- a difference between $\pi=0$ and $\pi>0$
- no difference between treatments when $\pi>0$
- for time
- no impact of $\pi$


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Preliminary conclusion: real incentive matter but subjects isolate from $\pi$

## Additional findings

- Inverse $S$ probability weighting is
- more pronounced for $\pi>0$
- not due do absence of incentives
- Under DEU, controlling for the time utility using the risk utility may create distortions
- here it creates the spurious impression that incentives impact discounting
- another illustration that risk preferences are not time preferences (incentives impact the risk utility but not the time utility)


## Back to our set of hypothesis

|  | for risk | for time |
| :---: | :---: | :---: |
| compounding | more risk taking for $0<\pi<1$ than for $\pi=1$ | more patience for $0<\pi<1$ than for $\pi=1$ |
|  | dilution | more risk taking and more errors for $\pi<1$ than for $\pi=1$ |

## Preference for simplicity?

- The random incentive system creates complexity about
- how questions are selection
- how lotteries are played
- In order to avoid this complexity, subject may select the sure outcome more often which would produce
- more risk aversion
- more certainty effect, hence more inverse $S$ probability weighting

Thank you!

