

Medium-term public transit route ridership forecasting: What, how and why? A case study in Lyon

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1	Medium-term public transit route ridership forecasting:
2	what, how and why ?
3	A case study in Lyon
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Abstract

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Demand forecasting is an essential task in many industries and the transportation sector q is no exception. This is because accurate forecasts are a fundamental aspect of any rationale 10 11 planning process and an essential component of intelligent transportation systems. In the 12 context of public transit, forecasts are needed to support different level of planning and or-13 ganisational processes. Short-term forecast, typically a few hours in the future, are developed to support real-time operations. Long-term forecast, typically 5 years or more in the future, 14 are essential for strategic planning. Those two forecast horizons have been widely studied 15 by the academic community but surprisingly little research deal with forecast between those 16 two ranges. The objective of this paper is therefore twofold. First, we proposed a generic 17 modelling approach to forecast next 365 days ridership in a public transit network at differ-18 ent levels of spatiotemporal aggregation. Second, we illustrate how such models can assist 19 public transit operators and transit agencies in monitoring ridership and supporting recurrent 20 tactical planning tasks. The proposed formulation is based on a multiplicative decomposition 21 that combines tree-based models with trend forecasting. The evaluation of models on unseen 22 data proves that this approach generates coherent forecast. Different use cases are then de-23 picted. They demonstrate that the resulting forecast can support various recurrent tactical 24 tasks such as setting future goals, monitoring ridership or supporting the definition of service 25 provision. Overall, this study contributes to the growing literature on the use of automated 26 data collection. It confirms that more sophisticated statistical methods can help to improve 27 public transportation planning and enhance data-driven decision making. 28

Keywords: Public transit, Ridership forecasting, Machine Learning, Smart Card Data, Trans port planning

³¹ Highlights

- Examines the need for medium-term forecasting in public transit systems
- Proposes an operational modelling framework to forecast ridership one year ahead at different levels of spatiotemporal aggregation
- Outlines different applications of the forecasts for tactical planning and ridership monitoring
- Exploitation of archived passive data can enhance data-driven decision making

37 Author statement:

Oscar Egu: Conceptualization, Methodology, Formal analysis, Data Curation, Writing - Original
 Draft, Visualization, Investigation. Patrick Bonnel: Supervision, Validation, Writing - Review
 and Editing.

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30 1 Introduction

Demand forecasting is an essential task in many industries and the transportation sector is no 31 exception. In fact, accurate prediction of future demand is an essential components of intelligent 32 transportation systems [Vlahogianni et al., 2014, Koutsopoulos et al., 2019] and a fundamental 33 aspect of any rationale planning process [Bonnel, 2002, Ortúzar and Willumsen, 2011]. Thus, it is 34 not surprising that passenger demand forecasting is a widely studied subject. To summarize this 35 area of research, we must take into account the domain of application and the type of planning 36 issues the forecast intend to address. In many organisations including public transport, they 37 are three commonly accepted level of planning and organisational control [van de Velde, 1999, 38 Pelletier et al., 2011, Ortúzar and Willumsen, 2011]. Strategic level deal with long-term decisions 39 and objectives. Tactical level focus on decisions that take place in the medium-term and aims to 40 guarantee that the means to reach long-term goals are in place. Operational planning is concerned 41 with short-term decisions that ensure the efficiency of the production. In agreement with this 42 hierarchical order of decision-making activities, operators and transport agencies must generate 43 different forecasts. 44

Short-term forecasting is a very active field [Vlahogianni et al., 2014] that deal with models that 45 predict demand from few minutes to few hours into the future [Vlahogianni et al., 2014, Noursalehi 46 et al., 2018]. The wide adoptions of smart card fare collection systems has provided new opportun-47 ities for short-term forecasting. Zhai et al. [2018] have discussed the literature about short-term bus 48 passenger flow forecasting models and methods. Ma et al. [2014] proposes an Interactive Multiple 49 Model-based Pattern Hybrid approach and evaluate it using empirical smart card data collected 50 along one bus route over one year in Jinan, China. Ding et al. [2016] forecast short term subway 51 ridership using gradient boosting decision trees. Using Beijing smart card data, Li et al. [2017] 52 proposes a novel multiscale radial basis function to forecast the irregular fluctuation of subway pas-53 senger flows under special events. Using smart card data from London Underground, Noursalehi 54 et al. [2018] proposed to predict short term passenger arrivals at transit stations using state-space 55 models and considering station interactions. In the context of public transit (PT), authors argue 56 that short-term forecasting can enable the design of better control strategies and improve passen-57 ger experience by proactively adjust services and customer information [Koutsopoulos et al., 2019, 58 Noursalehi et al., 2018, Ma et al., 2014, Wei and Chen, 2012]. While appealing and surely helpful, 59 short-term forecasting can be hard to implement in real-life settings because it requires real-time 60 data, continuous actualization of the model and trust in the model output. Short-term forecasts 61 are also developed to support near real-time operational decision making. However, PT systems 62 cannot always react efficiently in real-time due to limited flexibility in resources (e.g vehicles, staff) 63 and infrastructure constraints. Transport services and infrastructures are thus often designed and 64 planned years in advance. 65

Long-term ridership forecasting deals with models that predict demand for time horizon ranging 66 67 from 5 to 15 years ahead. In contrast to short-term forecasting, it is often a one-time exercise and forecasts are rarely generated continuously. Forecasts are produced to assess and evaluate future 68 scenarios and support long-range strategical planning. The most common method for long-term 69 ridership forecasting traditionally relies on four-step travel demand model [Boyle, 2006, Ortúzar 70 and Willumsen, 2011, Bonnel, 2002]. Those models are data-intensive as they incorporate many 71 elements such as land use, future population, choice model, network description etc. On one 72 hand, it is a strength as this type of model can be used to forecast structural changes such as the 73 introduction of a new route but also to evaluate different policy choice [Ortúzar and Willumsen, 74 2011, Bonnel, 2002]. On the other hand, it is a weakness because the resulting model can be costly, 75 complex and hard to modify. Consequently, other forecasting approaches have been developed. For 76 example, change in ridership in response to change in services or fares can be forecast using elasticity 77

⁷⁸ coefficient [Boyle, 2006, Totten and Levinson, 2016, Paulley et al., 2006]. Other approaches include,
⁷⁹ spatial regression method [Pulugurtha and Agurla, 2012], rules of thumb method based on similar
⁸⁰ routes or professional judgement [Boyle, 2006, Diab et al., 2019]. In practice, those models and
⁸¹ approaches are often calibrated for a limited set of situation such as an average weekday, a typical
⁸² peak hour etc. They are, therefore, difficult to use in recurrent monitoring of the demand and
⁸³ cannot support tactical and operational planning activities.

Surprisingly, little research deal with forecast between those two horizons i.e medium-term 84 forecasting. However, those kinds of forecasts are part of the toolbox needed for the effective 85 planning of public transit systems. They can be of great use for PT operators and agencies 86 that want not only to be able to adapt real-time operation (short-term forecasting) and evaluate 87 strategic plan (long-term forecasting) but also to monitor tactically and continuously the evolution 88 of demand. Toqué et al. [2017] have recently proposed to use machine learning models to predict 89 PT ridership one year ahead in a disaggregate and continuous manner. However, the authors 90 didn't introduce in their analysis a multiyear trend component neither a description of the level of 91 supply although they may surely be needed for medium-term forecasting. Moreover, they barely 92 discuss the practical aspect of the forecasting framework and motivate their work with use cases. 93 This paper seeks to address these research gaps and has two complementary objectives: 94

 To develop a generic forecasting approach that combined passenger flow trend analysis with machine learning model to predict one year in advance, at different levels of spatiotemporal aggregation, ridership volume in a PT network. The model should consider seasonal effects, holiday period, bank holiday, day of the week, hours of the day and unusual effect to forecast not only an average ridership one year in advance, but the variability of ridership across days, hours and network elements.

To illustrate how such forecasts can support tactical planning tasks and assist PT operators
 and agencies in monitoring ridership. The illustrations are based on real use cases from Lyon
 public transit network.

To this end, the paper has been organized in the following way. It begins with a presentation of the 104 modelling approach. After that, relevant data are identified, prepared and described. Then, the 105 forecasts are validated using unseen data and a bottom-up approach. Finally, use cases are provided 106 to illustrate the value of such data-driven framework. Results show that the proposed modelling 107 approach is valid. Transit agencies can leverage the resulting forecast to better monitor and 108 anticipate ridership in their network. Overall, this study contributes to the growing literature on 109 the use of automated data collection to improve public transportation planning. Findings confirm 110 that more sophisticated statistical methods can facilitate analysis that used to rely primarily on 111 professional judgement [Hanft et al., 2016, Pelletier et al., 2011, Koutsopoulos et al., 2019]. 112

¹¹³ 2 Modelling framework

Let's denote $Y_i = (y_{i,1}, ..., y_{i,t}, ..., y_{i,n})$ as the vector of observed ridership volume on element i of 114 a PT network for each time step $t \in 1, ..., n$. Let's denote $X_{i,t}$ the set of features (explanatory 115 variables) whose values are known for $t \in 1, ..., m$ where m (m > n) is the prediction horizon. 116 Our goal is to estimate a regression model $f_i(.)$ for each element i such that $y_{i,t} = f_i(X_{i,t}) + \varepsilon$ 117 where ε is the difference between the observed value and the predicted value $\widehat{y_{i,t}} = f_i(X_{i,t})$. 118 This formulation described a typical univariate regression problem where (1) each element of the 119 network i is considered independent of the rest of the network, (2) each observation $y_{i,t}$ is considered 120 independent of the other's observations. 121

As proposed by Toqué et al. [2017], to estimate $f_i(.)$ we can use machine learning models such 122 as ensemble of decision trees. Those models have recently gained much popularities in various 123 fields due to their ability to learn complex non-linear relation between features and provide higher 124 accuracy than single machine learning models [Friedman et al., 2001, Opitz and Maclin, 1999]. 125 126 Those models combine several decision trees into one single model that output the mean of all decision tree. A single decision tree can be seen as a stratification of the ridership volume into 127 some simple regions using a set of splitting rules based on the available features. The underlying 128 principle of those models is that by combining single decision trees we can significantly improve the 129 predictive performance and reduce the variance of a single tree [Friedman et al., 2001, Breiman, 130 2001, Friedman, 2001]. 131

To learn a set of decision trees effectively the two most common algorithms are random forest 132 (RF) and gradient boosting (GB). Random forest was introduced by Breiman [2001] and is based 133 on the concept of bagging. More precisely, each decision tree is built independently on a random 134 subset of the training data but also considering only a random sample of features at each split. In 135 doing so, the algorithm enforces diversity in the trees which when we average them may reduce the 136 variance of the model [Breiman, 2001]. Gradient boosting trees were formalized by Friedman [2001] 137 and differ from the random forest model in the sense that decision trees are built sequentially using 138 strategically resample training data. More specifically, each new tree is built to recover the errors 139 resulting from the model obtained with the ensemble of trees produced at the previous steps. In 140 this approach, each of the decision trees can remain rather small with performance slightly above 141 random guess. Fitting them sequentially can then help to improve the model in areas of the feature 142 space that were missed by previous ensemble [Friedman et al., 2001]. 143

One aspect of those machine learning models is that they assume independence between the $y_{i,t}$ 144 and thus can't learn time-dependent structure and forecast potential trend. In fact, as explained 145 above the model output are computed by averaging decision trees which are themselves based on 146 historical ridership data. However, ridership volume may have statistical properties that evolve 147 through time and might also be view as a non-stationary time series. To deal with this aspect, 148 we can assume that ridership volume has two components a yearly trend-cycle component $s_{i,T}$ 149 and a yearly adjusted component $a_{i,t}$. Ridership level can then be expressed using multiplicative 150 decomposition: 151

$$y_{i,t} = s_{i,T} \times a_{i,t} \tag{1}$$

were $s_{i,T}$ denotes the mean of $y_{i,t}$ in year $T, t \in T$ and $a_{i,t}$ is the yearly adjusted level ridership of element *i* at time step *t*.

The forecasting task can then be divided into two subtasks were we have to forecast $s_{i,T}$ and $a_{i,t}$. The rationale behind this process is twofold. First, $a_{i,t}$ is assumed to be stationary and free of trend and thus can be estimated with ensemble of decision trees $(\widehat{a_{i,t}} = f_i(X_{i,t}))$. Second, $s_{i,T}$ is supposed to be non-stationary and evolve slowly over time and can be forecast by taking the last value of the yearly trend-cycle component multiply by a growth factor α_i . $\widehat{y_{i,t}}$ can then be obtained in the following way:

$$\widehat{y_{i,t}} = \widehat{a_{i,t}} \times (1 + \alpha_i) s_{i,T-1} \tag{2}$$

In other words, the forecasted ridership for element *i* is equal to the mean ridership of the previous year $s_{i,T-1}$ multiply by a growth factor while the deviation from the mean yearly ridership volume $a_{i,t}$ is predicted using a regression model. α_i can then be estimated using a weighting average of the observed historical year-mean percentage evolution:

$$\alpha_i = \frac{\sum_{T=2}^N w_T \frac{s_{i,T}}{s_{i,T-1}}}{\sum_{T=2}^N w_T}$$
(3)

where N is the number of years used to train the model and $w_T = 1/(N + 1 - T)$ is the weight associated with year T defined with inverse time decay function. This weighted formulation is proposed to estimate α_i from multiyear behaviour of each element while giving higher weight to more recent years.

168 This forecasting formulation is well suited to our objectives for two reasons. First, it exploits the property of ensemble models to learn the influence of various features on detrended ridership 169 data. Second, it aligned forecast with previous year observed ridership volume of element i to 170 ensure coherency of the forecast with the most recent element state. This formulation can be seen 171 as a conservative continuation of previous year's ridership mean volume combined with a model 172 that learns historical behaviour of the network element under different conditions of the features 173 space. As noted by Hyndman and Athanasopoulos [2018], traditional time series models (such 174 as seasonal ARIMA) don't allow irregular events and have difficulty to accommodate multiple 175 imbricated seasonality. The intuition behind the above formulation is that the decision tree model 176 is able to capture those effects while remaining robust to potential outliers. 177

At this step, we have now a modelling approach that can be used to forecast the future ridership volume at time step t of each element i denoted as base forecast. To establish forecast for higher levels of the network hierarchy such as a group of elements J (e.g group of stops, group of routes) or larger temporal aggregation (e.g day, week, month, working day), we can employ the simple and straightforward bottom-up approach. In this case, the forecasted ridership volume of higher hierarchies element J for the period M = [t1, ..., t2] denoted $\widehat{R}_{J,M}$ is obtained by summing the different base forecast:

$$\widehat{R_{J,M}} = \sum_{i \in J} \sum_{t=t1}^{t2} \widehat{y_{i,t}}$$
(4)

This approach is a classical way to deal with time-series collections that naturally presents hierarchical properties and different seasonal pattern [Hyndman and Athanasopoulos, 2018, Kahn, 197 1998]. It has the advantage to preserve in the forecasting task the dynamic and characteristics of individual elements while making it possible for the analyst to obtain forecast at the desired spatiotemporal level of the PT network.

¹⁹⁰ 3 Data preparation and exploration

Since the introduction of automated data collection systems, it is now possible to access high-191 resolution ridership data. Those new data sources have the potential to change the current state 192 of practice in ridership forecasting if they are accurate and of good quality Boyle, 2006, Diab 193 et al., 2019. To be used in medium-term forecasting those data need also to be correctly curated 194 and archived so there are enough observations to train models. The proposed modelling approach 195 requires the definition of a base forecast level. This level should not be too noisy to ensure models 196 can properly learn patterns and at the same time sufficiently detailed for most of the required 197 tactical analysis. This level should also be set from the perspective of the organisation managing 198 the network which can be different from the passenger perspective. We suggest that the most 199 appropriate spatiotemporal base level of aggregation for medium-term forecasting are: 200

- Temporal aggregation (t): hourly data because it is needed to account for intra-day variation and define supply level accordingly. However, it should be noted that the same methodology could be applied to daily data if this resolution level is deemed sufficient.
- Spatial aggregation (i): route level is most suitable than stop level because supply level is more than anything else link to route elements.

In Lyon, the current fare transaction system is an entry only system that was introduced in 206 2002. Passenger can validate using either smart card or magnetic paper. Validation is mandatory 207 when boarding a bus or tramway and when entering the subway network. All transactions are 208 then anonymized and stored with timestamp and localisation attributes. For this research, the 209 210 fare transactions from 2014 to 2018 for the subway network (4 metro lines and 2 funicular lines), the tramway network (5 lines) and high-frequency buses known as line C (25 lines) were extracted 211 from the Lyon PT operator data warehouse. A map of the extracted network is given in figure 1. 212 Those routes were selected because they represent more than 80% of the total ridership of the 213 network. This sample was also deemed to be enough to evaluate correctly our approach. Fare 214 transactions were then summed by route and by hour¹. To ensure, the completeness of the data, 215 the following procedure was implemented recursively for each route: 216

- Generate the hourly time bin from the 1st of January 2014 00:00 to the 31st December 2018 23:00.
- Lookup for the number of fare transactions summed by hour. If no transaction is found for a given hour it was assumed that no passenger board the route and the ridership value was set to zero. This procedure is put in place to ensure the consistency of the training data which must contain periods with and without ridership to correctly learn the route historical behaviour².

For the rest of this paper, the dataset resulting from the above procedure will be referred to as the route ridership volume and will form the base level of our modelling framework.

Our modelling framework also required a set of features that may explain the route ridership 226 volume variations while being available one year in advance. It is well recognized that PT ridership 227 presents multiple temporal seasonalities and regular cycles that can be encoded with ordinary 228 calendar attributes. Consequently, a calendar features table common for all routes was manually 229 crafted. Features of this spreadsheet are described in table 1. Ridership is also influenced by the 230 level of supply i.e the quantity of service produced. One of the most common and simple indicator 231 to describe this aspect of transit is the number of commercial kilometres offered. This indicator 232 was thus extracted from the operator data warehouse and choose as an explanatory variable. 233 Unfortunately, for this research, this feature was available with enough historical depth only at the 234 level of day and route. Noted also that in Lyon, commercial kilometres offered by routes are set 235 one year in advance by the operator planning team for contractual and financial reasons. Thus, 236 like calendar features, they can be determined sufficiently in advance and be used as predictors 237 in medium-term forecasting (which is not the case of potential other features such as weather or 238 unplanned events). 239

The calendar table, the supply feature and routes ridership volumes were then merged. To 240 explore the characteristics of the resulting dataset we have aggregated the ridership volume of 241 the 36 selected routes and perform exploratory visualizations in figure 2. In figure 2a, it can be 242 seen that there are cyclical patterns that repeat every year such as a strong decrease of ridership 243 volume during summer months (July and August). There are also long-term dynamics in the 244 ridership volume with an observable increasing tendency. This is because Lyon network has been 245 gaining popularities in the last few years. In figure 2c, the variation of daily ridership volume for 246 the year 2018 are observed more finely. This figure indicated that they are multiple imbricated 247 seasonalities and calendar effects. More precisely, it can be seen that school holiday periods (e.g 248 in February, April, October and December) but also other events such as bank holidays or special 249

 $^{^{1}}$ Noted that for the subway fare transactions are linked to stations and were thus redistributed by route according to operator reporting procedure.

 $^{^{2}}$ Note that in the case of potential data loss this procedure will also result in ridership equal to zero.



Figure 1: Map of the study network, source: prepared by the authors

Features	Description				
Hour	24 categories				
Month	12 categories				
Week number	Numeric from 1 to 53				
Day of the week	7 categories				
School holiday	7 categories, one for each holiday period				
Public holiday	14 categories, one for each French public holiday				
Adjacent to public holiday	Binaries if weekdays and adjacent to public holiday				
Light and music festivals	Binaries if major citywide events				

Table 1: Hand crafted calendar features, source: prepared by the authors

events have an impact on the ridership volume. Similarly, we observe a strong decrease in ridership

during weekends and summer months. As indicated by figure 2a, those seasonalities seems to be

²⁵² recurrent every year but calendar effects are moving in time because each year events and holidays

²⁵³ can fall in different days of the year. In figure 2b, the relation between the total daily number

of commercial kilometres produced and the ridership volume is depicted. This figure shows that there are three main states in the network that correspond to three typical planned service output

(weekday, Saturday and Sunday). Figure 2b also demonstrates that there are more variations 256 in the ridership volume than in the service produced. For instance, 85,000 kilometres produced 257 corresponds to a typical weekday supply level but for this same amount of supply, the ridership 258 volume can vary between 0.8 to 1.1 million. This is because the supply is often fixed based on a 259 260 set of typical days while the demand is more volatile. Finally, in figure 2d the hourly ridership from the 5th May 2018 to 19th May 2018 is given. This period exhibits distinct hourly patterns. 261 During the first week, there are two public holidays on the 8th of May and 10th of May and the 262 demand pattern on those day does not exhibit strong peak compare to the other weekday of the 263 week. During Saturday and Sunday, the hourly ridership curve has a bell shape. Finally, from the 264 14th of May to the 18th of May we observe a typical demand pattern with peak periods in the 265 morning and the evening but also higher hourly ridership volume than during the previous week. 266 Overall, the previous plots confirm that ridership volume presents multiple moving imbricated 267 seasonality and irregular events. Changes appear from one year to another, from one month to 268 another, during the hour of the day, the days of the week etc. There is also a relation between 269 the level of supply and demand. Those observations are not per se surprising but we should 270 recall that those are the elements that each base model needs to capture independently for each 271 route. In fact, while the previous plots were obtained based on the aggregation of all route, 272 the model will be trained for each route separately and we can expect that routes have distinct 273 behaviour. For example, the influence of holiday may be less important for some part of the 274 network, some routes may show higher multi-year growth than other, some routes may have specific 275 276 characteristics on weekends because they serve specific areas of the city such as touristic places. Hence, it is fundamental that the model can adapt correctly and in an automatic way to varying 277 route behaviours while capturing system-wide demand variation and structure. 278

Name	Model	Features	Decomposition
HM	Historical median	Hour, Type of day, Month, Working day	
HMT	Historical median	Hour, Type of day, Month, Working day	х
\mathbf{RF}	Random forest	Calendar features	
RFT	Random forest	Calendar features	х
RFTS	Random forest	Calendar features and supply feature	х
GB	Gradient boosting	Calendar features	
GBT	Gradient boosting	Calendar features	х
GBTS	Gradient boosting	Calendar features and supply feature	Х

²⁷⁹ 4 Models fitting and forecast errors

Table 2: List of implemented models, source: prepared by the authors

In the previous sections, we have defined the problem, proposed a modelling framework, gather 280 the data and perform some preliminary exploratory analysis, we now present models fit. Table 281 2, depicts the list of models that we have decided to evaluate. The first model formulation is a 282 naive historical approach. In this case, the forecast is computed using the median of all past time 283 step over the historical observation with the same characteristic as the forecasted time step. Time 284 step characteristics were in this case defined with the cartesian product between the hour, the 285 month, the type of day (weekday, Saturday, Sunday) and a boolean indicator for working day (no 286 public holiday, no school holiday, no special events). This formulation will serve as the baseline to 287 evaluate the two ensemble models described in section 2. Table 2 also indicates if the models were 288





trained with the raw ridership volume or with the decomposed ridership volume. In the second case, the equation 2 was used to forecast future ridership volume.

The accuracy of a forecast procedure can only be truly determined using data that were not used to fit the model [Hyndman and Athanasopoulos, 2018]. To do so, there are two common approaches: the cross-validation where several sets of tests are sequentially constructed and the hold-out approach where the data is divided into two portions. In this research, the hold-out approach was selected. The data was thus divided between a training set comprising all observations from 2014 to 2017 and a test set consisting of 2018 observations. To measure forecast errors the following standard metrics were chosen:

$$MAE = \frac{1}{n} \sum_{i=1}^{n} |y_{i,t} - \widehat{y_{i,t}}|$$
(5)

298

MAPEv =
$$\frac{1}{n} \sum_{i=1}^{n} \frac{|y_{i,t} - \widehat{y_{i,t}}|}{y_{i,t}}, \quad \forall \ y_{i,t} > v$$
 (6)

299

$$MdAPE = median(\frac{|y_{i,t} - \widehat{y_{i,t}}|}{y_{i,t}})$$
(7)

In table 3, we have reported the error measures on the train and test dataset for different levels of 300 aggregations. First, as expected, when the aggregation level increases, errors decrease significantly. 301 For instance, the best model at the base forecast has a MdAPE of 11.7 % almost four times bigger 302 than the best model MdAPE once forecasts are aggregated by day (2.8 %). This indicates that 303 the base levels are challenging to forecast but the bottom-up approach allows to generate coherent 304 results. In other words, base forecast errors tend to compensate when forecasts are aggregated by 305 route or by time. A second important observation is that ensemble models outperform baseline 306 model in terms of absolute errors (MAE) but also in terms of percentage errors (MAPEv and 307 MdAPE). Ensemble models consider a more complex feature space but still can generalize to 308 previously unseen data more comprehensively and without overfitting. However, there are no 309 important differences in terms of accuracy between the gradient boosting and the random forest 310 which is not surprising since both methods have strong similarities. What is also clear from this 311 table is that the decomposition approach is essential when historical data with a certain depth is 312 used to model future ridership. This is because the decomposition ensures the coherency of the 313 forecast with the most recent observed ridership volume. Finally, the introduction of supply feature 314 in ensemble models can reduce the errors especially large errors. If we compare the RFT (random 315 forest with decomposition) and RFTS (random forest with decomposition and supply feature), it 316 can be seen that median absolute percentage errors are quite similar but mean absolute percentage 317 error can be considerably higher when the supply feature is omitted. This is because, when there 318 is a significant reduction in the kilometres produced the model based on calendar features will 319 assume no change in the ridership volume. 320

³²¹ 5 Use case analysis

In the previous section, we have fitted different models and generate forecasts of ridership volume one year in advance. We have shown that it was possible to obtain rather low errors at higher aggregated levels but the forecast quality decreases at lower levels of aggregation. While forecast accuracy is in itself an important matter it is also important to recall that PT networks are complex systems that are impacted by all sort of unexpected and exogenous events. Therefore, the above models should not be seen solely for their prediction capability but also for their ability to assist PT

		TRAIN SET (2014-2017)							
		HM	HMT	\mathbf{RF}	RFT	RFTS	GB	GBT	GBTS
Base level (route-hour)	MAE	97	93	79	74	69	81	77	67
	MAPE_50 (%)	17,4	16,8	15,1	14,5	12,9	$16,\! 6$	16,1	$13,\!4$
	MdAPE (%)	10,5	10,0	10,3	9,6	9,0	10,7	10,1	9,1
Aggregated (route-day)	MAE	1795	1670	1236	1063	712	1230	1088	859
	MAPE $(\%)$	$25,\!6$	24,8	11,2	10,3	$5,\!5$	13,1	12,1	8,2
	MdAPE (%)	6,3	5,6	5,2	4,3	3,0	5,4	4,6	3,8
Aggregated (hour)	MAE	2682	2618	1913	1816	1741	2040	1987	1564
	MAPE $(\%)$	16,0	15,7	17,1	16,9	18,0	20,2	20,1	$14,\!8$
	MdAPE $(\%)$	6,4	6,0	5,5	5,0	5,0	6,4	6,2	4,9
Aggregated (day)	MAE	51725	49869	30793	26737	18264	31063	28508	21007
	MAPE $(\%)$	67,0	67,1	14,7	14,1	6,3	18,5	18,4	11,5
	MdAPE $(\%)$	4,4	4,0	3,1	2,4	$1,\!8$	3,3	2,8	2,2
		TEST SET (2018)							
		HM	HMT	\mathbf{RF}	RFT	RFTS	GB	GBT	GBTS
Base level (route-hour)	MAE	131	115	118	99	95	123	104	93
	MAPE_50 (%)	21,7	21,7	19,9	19,8	17,2	21,1	21,4	17,4
	MdAPE (%)	14,5	12,8	13,7	11,9	11,7	14,4	$12,\! 6$	11,7
Aggregated (route-day)	MAE	2662	2157	2339	1708	1480	2351	1720	1497
	MAPE $(\%)$	$_{36,3}$	36,9	26,8	26,7	$16,\! 6$	28,1	27,8	17,7
	MdAPE (%)	10,7	7,7	9,9	6,8	6,4	10,0	6,9	6,5
Aggregated (hour)	MAE	3562	2878	2993	2140	2182	3226	2349	1976
	MAPE $(\%)$	25,7	24,9	19,7	19,1	16,7	$25,\!4$	25,1	16,4
	MdAPE (%)	10,0	7,1	8,4	5,7	5,9	9,7	6,8	5,8
Aggregated (day)	MAE	75721	54068	63457	33658	31259	63643	35738	30671
	MAPE $(\%)$	55,2	55,7	28,9	26,7	9,0	32,9	31,0	$13,\!8$
	MdAPE $(\%)$	8,1	4,4	7,2	2,8	3,1	7,8	3,5	3,1

Table 3: Model results on the train and test dataset for different level of aggregation (HM: historical median, RF: random forest, GB: gradient boosting, T indicates the use of the proposed decomposition approach, S indicates the incorporation of supply feature), source: prepared by the authors

organisations in monitoring ridership and in improving tactical decision-making activities. This is what we intend to demonstrate in this section by introducing a few use cases.

With the above modelling approach, it is possible to obtain coherent aggregated ridership 330 forecasts. These types of forecasts could be used for tactical decision making. For instance, they 331 can assist senior executives in setting next year goals and monitoring their PT network with a more 332 data-driven approach. Similarly, every year, transit agencies need to prepared next year budget 333 which obviously requires at one point some sort of ridership forecast. In practice, this process can 334 be tedious and is often a matter of expert. In the case where different operators coexist in the same 335 network, this task is even more complex and critical for the proper functioning and financing of 336 the system. Agencies could use the proposed approach to generate forecasts for all route and then 337 aggregated them to prepare budgets that match more closely the future variation of ridership and 338 fit the financial/operational division of the network³. To illustrate this first use case, the weekly 339 forecast for the two random forest models obtained through decomposition (RFT and RFTS) by 340 type of transportation mode is plotted in figure 3. 341

In figure 3, it can be seen that the different series are overall quite close and the aggregation of

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 $^{^{3}}$ Those same forecasts could also be used to schedule workforces such as field information officers or fare officers



Figure 3: Weekly forecast one year in advance for the three transportation mode (RFT: decomposed random forest, RFTS: decompose random forest with supply features, Y: real ridership volume), source: prepared by the authors

models captures typical calendar patterns such as the impact of school holidays, public holidays, 343 or citywide events (i.e peak at week 50 for subway network). It can also be seen that the ridership 344 volume of high-frequency bus network has increased more quickly than anticipated by the two 345 models, especially after September. Finally, figure 3 indicates that for the tramway routes both 346 model yield different forecast. This is because in 2018 the tramway network was impacted by 347 important construction work of a new tramway route (T6) that leads to change in the service 348 provision. Those type of elements can be further inspected by an analyst using models outputs in 349 a retrospective manner. Especially, models can be used to identify routes whose behaviour deviate 350 from historical behaviour as captured by the models. In doing so, analysts could identify and 351 prioritize which route they need to review first in a more efficient manner than doing it based on 352 "anecdotal knowledge" or fixed cycle [Coleman et al., 2018]. In figure 4, we have plotted each route 353 as a point in a two-dimension space where the x-axis is the annual percentage error between the 354 RFTS model and the real 2018 ridership and the y-axis is the total real ridership volume. Using 355 figure 4 it is easy to identify routes that require further analysis, balancing the importance of the 356 route (y-axis) and the importance of the deviation from the model (x-axis). Figure 4 indicates 357 that most routes errors are under 5% but some route exhibit higher discrepancies between model 358 and real observations such as C3, C14, C15, C9 or T5. This route level analysis can be further 359 extended to go deeper into the available data. For instance, real and model route ridership volume 360 were aggregated by month and inspected in figure 5. 361

In figure 5, we can observe that there is indeed a large diversity of route ridership historical 362 pattern. For instance, route C3 is the busiest bus route in Lyon and important road work were 363 carry on between mid-2016 to mid-2019 to provide exclusive right-of-way. The route was divided 364 into two sections and part of the stops were relocated. As indicated by figure 5, it had a great 365 impact on the 2017 ridership volume and the model forecast further decreased of the demand 366 in 2018. However, by the end of 2018, as the route progressively returns to better operational 367 condition, the ridership starts to increase significantly in an unforeseen manner for the model. 368 In 2016, a strong decrease of ridership is observed on route $C14^4$ follow by a return at historical 369 ridership volume during 2017. These disruptions were not well assimilated by the models, and 370

 $^{^4\}mathrm{Route}$ C14 share a portion of C3 layout and was also impacted by road work



Anual percentage difference between RFTS model and real data (%)

Figure 4: Annual ridership volume forecast error for decomposed random forest with supply feature model (RFTS), source: prepared by the authors

further growth of the route was forecast. As mentioned earlier, in 2018 the tramway network 371 was impacted by the construction of a new tramway line (T6). In figure 4, it can be seen that 372 while tramway routes T1 and T3 are forecast correctly the model underestimates/overestimates the 373 traffic on routes T2/T4. Figure 5 indicates that those routes exhibit a strong decrease in summer 374 month (July/August). Models with supply feature partially anticipate this decrease (see figure 5 375 and figure 3) but models with only calendar features couldn't predict those changes (see figure 3). 376 The impacts of those kinds of exogenous elements are in practice very difficult to understand and 377 measure clearly without confronting the real ridership with a "business as usual" scenario. With 378 the above modelling approach, transit agencies can now more easily do so. They can monitor 379 route ridership with a data-driven approach using a predictive model that is easy to re-actualize 380 but also to implement. Moreover, they can use these "business as usual" forecast to estimate in 381 advance the number of trips impacted by a planned disruption. Once the period of disruption 382 and the routes impacted are known, an analyst can interrogate models to retrieve the forecasted 383 number of impacted trips. This information can then be used in the design of replacement services 384 or mitigation plan. In a similar vein, if different periods of disruption are being considered, models 385 could also be used to identify the period that minimizes the impacted volume of trips. For this 386 kind of use case, one may prefer to leverage on model using calendar features so the forecast is a 387 pure "business as usual" prediction. 388

The above use cases were based on spatial and/or temporal aggregation of model outputs but the base model i.e by route and hour can also be of value to apprehend in-depth ridership pattern. To this aim, forecasts need to be synthesized in such a way that the information can directly be helpful for tactical planning purposes. One way to do so would be to cluster the model output to identify a set of typical daily ridership profiles. Spherical kmean is a popular text mining prototype-based clustering algorithm [Buchta et al., 2012]. It relies on the cosine distance to measure dissimilarity between objects which has interesting properties for our problem as the observations are cluster



Figure 5: Monthly time series of ridership volume by route (RFTS train: training of decomposed random forest with supply feature (2014-2017), RFTS test: testing of decomposed random forest with supply feature (2018), Y: real monthly ridership by route), source: prepared by the authors

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³⁹⁶ irrespectively of their magnitude i.e the ridership volume. It can be mathematically express as a ³⁹⁷ minimization of the cosine distance of all possible allocation of objects m to clusters $c(m) \in 1, ..., k$ ³⁹⁸ and over all prototypes $p_1, ..., p_k$ in the same feature space as object m denoted x_m :

$$\min \quad \sum_{m} 1 - \frac{x_m \cdot p_{c(m)}}{\|x_m\| \cdot \|p_{c(m)}\|} \tag{8}$$

In our problem, the observation x_m is the vector of hourly forecasted route ridership volume 399 on a given day. The features space dimension is 24 and the number of observations is equal to 400 the number of days ahead we forecast multiply by the number of routes⁵. In prototype-based 401 clustering, the number of clusters k need to be defined first. Then, a fixed-point algorithm can 402 iterate between optimal allocation of observations to cluster and optimal prototypes to attempt 403 to determine a partition that minimizes equation 8. For the sake of illustration, we have decided 404 to retain 8 clusters accounting for almost 80% of the dissimilarity. The fixed-point algorithm was 405 then run 20 times and the best solution was retained. The resulting clusters prototypes are given 406 in figure 6a and were named according to their shape: bell shape clusters (BP) from 1 to 4 are daily 407 ridership profiles that don't exhibit two peak periods while peak profiles clusters (PP) numbered 408 from 1 to 4 are daily ridership profiles that exhibit a morning and evening peak pattern. 409



(a) Clustering prototype derived from RFTS model (random forest decomposed with supply)

(b) Calendar of forecasted daily prototype for three selected routes: bus route C8, subway route MA and tramway route T3)

Figure 6: Clustering analysis of model forecast, source: prepared by the authors

Those 8 clusters synthesize the high-resolution data contained in the base model. They facilitate 410 the analysis and provide more manageable information to transportation planners and analysts. 411 They can be used to further explore the future demand of each route. A typical use case would 412 be to produce in addition to the previous analysis on the ridership volume a calendar of future 413 daily ridership profile. The output of this procedure is given in figure 6b for three selected routes 414 (bus route C8, subway route MA and tramway route T3). In this figure, it can be seen that the 415 models have learned differents daily ridership profiles for each route. For instance, bus route C8 is 416 characterized by a change from prototype PP3 to prototype PP4 during holiday weekdays. It means 417 that the model forecast that during school holidays the peak period will be less important with 418 regard to the daily volume. Moreover, the model has learned that a typical Saturday will exhibit 419 a BP3 profile while Sunday will exhibit a higher concentration of trip in the morning (prototype 420 BP2). Subway route A daily profiles are overall more stable. Unlike route C8, Saturday and Sunday 421

 $^{{}^{5}}$ For 2018, N= 13140 = 36x365

prototype are equal. During weekday the assigned prototype remains the same (PP1) except during 422 the month of august (PP4). Finally, the tramway route T3 is characterized by weekday with a high 423 concentration of trip during morning peaks periods (prototype PP2). Compared to the subway 424 route the weekend prototype is BP3 meaning that in proportion less ridership is forecasted in the 425 426 late evening. These observations demonstrate that the models have learned and forecast distinct daily ridership profiles. Once cluster those forecasts can be examined more easily and help analysts 427 to adjust service plans to intra-day demand variation. Altogether, this use case section offers 428 some insights into how the proposed modelling framework could be used in real-world applications 429 and answer common tactical issues. One of the main advantages of the proposed solution is the 430 flexibility to explore forecasts at different levels of aggregation. 431

432 6 Conclusions

This research was undertaken with two objectives. First, to design a modelling framework suitable 433 for medium-term forecasting of route ridership volume. Second to evaluate the potential benefit 434 of such forecasts for transit agencies and operators. The proposed model can identify trends in 435 ridership over the past years in order to consider them for forecasting. It is also able to consider 436 variability within each year due to seasonal effects, holiday, bank holiday, weekday effects and hour 437 of the day. Finally, the proposed model can consider measures of supply evolution over time for 438 each PT route. The evaluation of different models has shown that the proposed decomposition for-439 mulation can learn complex patterns from historical data that can then be satisfactorily projected 440 into the future. The resulting forecasts have proven to be quite appropriate to facilitate recurrent 441 tactical decision making and help planning better services. The use case section outlined different 442 applications to demonstrate the potential of such a modelling approach for tactical planning to 443 support PT operator or authority needs. Examples of applications include setting future goals, 444 monitoring ridership volume at different levels of aggregations, estimating the impact of future 445 disruptions and supporting the definition of future service provision. It is therefore recommended 446 that transit agencies complement their traditional reporting tools with these types of predictive 447 approaches. By doing so, they can value at their full potential their historical data and enhance 448 data-driven decision making. Moreover, the cost of implementation of such a tool is reduced and 449 not too challenging. Models should simply be trained automatically by batch (e.g. every month) 450 based on the above data preparation procedure. Then the provision of modern dashboarding 451 tools with drill-down capability will make the data available through a web application for anyone 452 interested in the organisation. 453

Although the study has demonstrated that the proposed modelling formulation generate co-454 herent forecasts and is operational, it also has several limitations that need to be considered and 455 further investigated. First, the ensemble models are trained using the same weight for all historical 456 observations. Even though this approach is simple and generic it would be interesting to elabor-457 ate methods to identify non-representative historical data that should not be part of the training 458 set. We should also investigate mechanisms that put more weight on recent observations such as 459 what is proposed for the estimation of trend component. Second, while we did incorporate one 460 supply feature in the analysis, more research is required to establish additional evidence on which 461 variables are needed and how they should be treated in the modelling process. In this regard, one 462 direction would be to incorporate previously calculated elasticities factors in the model. Third, for 463 this research, we assumed that higher hierarchies forecast can be obtained simply by summing the 464 base forecast but other approaches need to be considered such as optimal forecast reconciliation 465 or middle-out approach. 466

467 Highlights

- Examines the need for medium-term forecasting in public transit systems
- Proposes an operational modelling framework to forecast ridership one year ahead at different
 levels of spatiotemporal aggregation
- Outlines different applications of the forecasts for tactical planning and ridership monitoring
- Exploitation of archived passive data can enhance data-driven decision making

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