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► **To cite this version:**

Frédérique Bec, Raouf Boucekkine, Caroline Jardet. Why Are Inflation Forecasts Sticky? Theory and Application to France and Germany. 2017. halshs-01630571

HAL Id: halshs-01630571

<https://shs.hal.science/halshs-01630571>

Preprint submitted on 7 Nov 2017

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Why Are Inflation Forecasts Sticky? Theory and Application to France and Germany

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WP 2017 - Nr 44

Why are inflation forecasts sticky?

Theory and application to France and Germany*

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November 7, 2017

Abstract

This paper proposes a theoretical model of forecasts formation which implies that in presence of information observation and forecasts communication costs, rational professional forecasters might find it optimal not to revise their forecasts continuously, or at any time. The threshold time- and state-dependence of the observation reviews and forecasts revisions implied by this model are then tested using inflation forecast updates of professional forecasters from recent Consensus Economics panel data for France and Germany. Our empirical results support the presence of both kinds of dependence, as well as their threshold-type shape. They also imply an upper bound of the optimal time between two information observations of about six months and the co-existence of both types of costs, the observation cost being about 1.5 times larger than the communication cost.

Keywords: Forecast revision, binary choice models, information and communication costs.

JEL classification: C23, D8, E31.

*This work has benefited from many fruitful remarks by Anurag Banerjee, Mélika Ben Salem, Guillaume Chevillon, Annabelle De Gaye, Neil Ericsson, Hervé Le Bihan, David Hendry, Francesco Lippi, Sarah Mouabbi, Muriel Roger, Pierre Sicsic and Mark Watson, as well as by participants at the CIRET 2016 conference in Copenhagen, the 8th French Econometrics Conference, the 25th Symposium of SNDE in Cergy-Pontoise, the Durham University Economics Department's seminar, the 19th OxMetrics Conference in Paris and the Banque De France seminar. F. Bec acknowledges support by Labex MME-DII. The authors thank Isabelle Capelle and Céline Garnier for helpful research assistance. Of course, all remaining errors are ours. This paper reflects our opinion and does not necessarily express the views of the Banque de France.

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1 Introduction

Carroll [2003] has shown that the opinion of professional forecasters spreads to firms and households, and hence also influences their expectations and decisions. It is also now well known that central banks across the world monitor surveys of professional forecasters very closely. In fact, in recent years, they have tried to influence agents expectations through policies such as forward guidance for instance. Thus, understanding how these expectations are formed is crucial.

Recent empirical evidence from forecast surveys data reveals “forecasts stickiness”. As found from various forecast surveys by e.g. Coibion and Gorodnichenko [2012], Andrade and Le Bihan [2013], Doern [2013], Coibion and Gorodnichenko [2015], Doern, Fritsche, Loun-gani and Tamirisa [2015], forecasters fail to systematically update their forecasts and/or their information set. As will be discussed later in the paper, this is also a feature of our German and French panel data of professional forecasters from Consensus Economics database. It reveals that an average of 43% only revise their monthly forecast of yearly inflation rate for target years between 2000 and 2015.

These findings are inconsistent with the full information rational expectation hypothesis in a frictionless setup. Nevertheless, sticky information *à la* Mankiw and Reis [2002] or noisy information *à la* Woodford [2002] and Sims [2003] have been put forward in the recent literature as possible explanations of this forecast stickiness. In the noisy information model, agents continuously update their information set but have an imperfect access to it at each period. In the information stickiness model, information about macroeconomic conditions diffuses slowly through the agents because of either cost of acquiring information or costs to re-optimization. Therefore, it takes time for the population to reach full information and decisions are not always made from current information. Consequently, Mankiw and Reis [2002] assume that at each period, only a fraction of the agents update their information set on the current state of the economy while the rest of them continues to make decisions based on outdated information.

Yet, sticky and noisy information models have testable implications in terms of forecasts series properties. Coibion and Gorodnichenko [2012], using various forecast surveys of consumers, firms, central bankers, and professional forecasters, provide evidence of information rigidities and point to the noisy information model as the most compatible with their survey data. From a panel of forecasts for real GDP growth rate of individual institutions from 36 countries from 1989 to 2010, Doornik et al. [2015] find that individual forecasts are updated rather frequently but there is some degree of information rigidities in the average forecast revision, which suggests that imperfect information among the forecasters stems from noisy information model. Coibion and Gorodnichenko [2015] also point to a high degree of information rigidity. In the sticky information framework, their empirical findings correspond to an average duration of six to seven months between information updates, while in the noisy information setup, they imply that new information receives less than half of the weight it would have under full-information relative to prior beliefs. Finally, using ECB Survey of Professional Forecasters which is a quarterly panel of 90 forecasting units in the Euro area, Andrade and Le Bihan [2013] find predictable and biased forecast errors as well as disagreement among forecasters when they update their forecasts, which suggests that both sticky and noisy information assumptions may be good candidates to describe expectation formation. However, based on an estimated expectations model combining both sticky and noisy information, they show that there is more stickiness in experts forecasts than their model is able to generate.

It is worth noticing that neither noisy nor sticky information models acknowledges any state dependence in the expectations formation process. In these frameworks, state changes impact the forecast errors but not the forecast update frequency. The latter is continuous by assumption in the noisy information model and fixed by a constant exogenous parameter in the sticky information model. Yet, it seems reasonable to provide for the possibility that large state changes increase the forecast update probability since they are likely to produce large forecast errors. This is consistent with state-dependence in the information updating

process as introduced in Bonomo and Carvalho [2004], Gorodnichenko [2008], Woodford [2009] or Alvarez, Lippi and Paciello [2011]’s models. In these contributions, observation imperfections are associated to menu costs so as to study price-setting decisions: either lumped together as in Bonomo and Carvalho [2004] or Woodford [2009] or separately as in Alvarez et al. [2011]. In a subsequent paper, Alvarez, Lippi and Paciello [2015] show from a general equilibrium model calibrated on US data that both costs, modelled separately, are required to predict real effects of monetary shocks that are more persistent than in the corresponding menu-cost model, but smaller than in the observation-cost model. As summarized by these authors, the case of observation cost only, yields “time-dependent” rules while the case of menu cost only, yields “state-dependent” price setting rules. The rationale underlying the state dependence basically stems from the envelope theorem: as long as the cost of adjustment is greater than the cost of non-adjustment, the price remains unchanged. Yet, in the neighborhood of the optimum, where the value function slope is very flat, the loss stemming from not adjusting is very small — it can be shown to be of a second order magnitude compared to the change in the state variable. This in turn explains stickiness even in presence of very small menu costs¹, unless the change in the state variable is large enough.

In fact, empirical evidence of state dependence in the expectations formation process has been found by Doern [2013] and Coibion and Gorodnichenko [2015]: According to their results, the degree of information rigidity declines significantly during recessions. Hence, agents appear to adjust the resources devoted to the collection and processing

¹A few papers have tried to evaluate these costs quantitatively. Amongst them, Levy, Bergen, Dutta and Venable [1997] evaluate the menu costs to amount to 0.7% of revenues or 35.2% of net margins for a large US supermarket chain : this computation includes the labor cost of changing shelf prices, the costs of printing and delivering new price tags, the costs of mistakes made during the price change process, and the cost of in-store supervision of the price change process. Using data from a large U.S. industrial manufacturer, managerial costs (information gathering, decision-making and internal communication costs included) are found to be six times as large as menu costs by Zbaracki, Ritson, Levy, Dutta and Bergen [2004]. More recently, Stella [2014] evaluates the total cost from changing price to lie in the range of 0.22% to 0.59% of revenues, and of 11.05% to 29.32% of net margins.

of information in response to economic conditions. In this paper, we claim that some kind of menu costs might be the missing ingredient to generate state-dependence and therefore explain the observed degree of forecast stickiness. To our knowledge, it hasn't been incorporated in existing forecast formation models so far. The goal of this paper is to fill this gap by developing a forecast formation model which yields both time- and state-dependent forecast updates. To this end, we introduce separate observation costs and “communication” costs in a model of inflation forecast formation.² The implications of our theoretical model will then be tested empirically from Consensus Economics country-specific professional forecasters panels for France and Germany. Professional forecasters survey data provide a conservative benchmark as these forecasters are amongst the most informed agents. Moreover, as stressed earlier, their opinion spreads to firms and households and is also very closely monitored by central banks as they play an important role in the conduct of monetary policy. As will be seen later, our empirical results support the presence of both time- and state-dependence, as well as their threshold-type shape implied by our model. They also imply an upper bound of the optimal time between two information observations of about six months, which corresponds to Coibion and Gorodnichenko [2015]'s finding from data of inflation forecasts from the US Survey of Professional Forecasters (SPF): their evaluation of the degree of information rigidity implies an average duration of six to seven months between information updates. Finally, we also report evidence of the co-existence of both types of costs, the observation cost being about 1.5 times larger than the communication cost. This latter result is in line with Zbaracki et al. [2004]'s finding that managerial costs, which compare to our observation costs when transposed to a large U.S. industrial manufacturer price setting problem, are much larger than menu costs, which are the analogues of our communication costs, again transposed to a firm price setting problem.

²Indeed, the rest of the paper will focus on inflation forecasts, as they have been widely studied so that the results are readily comparable to previous work. However, our model can easily be adapted to e.g. GDP growth rate forecasts.

The paper is organized as follows. Section 2 presents our proposed model of inflation forecast formation and its implications for the forecast updates dynamics. Section 3 describes the data and proposes a first analysis of unconditional probabilities of forecasts revisions. Section 4 presents the binary choice models used to explore empirically the time- and state-dependence of forecast updates as well as the estimation results. Section 5 concludes.

2 A Model of Forecast Formation

As noticed in the introduction, a promising recent branch of the literature on firms price setting behavior has associated observation imperfections to menu costs. In particular, Alvarez et al. [2011] combine separately observation and menu costs in the firms program, which results in both time- and state-dependent price setting rules. We shall develop an inflation forecast formation model which is formally close to their set-up. In particular, we show that a natural model of inflation forecast does incorporate the two types of cost mentioned just above, leading to an optimal control problem which may be solved with the tools developed by Alvarez et al. [2011].

Let us present our problem. Time is continuous and $t \in (0, 1)$. Suppose we are in a base period, say $t = 0$, where the forecast is equal to $\pi_f(0)$. From there on, we seek to forecast the inflation rate at date $t = 1$. The instantaneous quadratic loss function faced by a representative professional forecaster is:

$$\left(\pi_f(t) - \pi_f^*(t)\right)^2, \tag{1}$$

where $\pi_f(t)$ is the value at time t , with $0 < t \leq 1$, of his “official” forecast of inflation rate at $t = 1$. As long as a new forecast has not been publicly adjusted and communicated, $\pi_f(t)$ is constant, equal to $\pi_f(0)$. $\pi_f^*(t)$ is the optimal value of this forecast, i.e. the one which would prevail if the information set available at date t was up to date and without any adjustment friction or cost. We will refer to it as the target forecast. As usual, it

is assumed that the forecaster’s objective is to produce the best possible forecast, which amounts to minimize the distance between his forecast and the optimal forecast. The latter is a stochastic target forecast.

We assume that it is costly for the forecaster, or forecasting unit, to update his information set and hence to observe $\pi_f^*(t)$: each time he does so, it incurs a fixed cost $\theta > 0$. Indeed, on top of i.e. data bank subscription fees, it takes time, or hours worked, to collect and process all relevant information and include it in the corresponding relevant files. This cost also includes the hours worked to process formally the new pieces of information — like the potential update or re-estimation of the forecasting model and/or the time devoted to run it again with the updated information set. To sum up, it includes all costs related to the knowledge or observation of $\pi_f^*(t)$. In the following, this cost will be labelled “observation cost”.

Beside, it is also costly to adjust “officially” the forecast, i.e to adjust $\pi_f(t)$: at the very least, communication costs are involved. To capture this essential side of the story, we introduce just like Alvarez et al. [2011] a “menu cost”, $\psi > 0$, which can be labelled in our framework “adjustment” cost. In short, they do cover all the costs associated with the official release of the revised forecast, such as public communication, writing of reports, interview with the media, etc. This cost also includes the loss of the forecaster’s credibility from its institution’s customers which would follow too frequent forecast revisions.

We assume that at time $t = 0$, the forecaster pays the cost θ and observes $\pi_f^*(0)$. Then, until the next observation of the target forecast, $E(\pi_f^*(h)|\mathcal{I}_0) = \pi_f^*(0)$ where \mathcal{I}_0 is the information set observed at time $t = 0$. Indeed, with $\pi_f^*(0) = E(\pi(1)|\mathcal{I}_0)$, where $\pi(1)$ is the inflation rate at $t = 1$, we have:

$$E(\pi_f^*(h)|\mathcal{I}_0) = E(E(\pi(1)|\mathcal{I}_h)|\mathcal{I}_0) = E(\pi(1)|\mathcal{I}_0) = \pi_f^*(0) \quad (2)$$

Hence, the target forecast dynamics is given by:

$$\pi_f^*(h) = \pi_f^*(0) + s\sigma\sqrt{h},$$

where s is a standard normal and σ^2 is the variance per unit of time..

Let $\tilde{\pi}_f(t) \equiv \pi_f(t) - \pi_f^*(t)$, denote the gap between the current and the target forecasts. We define the “uncontrolled” forecast gap as the forecast gap $\tilde{\pi}_f(t)$ between two observations of $\pi_f^*(t)$ and before a new adjustment of $\pi_f(t)$. It follows that starting from $\tilde{\pi}_f(0)$ at time $t = 0$, the uncontrolled forecast gap evolves as:

$$\tilde{\pi}_f(h) = \tilde{\pi}_f(0) - s\sigma\sqrt{h}. \quad (3)$$

As will be shown below, at optimum there will be adjustments at finite time in accordance with the loss minimization objective, which will make the forecast gap process globally stationary.

In this setup, the problem of the forecaster is to choose the time elapsed until the next observation of the target forecast, $0 < T \leq 1$, which will cost θ , as well as the number of forecast adjustments between two observations (at $t = 0$ and T respectively), $J \in N$, occurring at successive dates $0 \leq t_1, t_2, \dots, t_J < T$, each one incurring an adjustment cost ψ . He also chooses the size of the forecast update so that the expected value of the forecast gap on adjustment is $\hat{\pi}_{f,j}$, with $j = 1, \dots, J$.

As it is stated, the problem is formally similar to the one treated by Alvarez et al. [2011]. There are two apparent differences:

1. The first difference comes from the fact that the timing of the next observation, that is the choice of T , is bounded by the forecast horizon, 1. There is no upper bound of this sort in Alvarez et al. [2011]. However, this is a pure control constraint, the simplest one from the mathematical point of view, and we show in our empirical section that it’s never binding in practice. Without loss of generality, we shall omit it hereafter to unburden the presentation.

2. The second is even more lenient. The law of motion assumed by Alvarez et al. [2011] for the target has a time drift ($\mu \geq 0$), which also shows up in the law of motion of the analogous stochastic gap.³ While nonzero drifts make sense in their framework (as they are concerned with price setting and the time drift corresponds indeed to inflation), they do not in ours. As a result, from this point of view, our problem corresponds to a special case in Alvarez et al. [2011], explicitly treated in their Section V, pp 1928-1934.

Henceforth, we shall use the same formalism and methodology as in Alvarez et al. [2011]. Let $V(\tilde{\pi}_f)$ denote the value function of the forecaster at the time of an observation of the forecast gap $\tilde{\pi}_f$, and $V_J(\tilde{\pi}_f)$ the best value that the forecaster can reach by making J forecast updates between observations. Then, note that:

$$V(\tilde{\pi}_f) = \min_{J \geq 0} V_J(\tilde{\pi}_f), \quad \text{so that} \quad J^*(\tilde{\pi}_f) = \arg \min_{J \geq 0} V_J(\tilde{\pi}_f), \quad (4)$$

where $J^*(\tilde{\pi}_f)$ is the optimal number of forecast updates. The corresponding Bellman equations can be written accordingly. To ease the exposition, suppose that $J \in \{0, 1\}$, that's at most one forecast update is optimal. This will turn out to be true for our forecast formation model. Let's denote $\tilde{\pi}_f = \tilde{\pi}_f(0)$ the value of the forecast gap at time $t = 0$

For $J = 0$, the conditional value function for the forecaster problem writes:

$$V_0(\tilde{\pi}_f) = \theta + \min_T \int_0^T e^{-\rho t} (\tilde{\pi}_f^2 + \sigma^2 t) dt + e^{-\rho T} \int_{-\infty}^{\infty} V(\tilde{\pi}_f - s\sigma\sqrt{T}) dN(s). \quad (5)$$

The first component of the right member of $V_0(\tilde{\pi}_f)$ is of course the information observation cost, while the second one is the time $t = 0$ expected loss between $t = 0$ and T . In the third (continuation) component, $N(\cdot)$ is the probability density function of a Gaussian distribution.

For $J = 1$ it becomes (with the simplified notation $\hat{\pi}_f = \hat{\pi}_{f,1}$ the adjusted forecast at time t_1):

³See equation (1) in Alvarez et al. [2011], page 1917.

$$\begin{aligned}
V_1(\tilde{\pi}_f) &= \theta + \min_{T, \tilde{\pi}_f, t_1} \int_0^{t_1} e^{-\rho t} \tilde{\pi}_f^2 dt + \int_0^T e^{-\rho t} \sigma^2 t dt + e^{-\rho t_1} \left[\psi + \int_0^{T-t_1} e^{-\rho t} \tilde{\pi}_f^2 dt \right] \\
&\quad + e^{-\rho T} \int_{-\infty}^{\infty} V(\hat{\pi}_f - s\sigma\sqrt{T}) dN(s).
\end{aligned} \tag{6}$$

The unconditional value function is hence given by:

$$V(\tilde{\pi}_f) = \min\{V_0(\tilde{\pi}_f), V_1(\tilde{\pi}_f)\}. \tag{7}$$

Because of the quadratic functions involved, it is possible to provide with a partial analytical characterization of the solutions to these Bellman equations.⁴ Let us first focus on the optimal forecast revisions before turning to the optimal time between observations.

2.1 Optimal forecast revision

Using results in Alvarez et al. [2011]⁵, Proposition 2.1 below can be established straightforwardly.

Proposition 2.1 *Let $\theta > 0$, $\psi > 0$ and $\sigma > 0$.*

- (i) $J^*(\tilde{\pi}_f) \leq 1, \forall \tilde{\pi}_f \in \mathbb{R}$.
- (ii) *if $\tilde{\pi}_f$ is such that $J^*(\tilde{\pi}_f) = 1$, then the forecast update is full and occurs instantaneously ($\hat{\pi}_f = 0$ and $t_1 = 0$).*

This proposition means that for the loss function given by Eq. (1) and the forecast gap process defined in Eq. (3), there will be at most one forecast update/adjustment between two forecast target observations and if there is one, it will be fully and instantaneously adjusted to the updated forecast target. The intuition of this result is as follows. If ψ and

⁴Alvarez et al. [2011] do solve the more general case with positive time drift in Eq. (2). As mentioned above, only the zero drift case is relevant here.

⁵Actually, Alvarez et al. [2011] get the same characterization even if the law of motion (2) has a time drift provided its absolute value is small enough. See Proposition 1, page 1921. Our case — zero time drift — is indeed a very elementary special case.

σ are strictly positive, it is immediate to see that in case of inflation forecast adjustment, $\hat{\pi}_f = 0$. Then the optimal choice of the forecaster is to reset the forecast gap to zero. Indeed, it follows from Eq. (3) that the expected value of the forecast gap remains at zero between observations. Consequently, there are no gains to expect from a forecast update without the new pieces of information acquired thanks to an observation. By contrast, due to the fixed adjustment cost $\psi > 0$, the losses involved by a forecast update are strictly positive. So, it is not optimal to adjust the forecast between information set updates. Using the same type of arguments, one can also readily get why the adjustment, if any, should not only be full but also instantaneous. Indeed, if $t_1 > 0$, then the forecaster will incur losses in the time interval $[0; t_1[$. Because the presence of “menu costs” typically induces that adjustments only occur if the gaps are sufficiently large, delaying cannot be optimal as it involves starting the adjustment at such values of the gap: the corresponding trajectory of losses is clearly dominated by a trajectory where adjustment is made instantaneously. Hence $\hat{\pi}_f = 0$ and $t_1 = 0$. A first result of our theoretical model of forecasts formation is that forecasts plans, *i.e.* progressive revision of forecasts between two updates of the information set, are not optimal. The forecast revision, if any, is full and instantaneous at the observation time.

Notice that the resulting Bellman equation (6) can be rewritten as:

$$V_1 = \psi + \theta + \min_{T, \tilde{\pi}_f} \int_0^T e^{-\rho t} (\hat{\pi}_f^2 + \sigma^2 t) dt + e^{-\rho T} \int_{-\infty}^{\infty} V(\hat{\pi}_f - s\sigma\sqrt{T}) dN(s). \quad (8)$$

Remark that V_1 does not depend on $\tilde{\pi}_f$ since $t_1 = 0$. Hence the value function is given by:

$$V(\tilde{\pi}_f) = \min\{V_0(\tilde{\pi}_f), V_1\}, \quad (9)$$

One can see immediately that the value function V is symmetric around $\tilde{\pi}_f = 0$ and increasing for $|\tilde{\pi}_f| < \bar{\pi}$, where $\bar{\pi}$ is a threshold value such that $V_1 > V_0(\bar{\pi})$ for $\tilde{\pi}_f \in (-\bar{\pi}, \bar{\pi})$. Hence $(-\bar{\pi}, \bar{\pi})$ defines the range of inaction in which no forecast adjustment occurs. It means that when $\tilde{\pi}_f$ is smaller than $\bar{\pi}$ in absolute value, then the inflation forecast is not adjusted. Since V is not differentiable at $\tilde{\pi}_f = \bar{\pi}$, the value function is discontinuous,

non-smooth at the boundaries of the inaction band. These properties are summarized in the next proposition⁶:

Proposition 2.2 *The value function V is symmetric around $\tilde{\pi}_f = 0$, and V is strictly increasing in $\tilde{\pi}_f$ for $0 < \tilde{\pi}_f < \bar{\pi}$. $V'(\tilde{\pi}) = 0$ for $\tilde{\pi}_f > \bar{\pi}$ and V is not differentiable at $\tilde{\pi}_f = \bar{\pi}$.*

2.2 Optimal time between observations

As can be seen from Equations (5)-(8), T is a function of $\tilde{\pi}_f$ which will be denoted $T(\tilde{\pi}_f)$ hereafter. Since $\hat{\pi}_f = 0$ at the forecaster optimum, then the optimal time between observations, conditional on adjustment, is $\tau \equiv T(0)$. It follows that $T(\tilde{\pi}_f)$ has a maximum at $\tilde{\pi}_f = 0$ and is symmetric around 0 with an inverted U-shape.⁷ The function $T(\cdot)$ is discontinuous and not differentiable at $\tilde{\pi}_f = \bar{\pi}$, as stated in Proposition 2.3.⁸

Proposition 2.3 *As $\rho \downarrow 0$, the optimal rule for the time of the next observation of the forecast gap is given by*

$$T(\tilde{\pi}_f) = \begin{cases} \tau - \left(\frac{\tilde{\pi}_f}{\sigma}\right)^2 + o(|\tilde{\pi}_f^3|) & \text{if } \tilde{\pi}_f \in (-\bar{\pi}, \bar{\pi}) \\ \tau, & \text{otherwise} \end{cases} \quad (10)$$

Remark that the optimal rule for the time of the next observation is a threshold function of the forecast gap. It is also worth noticing that if there is no forecast gap after an observation, i.e. $\tilde{\pi}_f = 0$, then $T(0)$ is optimal. Finally, $T(\tilde{\pi}_f)$ decreases with $|\tilde{\pi}_f|$. When close to the boundaries of the range of inaction, the forecaster plans an early observation since the target is likely to cross the threshold.

⁶The proof of Proposition 2.2 follows the same steps as the proof of Proposition 3 and lemma 1 in Alvarez et al. [2011]

⁷Here we use Proposition 4, in Alvarez et al. [2011].

⁸The proof of Proposition 2.3 following the same steps as the proof of Proposition 4 in Alvarez et al. [2011], we refer the reader to the latter in order to lighten the presentation.

Let us now focus on the dynamics of the forecast gap on observation and before adjustment. The decision rules described by the threshold $\bar{\pi}$ and the function $T(\cdot)$ imply a stationary Markov process. Let $\tilde{\pi}_f \in \mathbb{R}$ denote the forecast gap immediately after an observation at time t_0 . Then, it follows from Proposition 2.1 that the forecast adjustment rule $\Delta(\tilde{\pi}_f)$ is zero in the inaction zone and $-\tilde{\pi}_f$ otherwise. Assume that the next observation occurs in $T' = T(\tilde{\pi}_f)$ periods and the corresponding forecast gap is $\tilde{\pi}'_f$. Then, it follows immediately from Proposition 2.3 that:

$$\tilde{\pi}'_f = \begin{cases} \tilde{\pi}_f - s\sigma\sqrt{\tau - \left(\frac{\tilde{\pi}_f}{\sigma}\right)^2}, & \text{if } \tilde{\pi}_f \in (-\bar{\pi}, \bar{\pi}) \\ -s\sigma\sqrt{\tau}, & \text{otherwise} \end{cases} \quad (11)$$

Again, this is a threshold process : if the forecast gap is large enough, i.e. larger than $\bar{\pi}$ in absolute value, then it is corrected by setting the forecast to its target and the remaining gap is entirely imputable to unexpected shocks. $\tilde{\pi}'_f$ increases with $|\tilde{\pi}_f|$. When close to the boundaries of the range of inaction but still inside it, the forecast gap reaches its largest values until it hits the boundary and then goes back to its minimum. This is the so-called S-s rule.

Finally, the next proposition can easily be shown to hold⁹:

Proposition 2.4 *Let $\theta > 0$, $\psi > 0$ and $\sigma > 0$, $\frac{\psi}{\theta} < 5.5$. As $\rho \downarrow 0$, there exists a unique solution for $T(0)$ and $\bar{\pi}$ and it is such that*

- (i) $T(0)$ is increasing in ψ and θ ,
- (ii) $\bar{\pi}$ is increasing in ψ and decreasing in θ .

As expected, the time to the next observation after a forecast update, $T(0)$, is increasing in the observation cost and the width of the inaction band defined by $(-\bar{\pi}, \bar{\pi})$ is increasing in the adjustment cost.

⁹Here, we use results from Alvarez et al. [2011] pp. 1931-1932.

3 Forecasts updates data

The empirical analysis below is based on forecasts of annual inflation rate from the monthly survey data set compiled by Consensus Economics Inc. This data set contains inflation rate forecasts made by public and private economic institutions such as banks and research institutes. Due to the fact that Consensus Economics Inc. asks the forecasters to report their forecasts for the annual inflation rates of the current and next calendar years, the data set is a three dimensional panel: forecasters indexed by i , target years indexed by t and horizons indexed by h . For each target year, the data set contains a sequence of 24 forecasts from each forecasters made from January of the year before the target year to December of the target year. The latter will be labelled $h = 0$ since this corresponds to nowcasting. Accordingly, the former will correspond to $h = 23$.

Let $\pi_{i,t|h}$ denote agent i forecast of year t inflation rate, made h months before December of year t . The unconditional probability of updating a forecast for horizon h , denoted $\lambda(i, h)$ after Dovern [2013], is given by the probability that a forecast for the same object, e.g. year t inflation rate, is revised by institution i between two consecutive forecast horizons: $Pr(\pi_{i,t|h} \neq \pi_{i,t|h+1})$. As noted by Dovern [2013], it can be estimated for each horizon, assuming that the probability is the same for each institution as:

$$\hat{\lambda}(h) = \frac{1}{T} \sum_{t=1}^T \frac{1}{N_{t|h}} \sum_{i=1}^{N_{t|h}} 1[\pi_{i,t|h} \neq \pi_{i,t|h+1}], \quad (12)$$

where T is the total number of target years in the sample, $N_{t|h}$ is the number of observed forecasts for target year t with forecast horizon h and $1[.]$ is the indicator function which takes on value 1 if the condition into brackets is verified and zero otherwise.

Our data set includes yearly inflation rate forecasts for the current and next years, made monthly by individual professional forecasters since January 1998 for target years from 2000 to 2015. In the subsequent analysis, we will consider country-specific forecast data. Indeed, this guarantees that the series to forecast, namely the national inflation rate, is homogenous across forecasting units. Moreover, this will allow to emphasize similarities

and differences in forecasting behaviour across country, if any. For France and Germany, the sample includes respectively 36 and 51 forecasters. The main descriptive statistics of the average probabilities of updating between two consecutive months for $h = 22, \dots, 0$, whose expression is given in Eq. (12), are reported in Table 1.¹⁰ Figure 1 shows these update probabilities as a function of the forecast horizon. These basic statistics look quite

Table 1: Descriptive statistics of $\hat{\lambda}(h)$

	Average	Min [h]	Max [h]	$h = 22$	$h = 0$
France	44.8%	27.4% [16]	63.3% [9]	28.8%	32.4%
Germany	41.6%	29.9% [19]	61.5% [12]	30.0%	34.2%

homogenous amongst countries. On average over all horizons, 41.6% (Germany) to 44.8% (France) of forecasters revise their forecasts between two consecutive months. This result is slightly less than Dovern’s [2013] average estimation of nearly 50% over 14 advanced economies : The European professional forecasters considered in our study aren’t the most attentive ones among advanced countries. Nevertheless, this implies a degree of information rigidity which is much lower than the one obtained from aggregate (or average/median) forecast. For instance, Coibion and Gorodnichenko [2012] find that the average inflation forecast across 40 US agents surveyed by SPF is updated every six to seven quarters.¹¹ Similarly high degree of information rigidity is found by Coibion [2010]. Our sample means that 43.2% of the professional forecasters update their forecasts at the monthly frequency.¹²

¹⁰The panel is heavily unbalanced since a large part of the “individuals” have given their forecast in an irregular manner. Consequently, a significant part of forecasts observations could not be used to compute revisions because they are adjacent to missing values. As a result, we are left with a total of 4,990 usable points for France and 8,202 for Germany.

¹¹By contrast, in our French sample for instance, the update share reaches 78% when the probability of updating at least once over the last three months is considered.

¹²The relative frequencies of individual-specific unconditional probability of updating can be obtained by computing the average of $1[\pi_{i,t|h} \neq \pi_{i,t|h+1}]$ across target years and forecast horizons for each forecaster. To save space, descriptive statistics of these $\hat{\lambda}(i)$ ’s are not reported here but are available upon request. Note that their mean is again found to be close to 45%.

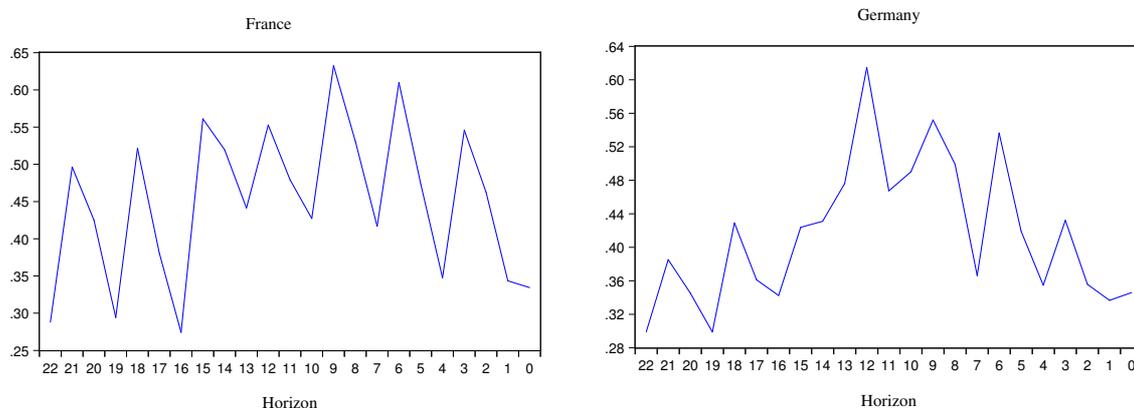


Figure 1: Average revision probability as a function of the forecast horizon

As can be seen from Figure 1, there is no obvious linear trend in the revision probability as horizon increases or decreases, unlike Doovern’s [2013] findings. It can be seen that attentiveness increases until $h = 12$ (Germany) and $h = 9$ (France) and decreases afterwards. The pattern of French update rate shows pronounced seasonality with clear quarterly peaks in March, June, September and December. This could stem from two reasons. First, it is likely that the forecasting exercise is done at the quarterly rather than monthly frequency. Second, the French National Institute of Statistics and Economics Studies releases its first estimate of quarterly real GDP growth 45 days after the end of the quarter, which means around the middle of the second month of each quarter. Since the monthly Consensus Economics Survey is completed before the 12th day of each month, this information is not available when forming the forecast of the quarter’s second month. It is incorporated in the quarter’s third month instead, enhancing the revision probability. This quarterly pattern is also present in Germany, but to a lesser extent and mainly during the target year itself, i.e. for $h = 12, 9, 6$ and 3 .

4 Empirical testing of our model's implications

4.1 Methodology

The empirical testing of our model's implications in terms of time- and state-dependence of the inflation forecast updates will rely on the estimation of binary choice models for panel data. More precisely, the traditional random or fixed effects logit models will be considered to analyze the conditional probability of forecasts revisions. Using a latent variable framework, where $\lambda_{i,t,h}^*$ is a continuous variable that is not observed, it may be written as

$$\begin{aligned}\lambda_{i,t,h}^* &= X_{i,t}\beta + c_i + u_{it} \\ \lambda_{i,t,h} &= 1[\lambda_{i,t,h}^* > 0],\end{aligned}$$

where $\lambda_{i,t,h}$ is an indicator for forecast updates and

$$Pr(\lambda_{i,t,h} = 1 | X_{i,t}, c_i) = G(X_{i,t}\beta + c_i),$$

where $G(\cdot)$ is the logistic CDF for the logit model and the standard normal CDF for the probit model. $X_{i,t}$ is a vector of exogenous explanatory variables and c_i is an unobserved individual-specific effect. In the random effect version, it is assumed that $X_{i,t}$ and c_i are independent and that c_i has a Gaussian distribution with zero mean and constant variance σ_c^2 so that it is possible to estimate the model by maximum likelihood techniques, integrating out the unobserved c_i from the likelihood. The assumption of independence between $X_{i,t}$ and c_i is relaxed in the fixed effect version, and in this case, conditional maximum likelihood estimator is used.¹³

In order to account for the threshold dynamics of forecasts updates implied by the theoretical model presented in Section 2, and particularly from equations (10) and (11), let us introduce a distinction between the switching and non-switching regressors in $X_{i,t}$, denoted respectively by $X_{i,t}^S$ and $X_{i,t}^0$.

¹³All estimations have been performed using version 14.1 of Stata software.

Two regressors will be allowed to switch according to the size of the forecast gap, following the results given in Section 2.2: the time elapsed between two observations ($T(\tilde{\pi}_f)$) and the forecast gap itself ($\tilde{\pi}_f$). The time dependence ($T(\tilde{\pi}_f)$) is captured by a dummy variable denoted $D(d=m)$, $\forall m = 2, 3, \dots$, which is equal to one if the unit's last revision occurred m months ago and zero otherwise. Since very few observations belong to each $D(d=m)$ for $m \geq 8$, the latter are gathered into $D(d \geq 8)$. The threshold variable, namely the forecast gap, is unobservable since the target forecast from which it is evaluated is unobservable. To circumvent that issue, we will use a proxy denoted $Dpm(-1)$. This is the last known monthly inflation rate, weighted by its mechanical contribution to the yearly inflation rate forecast, released at the end of last month/very beginning of the current month (Eurostat release). This is a proxy of the drift of the inflation rate between two consecutive months, which should be incorporated in the new forecast. Assuming the monthly forecasts are constant, this is a proxy of the forecast gap $\tilde{\pi}_f$. From our theoretical model, we expect updates to be triggered only by large changes in the state variable: $|Dpm(-1)|$. Let s_t denote the transition function defined as follows:

$$s_t = 1(|Dpm(-1)| > \gamma),$$

which takes on value 1 for large absolute values of $Dpm(-1)$ and 0 otherwise. Accordingly, the variables $s_t X_{i,t}^s$ and $(1-s_t)X_{i,t}^s$ are introduced as regressors along with the non switching regressors $X_{i,t}^0$. The threshold estimate $\hat{\gamma}$ is obtained by grid search over $\Gamma = [\gamma_{15\%}, \gamma_{85\%}]$, as the one which maximizes the Log-likelihood of the logit model described above. Here, $\gamma_{15\%}$ and $\gamma_{85\%}$ denote the 15% and 85% quantiles of $Dpm(-1)$.

The variables included amongst the non-switching regressors $X_{i,t}^0$ aim at controlling for various effects which have been shown to influence the forecast updating behavior in previous empirical studies¹⁴. Firstly, in order to capture a potential institutional pattern of updating within a given quarter, dummies indicating the second and third month of a quarter, denoted $D(2nd)$ and $D(3rd)$ respectively, are introduced. Secondly, since August

¹⁴See for instance Dovern [2013] and Dovern et al. [2015] and references therein.

is the month when most people are having their summer vacation in the countries considered, it is also introduced as a dummy variable. Thirdly, we introduce the percentage of forecasting units which have revised their forecast last month so as to capture a “cascade” effect ($Sha(-1)$), as described e.g. in Banerjee [1992] or Graham [1999]. Fourthly, a variable called $|Dev(-1)|$, which measures the previous period deviation of the unit’s forecast from the average in absolute value is considered to capture a possible “herding” effect¹⁵. Finally, in order to take into account a business cycle effect, we introduce a target year fixed-effect.

4.2 Estimation results

The estimation results are reported in Table 2 below. The models estimates presented below include both individual and target year fixed effect, since the Hausman statistic p-value strongly rejects the null that both RE and FE models yields the same estimates. Note that only regressors significant in one country at least are reported in this table.

Let us begin with the non-switching variables, at the bottom panel of the regressors list. It appears that the update probability is smaller (respectively larger) the second (third) month of each quarter, revealing an institutional pattern of end-of-quarter forecasting exercise. The August summer vacation effect is particularly strong in France, where the update probability is decreased by around 7% this month. Then, both the cascade and herding effects found out by Dovern [2013] are present in our panels. When the proportion of updaters is high at some time t , then the updating probability is significantly enhanced in $t+1$ (variable $Sha(-1)$). Similarly, the probability to update is significantly increased when a forecaster’s previous forecast is far from last period average forecast (variable $—Dev(-1)—$).

Let us now turn to the threshold effect. First, it is worth it noticing that the threshold models likelihoods are improved compared to their non-switching analogues¹⁶. Then, and surprisingly, the threshold estimates correspond to the 57% quantile of $|Dpm(-1)|$ distri-

¹⁵See e.g. Lamont [2002] or Pons-Novell [2003].

¹⁶The latters estimates aren’t reported to save space, but their log-likelihoods are -3147.81 and -5100.37 for France and Germany respectively.

Table 2: Threshold Logit models with fixed effects

	FR		GE	
	coef.	p-val	coef.	pval
$ Dpm(-1) > \hat{\gamma}$:				
$s_t D(d=3)$	0.024	(0.382)	0.061***	(0.003)
$s_t D(d=6)$	0.184***	(0.008)	0.069	(0.156)
$s_t Dpm(-1) $	0.275***	(0.000)	0.345***	(0.000)
$ Dpm(-1) \leq \hat{\gamma}$:				
$(1 - s_t) D(d=3)$	0.090***	(0.001)	0.112***	(0.000)
$(1 - s_t) D(d=6)$	0.297***	(0.001)	0.140***	(0.003)
$(1 - s_t) Dpm(-1) $	-0.316	(0.424)	-0.784***	(0.000)
D(2nd)	-0.039**	(0.028)	-0.023*	(0.092)
D(3rd)	0.076***	(0.000)	0.067***	(0.000)
August	-0.074***	(0.005)	-0.023	(0.226)
Sha(-1)	0.099**	(0.020)	0.245***	(0.000)
$ Dev(-1) $	0.352***	(0.000)	0.035***	(0.000)
$\hat{\gamma}$ (quantile)	0.068 (57%)		0.085 (57%)	
# obs	4990		8202	
Log-lik	-3141.47		-5082.55	
No year-FE LR(p-val)	0.003		0.008	
# i	36		51	

Numbers are marginal effects computed at sample means for continuous covariates. For dummies, they show the effect of moving from one discrete state to the other one. z-statistics are given into parenthesis. (p-value)

*, ** and *** denote 10, 5 and 1% significance levels.

bution in both countries. This means that the forecast gap does not need to be very large to trigger more updates among the forecast units of our sample: this only requires the gap to be slightly above the median.

Regarding the time dependence of updates, empirical evidence supporting this view comes from the significant increase in the probability of updating if the last revision has been made 3 or 6 months ago. With our theoretical model's implication that forecast update is triggered immediately after observation if the forecast gap is large enough, this gives an upper bound estimate for $T(0)$ of 6 months in both regimes, as predicted by the theoretical model. The six month pattern is even stronger than the 3 month one. This is particularly true in France, where the probability of update is increased by 18.4% if the last revision was six months ago compared to 2.4% if it occurred three months ago in the outer regime. This result holds despite the inclusion of D(2nd) and D(3rd), hence revealing a pure time dependence effect which is not exclusively imputable to forecasters institutional framework. Also as expected by the model, the optimal time to next observation can be shorter in the inaction band, as the estimated coefficients associated to $(1 - s_t)D(d=3)$ are larger than the ones related to $s_tD(d=3)$.¹⁷

Finally, our empirical results also support the state-dependence of the forecast update decision rule. Actually, the update probability is significantly increased when the forecast gap crosses the threshold, by 27.5% in France and 34.5% in Germany. By contrast, this probability is strongly decreased in the aptly named inaction band. There is a significant decrease of 78.4% for German data. French updates also decrease, but by 31.6% only and this result is subject to caution since the z-test p-value is more than 42%. Again, these conclusions are robust to the random effect version of the logit model.

¹⁷The conclusions of these models remain unchanged from random effect logit model estimation and also if a probit model is substituted to the logit model. The exclusion of institutions who provide less than 20 usable observations does not affect the conclusions neither. These results are not reported to save space but are available upon request.

4.3 Empirical evidence of coexistence of observation and adjustment costs

In our set up, the ratio of adjustment to observation costs, ψ/θ , is a non-linear function of observations to adjustment frequencies ratio, denoted n_o/n_a . As shown in Alvarez et al. [2011], this function is well approximated by:

$$\frac{\psi}{\theta} \approx \left(\frac{n_o}{n_a} - 1 \right)^2 \quad (13)$$

Amongst those who observe are of course the adjusters, but also the non-adjusters when the forecast gap (in absolute value) is below the threshold. Yet the latter could also be inattentive forecasters in the sense that they don't update because they don't observe as well. As a consequence adding up these two categories will give us an upper bound of the proportion of observers. The adjustment frequency is obtained straightforwardly from the proportion of adjusters (i.e the ones who have changed their forecasts between two consecutive months).

Using these approximations, we obtain $\psi/\theta = 55,7\%$ in France and $67,1\%$ in Germany.

Table 3: An evaluation of relative costs

	n_o	n_a	ψ/θ
FR	78.6%	45.0%	55.7%
GE	75.9%	41.7%	67.1%

It is worth noting that this ratio is neither zero nor infinity therefore confirming coexistence of both costs. In addition it is below one in both countries, meaning that observation costs dominate communication costs. Even though applied to price setting rules, conclusions obtained by Zbaracki et al. [2004] have the same flavour as ours in the sense that the managerial costs of a large U.S. industrial manufacturer (including information gathering, decision-making, and internal communication costs) are found to be larger than its menu costs (comparable to the external communication costs of our model).

5 Conclusion

This paper first develops a theoretical model of forecasts formation which incorporates separate observation and communication costs. As a result, forecast update decision rule is found to be both time- and state-dependent. The main model's implications for forecasts update process are the following. First, the time between two observations is a non-linear function of the forecast gap: for small gaps $\in (-\bar{\pi}, \bar{\pi})$, the closer to the boundaries, the sooner the next observation. Second, the time between two observations reaches a maximum when the gap is closed. This maximum time increases in both observation and communication costs. Third, the forecast update is triggered immediately after observation if the forecast gap upon observation is large enough in absolute value. If so, the gap is closed by the update. Fourth, the width of the inaction band is increasing in the adjustment cost parameter.

The time- and state-dependence of the observations and forecasts revisions implied by this model are then tested using inflation forecast updates of professional forecasters from recent Consensus Economics panel data for France and Germany. To this end, conditional probabilities as estimated from binary choice models are used.

Our findings clearly support time-dependent updates, a result which is compatible with the observation cost assumption as introduced by Mankiw and Reis [2002]. Indeed, they point to a strong positive effect when the last update has occurred three and/or six months ago, even after controlling for the institutions periodic forecast framework (quarterly or bi-annual). This gives an upper bound estimate of the optimal time between two observations of six months which is well in line with Coibion and Gorodnichenko [2015]'s estimate of the average duration between information updates (six to seven months).

Evidence of updates state-dependence is also provided. Actually, a strong positive and significant effect is found on updates when the forecast gap is larger than the estimated threshold, as proxied by the last known monthly inflation rate, weighted by its mechanical contribution to the yearly inflation rate forecast.

Finally, our results confirm the co-existence of both types of costs with a forecast communication cost smaller than the observation cost. This latter result is very much in line with Zbaracki et al. [2004] findings for firms price setting decision rules.

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