

# Spending Multipliers with Distortionary Taxes: Does the Level of Public Debt Matter?

Rym Aloui, Aurélien Eyquem

## ▶ To cite this version:

Rym Aloui, Aurélien Eyquem. Spending Multipliers with Distortionary Taxes: Does the Level of Public Debt Matter?. 2018. halshs-01942746

# HAL Id: halshs-01942746 https://shs.hal.science/halshs-01942746

Preprint submitted on 3 Dec 2018

**HAL** is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers. L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.



93, chemin des Mouilles 69130 Ecully - France

Maison de l'Université, Bâtiment B 10, rue Tréfilerie 42023 Saint-Etienne cedex 02 - France

http://www.gate.cnrs.fr gate@gate.cnrs.fr

WP 1831 - December 2018

# Spending Multipliers with Distortionary Taxes: Does the Level of Public Debt Matter?

Rym Aloui, Aurélien Eyquem

#### Abstract:

We investigate the link between the size of government indebtedness and the effectiveness of government spending shocks in normal times and at the Zero Lower Bound (ZLB). We develop a New Keynesian model with capital, distortionary taxes and public debt in which the ZLB constraint on the nominal interest rate may be binding. In normal times, high steady-state levels of government debt to GDP lead to reduced output multipliers. After a negative capital quality shock that pushes the economy at the ZLB however, high steadystate debt levels produce larger output multipliers. Our results rely on the fact that fiscal policy becomes self-financing at the ZLB, and that distortionary taxes rise (respectively fall) after a spending shock at the steady state (resp. ZLB). Our results have non-trivial consequences on the design of optimized spending policies in the event of large economic downturns.

#### Keywords:

Zero Lower Bound, Fiscal Policy, Distortionary Taxes, Public Debt

#### JEL codes:

E62, E32



## Spending Multipliers with Distortionary Taxes: Does the Level of Public Debt Matter?\*

Rym Aloui<sup>†</sup> Aurélien Eyquem<sup>‡</sup>

November 28, 2018

#### Abstract

We investigate the link between the size of government indebtedness and the effectiveness of government spending shocks in normal times and at the Zero Lower Bound (ZLB). We develop a New Keynesian model with capital, distortionary taxes and public debt in which the ZLB constraint on the nominal interest rate may be binding. In normal times, high steady-state levels of government debt to GDP lead to reduced output multipliers. After a negative capital quality shock that pushes the economy at the ZLB however, high steadystate debt levels produce larger output multipliers. Our results rely on the fact that fiscal policy becomes self-financing at the ZLB, and that distortionary taxes rise (respectively fall) after a spending shock at the steady state (resp. ZLB). Our results have non-trivial consequences on the design of optimized spending policies in the event of large economic downturns.

Keywords: Zero Lower Bound, Fiscal Policy, Distortionary Taxes, Public Debt.

JEL Classification: E62, E32.

## 1 Introduction

The massive rise in government debt levels and sovereign spreads that followed the 2008 Great Recession and the 2011 recession in countries of peripheral Europe raises the question of whether the level of public debt affects the effectiveness of government spending shocks. In other words, do high levels of sovereign debt undermine the ability of governments to make use of government spending to stabilize the economy? Conventional wisdom suggests that countries with high levels of public debt have less room for fiscal stimulation than countries with low levels of public debt in the event of an economic crisis, and would therefore advocate for low debt levels on average.

We investigate this question in a standard New-Keynesian model with capital accumulation where fiscal solvency is achieved through distortionary taxes on either labor or capital income. In the

<sup>\*</sup>We would like to thank Julien Albertini, Hafedh Bouakez, Thomas Brand and participants of the T2M Lisbon and SCE New York conferences for thoughtful comments. Aurélien Eyquem gratefully acknowledges financial support of the ANR program entitled ANR-15-CE33-0001-02 FIRE.

<sup>&</sup>lt;sup>†</sup>Univ Lyon, Université Lumière Lyon 2, GATE UMR 5824, F-69130 Ecully, France. aloui@gate.cnrs.fr.

<sup>&</sup>lt;sup>‡</sup>Univ Lyon, Université Lumière Lyon 2, GATE UMR 5824, F-69130 Ecully, France; Institut Universitaire de France. aurelien.eyquem@univ-lyon2.fr.

data, countries with higher levels of debt also feature higher levels of tax rates (see Appendix A). Because debt is high, they potentially face larger costs of debt rollover, and because taxes are high, they face larger efficiency costs of distortionary taxation. In this paper, we show that the initial level of debt lowers public spending multipliers in normal times but raises public spending multipliers the Zero Lower Bound (ZLB). In normal times, a spending shock financed by a combination of public debt and a distortionary tax rule leads to a larger increase in public debt and in future tax rates. This imposes more distortions on production factors and reduces the positive effects of a spending shock on output. At the ZLB, in line with Erceg and Lindé (2014). we find that a spending shock at the ZLB is self-financing. This leads public debt and future tax rates to *fall*, lowers the amount of distortions imposed on production factors, and further raises output. The shock leading the ZLB to be binding is here a negative capital quality shock, as in Gertler and Karadi (2011), but our results are robust to considering a discount factor shock. One important difference between capital quality shocks and discount factor shocks is that the latter produce a *rise* in private investment while the former produce a *fall* in private investment. We thus consider the former to be more consistent with the Great Recession narrative, and with the factors that most likely led nominal interest rates to hit the ZLB.

Quantitatively speaking, our model produces public spending multipliers that line-up quite well with the literature. During normal times, short-run multipliers (at a 2 years horizon) roughly range from 0.2 to 0.3 for an empirically plausible calibration of the model. When the spending shock hits conditional on a negative capital quality shock that pushes the economy at the ZLB for a few quarters, short-run multipliers range from 1.4 to 1.45 for the same calibration. In any case, spending multipliers at the ZLB are larger than spending multipliers at the steady-state, as in Christiano, Eichenbaum, and Rebelo (2011) and the subsequent literature. The impact of the initial level of debt is relatively small for short-run multipliers at the steady state, but can be very large for short-run multipliers at the ZLB. These results are quantitatively but not qualitatively sensitive to a small subset of parameters such as the Frisch elasticity on labor supply, the degree of complementarity between public and private goods in the utility function of households, or the responsiveness of the tax rules. Finally, we show that the initial level of debt crucially affects the optimized response of government spending to a large crisis that pushes the economy to the ZLB. The size and persistence of the rise in public expenditure varies depending on the initial level of debt, which is only a consequence of the fact that the effects on output of changes in spending are stronger when the initial level of debt is higher.

Our paper relates to the literature on spending multipliers that questions how the economic environment may affect the latter. Empirically, one of the first papers to raise the question was Perotti (1999). More recently, the subject has been revived by Auerbach and Gorodnichenko (2012), investigating whether the business cycle position matters for the value of multipliers. Two papers, respectively by Corsetti, Meier, and Müller (2012) and by Ilzetzki, Mendoza, and Végh (2013) question more precisely the impact of debt or fiscal stress on spending output multipliers. Their results converge and conclude that fiscally stressed or highly indebted economies tend to be characterized by lower spending multipliers. Our results about the impact of the initial level of debt on the size of fiscal multipliers are in accordance with those results, as we find that a high level of debt lowers the spending multiplier. Further, according to Corsetti, Meier, and Müller (2012), when an economy experiences a financial crisis, spending multipliers are much larger than in normal times. If one admits that financial crises are more likely to lead to ZLB episodes, this result is also consistent with more theoretical contributions like Christiano, Eichenbaum, and Rebelo (2011) and the subsequent literature. Our results are also consistent with this empirical result, as we find that spending multipliers are larger during a financial crisis, triggered by a negative capital quality shock that pushes the economy at the ZLB. A recent paper by Boitani and Perdichizzi (2018) tests the joint conditional impact of recessions and the level of debt on the size of spending multipliers. Boitani and Perdichizzi (2018) find evidence of self-financing public spending shocks during recessions in Euro Area countries, and find that multipliers are larger in high deficit countries than in low deficit countries, providing empirical evidence in favor of our results.

Our paper also belongs to a model-based literature that investigates the effects of the ZLB on the size of fiscal multipliers, summarized and referenced in Eggertsson (2011). In particular, Erceg and Lindé (2014) find that fiscal policy becomes self-financing at the ZLB, a result that is also present in our paper and key to our main result. To our knowledge however, there are only very few papers questioning the effect of the initial debt level on the size of public spending multipliers. Corsetti, Kuester, Meier, and Müller (2013) do investigate this question but their analysis does not consider capital accumulation, and essentially focuses on the case of lump-sum taxes, while our main focus is on distortionary taxes. Along this dimension, our framework is closer to Nakata (2017), although we consider a richer model with capital accumulation, and our main focus is not on Ramsey equilibria but on the size of government spending multipliers and optimized policies. Our paper also echoes the recent contribution of Bilbiie, Monacelli, and Perotti (2018), who derive optimal spending policies at the ZLB with an additional focus on spending multipliers. However, they consider lump-sum taxes and do not investigate the impact of the initial level of debt on spending multipliers and optimized policies.

The paper is organized as follows. Section 2 presents the model and details our calibration. Section 3 analyzes the Impulse Response Functions to spending shocks hitting at the steady state or conditional on a negative capital quality shock that pushes the economy at the ZLB, depending on whether the initial debt-to-GDP ratio and taxes are low or high. Section 4 summarizes our results by presenting the value of spending multipliers at various horizons and under the different cases considered, and produces an extensive sensitivity analysis. Section 5 investigates the design of optimized spending rules, and Section 6 concludes.

### 2 Model

Our framework builds on a standard New Keynesian model with capital accumulation, sticky prices, public goods entering the utility of households and a monetary policy that is restricted by a (zero) lower bound on the nominal interest rate. Public expenditure are financed through public debt and distortionary taxes on capital and labor income.

#### 2.1 Households

Households choose consumption, labor supply, deposits and government bonds maximizing lifetime welfare

$$E_t \left\{ \sum_{s=t}^{\infty} \left( \beta^{s-t} \right) u \left( c_s, g_s, \ell_s \right) \right\},\tag{1}$$

where  $u_{\ell,t} \leq 0$ ,  $u_{c,t} \geq 0$  and  $u_{g,t} \geq 0$  are the first-order partial derivatives with respect to the private consumption,  $c_t$ , hours worked,  $\ell_t$  and the amount of public spending,  $g_t$ . Parameter  $\beta \in (0,1)$  denotes the subjective discount factor. Households optimize subject to the following budget constraint

$$b_t^g + p_t \left( (1+\mu) c_t + k_t \right) = r_{t-1} b_{t-1}^g + p_t \left( (1-\tau_t) w_t \ell_t + R_t^k k_{t-1} \right) + \Pi_t.$$
(2)

In this equation,  $b_t^g$  denotes the nominal amount of government bonds that returns  $r_t$  between period t and period t + 1. Further,  $\mu$  is a (constant) distortionary tax on consumption,  $w_t$  is the real wage, and  $\tau_t$  is a distortionary tax on labor income.<sup>1</sup> Variable  $R_{kt} = 1 + (1 - \eta_t) (r_t^k - \delta)$ is the after-tax real gross return on capital where  $\eta_t$  is the capital income tax that comes with a deduction for capital depreciation  $\delta$ , and  $r_t^k$  denotes the real rental rate on the capital stock. Finally,  $\Pi_t$  comprises monopolistic profits from firms. An additional constraint to the optimization program is the law of capital accumulation

$$k_t - (1 - \delta) \,\xi_t k_{t-1} = i_t \left( 1 - \left( \varphi^i / 2 \right) x_t^2 \right), \tag{3}$$

where  $i_t$  is the amount of investment in physical capital,  $x_t = i_t/i_{t-1} - 1$  is the growth rate of investment, and  $\varphi_i > 0$  controls the size of investment adjustment costs. The stock of capital is potentially affected by a quality shock  $\xi_t$ , that follows an AR1 process:  $\xi_t = (1 - \rho_{\xi}) \xi + \rho_{\xi} \xi_{t-1} + \varepsilon_{\xi,t}$ , where  $\rho_{\xi} \in [0, 1)$  and  $\varepsilon_{\xi} \sim \mathcal{N}\left(0, \sigma_{\xi}^2\right)$ . First-order conditions with respect to deposits, bonds

<sup>&</sup>lt;sup>1</sup>The consumption tax rate is introduced in the model to allow for a more realistic baseline calibration. In particular, we want both capital and labor income tax rates to be on the increasing part of the Laffer Curve to allow these instruments to be effective in stabilizing the level of debt. However,  $\mu$  will not be considered as an active policy instrument.

and labor supply imply

$$E_t \{\beta_{t,t+1} r_t / \pi_{t+1}\} = 1, \tag{4}$$

$$u_{\ell,t} + (1 - \tau_t) u_{c,t} w_t / (1 + \mu) = 0, \qquad (5)$$

where  $\beta_{t,t+1} = \beta u_{c,t+1}/u_{c,t}$  and where  $\pi_t = p_t/p_{t-1}$  is the inflation rate. The first equation prices government bonds. The second equation relates the marginal disutility of working to the real wage, expressed in terms of the marginal utility of consumption. We define  $q_t p_t u_{c,t}$  as the Lagrangian multiplier associated with the capital accumulation constraint, and derive the following first-order conditions with respect to the capital stock and investment:

$$E_t \left\{ \beta_{t,t+1} \left( q_{t+1} \left( 1 - \delta \right) \xi_{t+1} + \left( 1 - \eta_t \right) r_{t+1}^k + \eta_t \delta \right) \right\} = q_t, \qquad (6)$$

$$q_t \left(1 - \left(\varphi^i/2\right) x_t^2 - \varphi^i x_t \left(1 + x_t\right)\right) + E_t \left\{\beta_{t,t+1} q_{t+1} \varphi^i x_{t+1} \left(1 + x_{t+1}\right)^2\right\} = 1.$$
(7)

#### 2.2 Firms

A perfectly competitive representative firm produces a final consumption good  $y_t$  using a continuum of intermediate goods indexed in  $j \in [0, 1]$ , according to the following production function:

$$y_t = \left[\int_0^1 y_t\left(j\right)^{\frac{\theta-1}{\theta}} dj\right]^{\frac{\theta}{\theta-1}},\tag{8}$$

where  $y_t(j)$  denotes the time t input of intermediate good j and  $\theta$  the elasticity of substitution across intermediate goods. The firm takes the price of output  $p_t$  and the input price  $p_t(j)$  as given. Profit maximization leads to the following first-order condition:

$$y_t(j) = (p_t(j)/p_t)^{-\theta} y_t.$$
 (9)

Substituting (8) into (9) yields the following relationship between the aggregate price level and the price of intermediate goods:

$$p_{t} = \left[ \int_{0}^{1} p_{t} \left( j \right)^{1-\theta} dj \right]^{\frac{1}{1-\theta}}.$$
 (10)

Intermediate good  $j \in (0, 1)$  is produced under monopolistic competition using capital  $k_{t-1}$  and labor  $\ell_t$  with the following production function:

$$y_t(j) = (\xi_t k_{t-1}(j))^{\iota} \ell_t(j)^{1-\iota}, \qquad (11)$$

where  $\iota \in (0, 1)$  is the share of capital in value-added. Intermediate good producers rent the effective capital stock and hire workers in perfectly competitive markets. Profits are distributed

to the households at the end of each period. Recalling that  $r_t^k$  and  $w_t$  denote the real rental rate on capital and the real wage, respectively, the real marginal cost of intermediate good producers is:

$$s_t = \left(\iota^{\iota} \left(1 - \iota\right)^{1 - \iota}\right)^{-1} \left(r_t^k\right)^{\iota} (w_t)^{1 - \iota}.$$
 (12)

Profits are  $[p_t(j)/p_t - s_t] p_t y_t(j)$ , where  $p_t(j)$  is the price of the good produced by firm j in period t. We assume there are Calvo price-setting contracts, where  $1/(1-\gamma)$  and  $\gamma_p$  respectively represent the average length of contracts and an indexation parameter with respect to past inflation. The optimal pricing conditions are standard and therefore not reported.

#### 2.3 Government, Central Bank and Aggregation

Given our assumptions regarding taxes, the budget constraint writes:

$$b_t = r_t b_{t-1} + p_t \left( g_t - \tau_t w_t \ell_t - \eta_t \left( r_{kt} - \delta \right) k_{t-1} - \mu c_t \right).$$
(13)

where  $b_t$  is the amount of nominal bonds issued by the government. Expressed in real terms, the budget constraint writes

$$b_t^r = r_t b_{t-1}^r / \pi_t + g_t - \tau_t w_t \ell_t - \eta_t \left( r_{kt} - \delta \right) k_{t-1} - \mu c_t.$$
(14)

where  $b_t^r = b_t/p_t$ . The stability of the debt-to-GDP ratio in the long run is ensured by the following tax rules:

$$\tau_t = \tau + d_\tau \left( b_{t-1}^r - b^r \right)$$
(15)

$$\eta_t = \eta + d_\eta \left( b_{t-1}^r - b^r \right), \tag{16}$$

where the parameters  $d_{\tau}$  and  $d_{\eta}$  respectively measure the responsiveness of the labor income tax and the capital income tax to the deviation of the ratio from its initial steady state value. Government spending evolve following a standard AR(1) process:

$$\log\left(g_t/g\right) = \rho_g \log\left(g_{t-1}/g\right) + \varepsilon_{g,t},\tag{17}$$

where  $\rho_g \in [0, 1)$  and  $\varepsilon_g \sim \mathcal{N}(0, \sigma_g^2)$ , and where g is the initial steady state level of government expenditure. The Central Bank sets the gross nominal interest rate  $r_t$  according to

$$r_t = \max\left(1, rn_t\right),\tag{18}$$

where  $rn_t$  is the desired gross nominal interest rate that evolves according to:

$$\log(rn_t/r) = d_\pi \log\left(\pi_t/\pi\right) + d_y \log\left(y_t/\widetilde{y}_t\right),\tag{19}$$

In the above equation,  $\pi_t$  is the inflation rate and  $\tilde{y}_t$  is the natural level of output.<sup>2</sup> Parameters  $d_{\pi}$  and  $d_y$  are the elasticities of  $rn_t$  to inflation and the output gap, respectively. The central bank sets  $r_t$  equal to  $rn_t$  if and only if its policy rule implies a non-negative level for the nominal interest rate. Otherwise, the ZLB binds and  $r_t$  equals one. A competitive equilibrium in our model is defined as a situation where (i) households and firms optimize for a given path of policy instruments, and (ii) prices clear markets according to:

Intermediate goods: 
$$(\xi_t k_{t-1})^{\iota} \ell_t^{1-\iota} = \int_0^1 y_t(j) \, dj = y_t dp_t,$$
(20)

Final goods: 
$$y_t = c_t + i_t + g_t$$
 (21)

- Government bonds:  $b_t = b_t^g$  (22)
  - Deposits:  $d_t = 0$  (23)

where  $dp_t = \int_0^1 (p_t(j)/p_t)^{-\theta} dj \ge 1$  measures the dispersion of prices.

#### 2.4 Calibration and set-up

The model is quarterly and our calibration is intended to capture an average OECD country. We adopt a formulation of the utility where private and public goods provide direct utility:

$$u(c_t, g_t, n_t) = \log\left(\widetilde{c}_t\right) - \omega \ell_t^{1+\psi} / \left(1+\psi\right), \qquad (24)$$

where

$$\widetilde{c}_{t} = \left(\kappa c_{t}^{\frac{\nu-1}{v}} + (1-\kappa) g_{t}^{\frac{\nu-1}{v}}\right)^{\frac{\nu}{\nu-1}}, \ \nu > 0.$$
(25)

In equation (25),  $\kappa$  denotes the weight of private consumption in the effective consumption index, and  $\nu$  is the elasticity of substitution between the private and the public good. When  $\nu = 0$ , public and private goods are pure complements. As  $\nu$  increases, private and public goods become more and more substitutable, and pure substitutability arises when  $\nu \to \infty$ . This specification is in the spirit of Leeper, Traum, and Walker (2015), but our choice of a CES specification is justified by the need to capture the diminishing marginal returns to public spending in order to achieve a given level of effective consumption, *ceteris paribus*. Empirical evidence favor estimates pointing to a mild complementarity (see Bouakez and Rebei (2007)) and we set  $\nu = 0.45$  in the benchmark calibration.<sup>3</sup> We also impose the value of  $\kappa$  so that the marginal utilities of private and public goods are equal in the steady state, an application of Samuelson's principle.<sup>4</sup>

$$\kappa = g^{-\frac{1}{\nu}} / \left( c^{-\frac{1}{\nu}} + g^{-\frac{1}{\nu}} \right).$$

<sup>&</sup>lt;sup>2</sup>As in Gertler and Karadi (2011), variations in the mark-up serve as a proxy for variations in the output gap.

<sup>&</sup>lt;sup>3</sup>This second value is also broadly consistent with the point estimates found by Auray and Eyquem (2017), between 0.5 and 0.6, and with the estimates of Leeper, Traum, and Walker (2015), according to which public and private goods are complements.

<sup>&</sup>lt;sup>4</sup>The value of  $\kappa$  that is consistent with the optimal provision of public good in the steady-state is indeed  $u_c = u_g$ and implies:

The discount factor is  $\beta = 0.99$  implying an annual real interest rate of 4.1 percents. The inverse of the Frisch elasticity of labor supply is typically a controversial and important parameter. We impose  $\psi = 3$  to capture relatively sluggish labor markets, a value that lies in-between the calibration of Corsetti et al. (2013) and that of Galí, López-Salido, and Vallés (2007). Because this parameter is both non-consensual, and key in generating our results, a sensitivity analysis will be conducted. On the production side, the share of capital is  $\iota = 0.33$ , and the steadystate depreciation rate is  $\delta = 0.018$  (7% annually). The investment adjustment cost parameter,  $\varphi_i$ , is set to 1.8. The steady-state mark-up is 30%, implying  $\theta = 4.33$ , the Calvo parameter on price contracts is  $\gamma = 0.75$  a standard value in quarterly models of price adjustments, and the indexation parameter is  $\gamma_P = 0.5$ . The feedback parameters of the fiscal rules are  $d_{\tau} =$  $d_{\eta} = 0.1$ , which ensures medium-run fiscal solvency, and makes fiscal policy passive in the sense of Leeper (1991). These values are quite larger than usually estimated to built intuition. Given their importance in generating our results, a sensitivity analysis with respect to these parameters will be conducted. Parameters of the Taylor rule are  $d_{\pi} = 1.5$  and  $d_y = 0.125$  and the persistence parameters of shocks are  $\rho_{\xi}$  = 0.7 and  $\rho_g$  = 0.85. In the baseline calibration, we impose  $b^g/(4y) = 0.8$  and adjust the value of  $\omega$  to get  $\ell = 0.3$ . Both targets are realistic when it comes to match observed values in OECD countries. Whenever the debt-output ratio is varied,  $\omega$  remains unchanged. In line with OECD averages, the share of public consumption in GDP is  $s_g = g/y = 0.2$ , the capital income tax rate is  $\eta = 0.2$ , the consumption tax rate is  $\mu = 0.15$  and the labor income tax rate is adjusted to match the debt-to-GDP ratio target, implying  $\tau = 0.2207$  when  $b^{g}/(4y) = 0.8$ , a number well within OECD average labor income tax measures. Table 1 summarizes our parameter values.

In the next paragraphs we consider various steady-state levels of debt-to-GDP ratios  $b^{g}/(4y)$ . When varying  $b^{g}/(4y)$ , we let the labor income tax rate adjust to maintain fiscal solvency in the steady state. This approach is backed by a quick glance at the data. Indeed, we show in Appendix A that debt-to-GDP ratios relate positively to labor income taxes across years and countries, using two separate datasets.<sup>5</sup>

### 3 Impulse response functions

In the following experiments, we investigate the responses of our model economy under two polar cases for the debt level,  $b^g/(4y) = 0.6$  referred to as the case of low debt, and  $b^g/(4y) = 1.15$ , referred to as the case of high debt. In each case, the calibration remains the same except for the steady-state level of debt and for the labor or capital income tax rate. In particular, the labor disutility parameter  $\omega$  remains unchanged, so when tax rates change the steady-state level of hours worked, capital and output change as well. We get  $\tau = 0.2050$  in the case of low debt-

<sup>&</sup>lt;sup>5</sup>The relation is less clear for consumption tax rates but we do not consider this instrument in our analysis.

Discount factor	$\beta = 0.99$
Edgeworth preference parameter	$\nu = 0.45$
Inverse of the Frisch elasticity of labor supply	$\psi = 3$
Steady-state depreciation rate of capital	$\delta = 0.018$
Production function, capital parameter	$\iota = 0.33$
Investment adjustment cost parameter	$\varphi_i = 1.8$
Steady-state mark-up	$\theta/\left(\theta-1\right)=1.3$
Calvo parameter	$\gamma = 0.75$
Indexation parameter	$\gamma^p = 0.5$
Fraction of time spent working	$\ell = 0.3$
Labor disutility parameter	$\omega = adjusted$
Government debt to annual GDP	$b^g/\left(4y\right) = 0.8$
Government spending to GDP	$s_g = 0.2$
Labor income tax rate	$\tau = 0.2207$
Capital income tax rate	$\eta = 0.2$
Consumption tax rate	$\mu = 0.15$
Tax rule parameters	$d_{\tau} = d_{\eta} = 0.1$
Taylor rule, response to inflation	$d_{\pi} = 1.5$
Taylor rule, response to output gap	$d_y = 0.125$
Persistence of public spending shock	$\rho_{g} = 0.85$
Persistence of capital quality shock	$\rho_{\xi} = 0.7$

 Table 1: Baseline parameter values

to-GDP ratio and  $\tau = 0.2481$  when the steady-state ratio is high. These numbers are reasonable in comparison to observed labor and capital income tax rates in OECD countries (See Appendix A).

#### 3.1 Public spending shocks

Figure 1 reports the Impulse Response Functions (IRFs hereafter) of the economy to a one percent public spending shock with a labor income tax rule. The top panel reports the dynamics when the shock hits at the steady state while the bottom panel reports the dynamics conditional on a 5% capital quality shock that depresses the economy and pushes the nominal interest rate to the ZLB.<sup>6</sup> The model is simulated using the fully non-linear model under perfect foresight, based on a Newton-Raphson algorithm.<sup>7</sup> Even though we solve under perfect foresight, the shock that hits in period 1 is a surprise to the agents. Therefore, because there are only shocks at period 1

<sup>&</sup>lt;sup> $^{6}</sup>Appendix B$  provides the IRFs to this shock only. In line with Gertler and Karadi (2011), a capital quality shock induces a fall in output, consumption, investment, real wages, hours worked, the price of equity, and inflation, pushing the economy to the ZLB for 4 quarters. It also raises public debt and tax rates. While Gertler and Karadi (2011) set a smaller shock value, notice that our model does not feature banking frictions and therefore requires a larger innovation to produce a similar negative output dynamics – as well as a binding ZLB.</sup>

<sup>&</sup>lt;sup>7</sup>The algorithm is a built-in routine of Dynare 4.5.1 (Adjemian (2011)). It is an application of the Newton-Raphson algorithm that takes into consideration the special structure of the Jacobian matrix in dynamic models with forward-looking variables. The details of the algorithm are explained in Juillard (1996). The algorithm *does* not rely on linearization.

under all our simulations, the model solution captures accurately the relevant non-linearities of the model, including the ZLB constraint. The black solid line shows the response of the economy with a low steady-state debt-to-GDP ratio (60%) while the red line shows the response with a high ratio (115%).

The top panel of Figure 1 shows that a spending shock has positive effects on output, does not crowd out private consumption much (remember that public and private goods are complements), and lowers investment. The real wage and hours worked both increase since the demand for final goods rises, as shown by the rise in the inflation rate. In terms of public finance, both public debt to GDP and tax rates increase, which contributes to moderate the rise in hours worked further crowd-out private investment compared to the case of lump-sum taxes.<sup>8</sup> The most interesting feature of this figure lies in the differences between a low or a high steady-state debt-to-GDP ratio. With a high steady-state ratio, a public spending shock leads the debt-output ratio to rise much more than with a low initial ratio. For a given dynamics of the nominal interest rate, a country with a higher debt-output ratio faces a larger rollover cost when debt increases, which requires a larger subsequent fiscal adjustment. In addition, a country with a high level of debt also faces a higher level of taxes. Since the cost of taxation is convex, the tax rate has to increase more to produce the required increase in government revenue. Thus, the shock induces both the labor income tax rate and the capital income tax rate to increase more, imposing larger distortions on hours worked, private investment and hence on output. The dynamics of the real wage is further marginally less positive in this case, which translates into slightly smoother inflation and nominal interest rate dynamics.

Let us now focus on the case where the public spending shock hits conditional on a crisis. The latter is triggered by a 5% capital quality shock. The dynamics generated by the public spending shock conditional on a crisis is obtained by taking the difference between the joint shock and a crisis shock only. The bottom panel of Figure 1 thus reports the net effects of the public spending shock.

On impact, when the ZLB is strictly binding, an increase in government spending leads to a rise in output, marginal cost, and inflation. The increase in expected inflation lowers the real interest rate, which drives up private consumption much more than when the shock hits at the steady state. This rise in private consumption expenditure leads to a further rise in output, marginal cost, and expected inflation and a further decline in the real interest rate. In addition, at the ZLB, the price of capital *rises* instead of *falling* which also boosts private investment instead of depressing it. These results line up very well with the findings of Christiano, Eichenbaum, and Rebelo (2011). Interestingly enough, output increases more in the case of a high initial

<sup>&</sup>lt;sup>8</sup>IRFs under lump-sum taxes do not show any difference whether debt is high or low, under any of the situations we consider. These IRFs are available upon request.

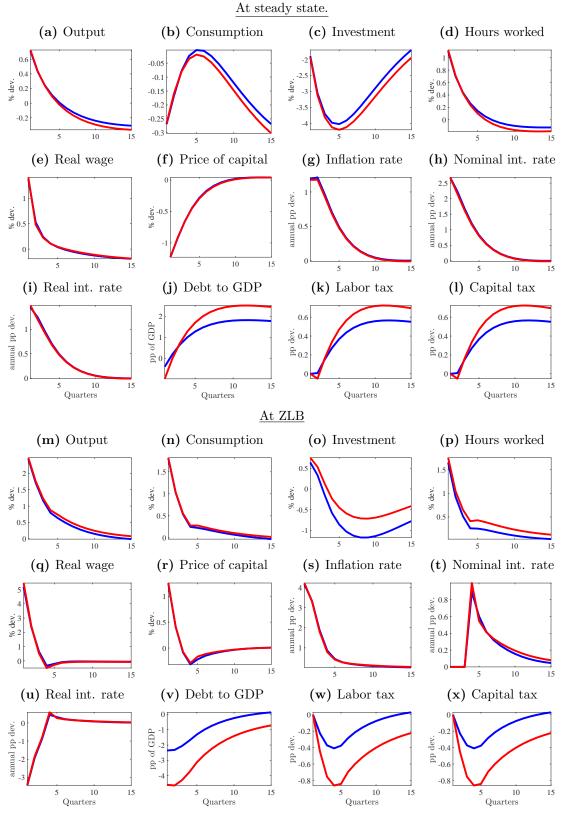


Figure 1: IRFs to a 1% public spending shock.

Black:  $b^g/(4y) = 0.6$  and  $\tau = 0.2050$ . Red:  $b^g/(4y) = 1.15$  and  $\tau = 0.2481$ .

debt-to-GDP ratio, leading to a larger value of the government spending multiplier. We explain these results in the following way.

When a government spending shock hits at the ZLB, consumption is more strongly crowded-in and private investment is crowded-in instead of being crowded-out. Aggregate demand is thus boosted by much more, which results in a massive rise in labor demand: hours worked and the real wage both rise more at the ZLB. Hours increase by more than 1.5% (instead of 1% out of the ZLB) and the real wage increases by more than 4% (instead of 1.5%). These effects are clearly not new and explained extensively in several papers (see Christiano, Eichenbaum, and Rebelo (2011) and the subsequent literature). In addition, as in Erceg and Lindé (2014), fiscal policy becomes self-financing because tax bases increase massively. Hence, the debt-to-GDP ratio falls instead of rising, triggering a *fall* in the labor and capital income tax rates. The latter further boost the economy by lowering the overall distortions on labor supply and capital accumulation. Finally, because countries with a higher debt level also have a higher tax level, and because the costs of taxation are convex, these movements are larger for economies featuring a large initial debt-to-GDP ratio. Therefore, when the public spending shock hits at the ZLB and produces a fall in the debt-to-GDP ratio, the high-debt economy features a larger public spending multiplier. We expect this result to be sensitive to the labor supply elasticity, as the strength of tax base dynamics depends on how much households are willing to increase their labor supply after a spending shock, but also to the parameters of the tax rules.

## 4 Government spending multipliers

We now investigate more systematically the extent to which the initial debt-to-GDP ratio affects the value of present-value public spending multipliers. While the impact multiplier is an important measure of the effectiveness of fiscal policy, looking at longer horizons matters insofar the dynamics of subsequent fiscal adjustments matters for the overall effectiveness of fiscal policy. Our preferred measure will therefore be the present-value multiplier at different horizons. The latter is defined as the discounted cumulative increase in output over T periods that results from the discounted cumulative increase in public spending over T periods after a spending shock in period 1:

$$PVM_T = \frac{\sum_{j=1}^T \beta^j (y_{t+j} - y_t)}{\sum_{j=1}^T \beta^j (g_{t+j} - g_t)}.$$
(26)

Table 2 below reports the values of the present-value multipliers at 2 years (T = 8) and at 5 years (T = 20) under various configurations, when the shock hits at the steady state or conditional on a crisis. We consider both a labor income tax rule and a capital income tax rule, and investigate the sensitivity of our result to the Edgeworth complementarity parameter, to the Frisch elasticity of labor supply and to the strength of the response of tax rates in the tax rules.

				, ,		0.45						
	$c_t$ and $g_t$ complements ( $\nu = 0.45$ )											
			$^{g}/\left( 4y\right) =0.$			High debt $(b^g/(4y) = 1.15)$						
		y state	ZI	LB		y state	ZI	ZLB				
	2 years	5 years	2 years	5 years	2 years	5 years	2 years	5 years				
$\psi = 3$	0.207	-0.263	1.403	1.124	0.177	-0.359	1.492	1.321				
$\psi = 2$	0.308	-0.196	1.363	1.079	0.277	-0.298	1.480	1.326				
$\psi = 1$	0.494	-0.061	1.191	0.848	0.468	-0.159	1.292	1.059				
$d_{\tau} = d_{\eta} = 0.05$	0.255	-0.131	1.426	1.164	0.239	-0.188	1.470	1.286				
$d_{\tau} = d_{\eta} = 0.04$	0.265	-0.099	1.424	1.162	0.253	-0.146	1.464	1.269				
$d_{\tau} = d_{\eta} = 0.03$	0.275	-0.064	1.420	1.156	0.266	-0.100	1.453	1.244				
$d_{\tau} = d_{\eta} = 0.02$	0.286	-0.027	1.413	1.146	0.280	-0.052	1.437	1.210				
$d_{\tau} = 0.1, d_{\eta} = 0$	0.232	-0.194	1.389	1.119	0.210	-0.271	1.452	1.269				
$d_{\tau} = 0.05, d_{\eta} = 0$	0.273	-0.073	1.424	1.164	0.263	-0.114	1.460	1.257				
$d_{\tau} = 0.02, d_{\eta} = 0$	0.295	0.006	1.416	1.148	0.291	-0.011	1.437	1.196				
	$c_t$ and $g_t$ substitutes ( $\nu = 1$ )											
	L	ow debt (b	$\overline{g/\left(4y\right)} = 0.$	6)	Hi	High debt $\left( b^{g} / \left( 4y \right) = 1.15 \right)$						
	Steady	y state	ZI	LB	Stead	y state	ZLB					
	2 years 5 years		2 years	5 years	2 years	5 years	2 years	5 years				
$\psi = 3$	0.057	-0.301	0.765	0.501	0.039	-0.359	0.864	0.672				
$\psi = 2$	0.092	-0.318	0.705	0.407	0.073	-0.381	0.826	0.615				
$\psi = 1$	0.158	-0.351	0.584	0.195	0.141	-0.412	0.709	0.414				
$d_{\tau} = 0.05$	0.106	-0.171	0.782	0.561	0.096	-0.205	0.836	0.662				
$d_{\tau} = 0.04$	0.116	-0.138	0.785	0.573	0.109	-0.167	0.829	0.657				
$d_{\tau} = 0.03$	0.127	-0.104	0.787	0.585	0.121	-0.126	0.820	0.650				
$d_{\tau} = 0.02$	0.138	-0.066	0.789	0.597	0.134	-0.081	0.811	0.642				
$d_{\tau} = 0.1, d_{\eta} = 0$	0.078	-0.238	0.756	0.516	0.064	-0.285	0.842	0.657				
$d_{\tau} = 0.05, \dot{d}_{\eta} = 0$	0.121	-0.117	0.777	0.574	0.114	-0.143	0.824	0.655				
$d_{\tau} = 0.02, d_{\eta} = 0$	0.146	-0.036	0.786	0.605	0.144	-0.046	0.807	0.639				

 Table 2: Multipliers at different horizons.

Quantitatively speaking, multipliers at 2 years broadly range from 0.05 to 0.5 when the shock hits at the steady state, and from 0.6 to 1.5 at the ZLB. These intervals are wide but the value of multipliers is crucially affected by the complementarity parameter  $\nu$  and by the labor supply elasticity  $1/\psi$ . Empirically,  $\nu$  and  $\psi$  are more likely to be close to the baseline calibrated values  $\nu = 0.45$  and  $\psi = 3$ , suggesting multipliers at 2 years between 0.18 and 0.29 at the steady state, and between 1.4 and 1.45 at the ZLB. These are relatively consensual values in the literature.

As already suggested by the analysis of the IRFs, multipliers at the ZLB are much larger than multipliers at the steady state, both at the horizon of 2 years and 5 years. This statement is true both at low and high levels of debt. While this result may not be new, the fact that multipliers are large at the ZLB are clearly the explanation for the fact that fiscal policy becomes selffinancing (see Erceg and Lindé (2014)), leading public debt to fall and future tax rates to drop as well. Because of their distortionary nature, this in turn impacts the dynamics of factor prices and quantities, and then the dynamics of output. Indeed, when the shock hits at the steady state, multipliers are either slightly lower (2 years) or substantially lower (5 years) in the high debt economy, because debt and taxes increase after the shock. The pattern reverses at the ZLB because debt and taxes fall after the shock. These results hold qualitatively for all the parameter values considered in Table 2.

In addition, when public and private goods are complements, multipliers are always larger whatever the configuration or the calibration. This too shall not be surprising as an increase in public spending crowds-in consumption (at the ZLB) or reduces consumption crowding-out (at the steady state) when goods are complements, while consumption is clearly crowded-out when goods are substitutes. However, as will be clear when discussing the role of key parameters such as the labor supply elasticity, whether goods are complements or substitutes is far from neutral, as this not only affects the dynamics of consumption but also that of labor supply and aggregate demand.

Let us now discuss the implications of some key parameters on our results, starting with the labor supply elasticity  $1/\psi$ . First, when labor becomes more elastic, labor supply becomes more sensitive to the variations of the after-tax real wage. This is the direct effect through which a more elastic labor supply (lower  $\psi$ ) raises labor supply and thus output in the short run after a spending shock. It also lowers labor supply and thus output more in the medium run after an increase in the tax rate, that lowers the after-tax real wage. Second, when labor supply becomes more elastic, the real wage rises less after a spending shock, as the labor supply curve is flatter. It attenuates the rise in the equilibrium real wage, the rise in private consumption and the rise in aggregate demand. As such, it contributes negatively to aggregate output. This indirect effect is stronger when consumption is crowded-in after a spending shock, that is, when public and private goods are complements ( $\nu < 1$ ) or at the ZLB. Clearly, short-run multipliers (2 year) at the steady state are always larger when labor becomes more elastic, as the direct effect dominates.

On the contrary, short-run multipliers at the ZLB are always lower when labor supply becomes more elastic, as the indirect effect dominates since consumption is strongly crowded-in. This pattern also applies to medium run (5 years) multipliers.

Let us now shift the discussion to the impact of tax rule parameters  $d_{\tau}$  and  $d_{\eta}$ . The baseline calibrated value is quite larger than suggested by the empirical estimates, a choice that was made to illustrate our main results graphically.<sup>9</sup> However, Table 2 shows very clearly that our main result remains qualitatively unchanged when considering more realistic values of  $d_{\tau}$  and  $d_{\eta}$ . When the spending shock hits at the steady state, a less aggressive response of taxes raise the value of multipliers. Public debt increases after the shock, so a larger rise of tax rates implies more distortions imposed on labor or capital, and therefore lower multipliers. When the shock hits at the ZLB, less aggressive tax rules actually lower the value of multipliers. As already explained and shown in Figure 1, fiscal policy becomes self-financing at the ZLB and a spending shock implies a large rise in tax bases. Public debt falls, and if taxes respond less firmly to those changes in public debt, they fall less and subsequently produce a smaller fall in the distortions imposed on capital accumulation and labor, a smaller boost to the economy and slightly lower multipliers.

To summarize, our main result is the fact that high levels of public debt in the steady state produce lower multipliers when the public spending shock hits at the steady state but larger multipliers when the shock hits at the ZLB. The chief reason relies on the combination of two features of our economy: (i) the fact that fiscal policy becomes self-financing at the ZLB, therefore implying a fall in public debt and then a fall in distortionary taxes, while the opposite occurs in normal times; and (ii) the fact that the rollover cost of debt and the output costs of taxation are higher when debt and taxes are larger. When debt is initially high, taxes are initially high as well, and the responses of debt and taxes are larger after a spending shock: public debt and taxes increase more in the high debt economy when the shock hits at the steady state, and fall more when the shock hits at the ZLB. Our main result is robust to considering substitutable public and private goods, and therefore does not rely on an exotic assumption, even though we argue that complementarity is empirically more realistic. It is also insensitive to the type of tax used to ensure fiscal solvency in the long run, as long as the tax used is distortionary: all the above results hold when considering tax rules separately. Finally, it holds true under various tax rule parameters and for a range of empirically realistic values for the labor supply elasticity.

## 5 Optimized public spending rules in a crisis

We now consider endogenous variations of public spending. Our goal is to assess the extent to which higher levels of debt imply different optimized responses of public spending to a crisis

 $<sup>^{9}</sup>$ Corsetti, Meier, and Müller (2012) show that this large value is necessary to guarantee the determinacy of the equilibrium.

shock. On the one hand, public spending might be more effective in stimulating output and hence escape a crisis. On the other hand, too much public spending could become costly if fiscal policy becomes non-self-financing and thus provokes a rise in future distortionary taxes. Thus, what is the welfare-maximizing path of public spending? Do higher initial levels of debt imply larger or smaller changes in public spending? Or should this more effective tool be used less intensively? To anwser these questions, we abstract from spending shocks *per se* and consider that the government follows a simple spending rule. The rule makes government spending react directly to the initial capital quality shock with some persistence:

$$g_t - g = \rho_g^* (g_{t-1} - g) - d_g^* \varepsilon_{\xi,t}$$
(27)

The coefficients  $(\rho_g^*, d_g^*)$  are chosen to maximize the Hicksian consumption equivalent  $\epsilon$  that solves:

$$E_t \left\{ \sum_{s=t}^{\infty} \left( \beta^{s-t} \right) u\left( c_s, g_s, \ell_s \right) - \sum_{s=t}^{\infty} \left( \beta^{s-t} \right) u\left( c\left( 1 + \epsilon/100 \right) \right), g, \ell \right) \right\} = 0$$
(28)

Variable  $\epsilon$  is expected to be negative after a large economic downturn. It measures the steadystate percentage of consumption loss associated with experiencing macroeconomic fluctuations, induced in our case by a negative capital quality shock. As seen in Appendix B, the shock implies an important drop in private consumption, inducing large current-period utility losses.

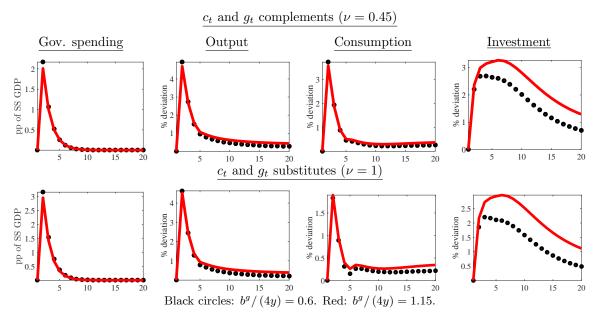
Figure 2 reports the optimized dynamic response of government spending after a 5 percent negative capital quality shock, as well as the net effects of this spending policy on macroeconomic aggregates. The latter are computed as the difference between the responses with an optimized policy and the responses with constant public spending.

First, Figure 2 shows that the optimized response of the government is to increase government spending under all configurations. Intuitively, raising public spending provides direct utility gains, since public expenditure enter the utility function of households. It also provides indirect utility gains as raising public spending at the ZLB produces a crowding-in effect of private consumption, and lowers the private investment crowding-out effect with respect to what happens during normal times. This result holds irrespective of the Edgeworth complementarity parameter  $\nu$ . As such, raising public spending raises the welfare of households.<sup>10</sup>

Second, the size of the government intervention is affected by the initial debt-to-GDP ratios, and by the Edgeworth complementarity parameter  $\nu$ . We shown in the previous sections that government spending policies are more effective (in the sense of a larger output multiplier) at the ZLB when the initial debt-to-GDP ratio is high. Figure 2 confirms this, as the optimized response of public spending is slightly smaller in this case, but produces comparable or larger

<sup>&</sup>lt;sup>10</sup>Our results, although derived in a different environment, are qualitatively and quantitatively consistent with those reported by Bilbiie, Monacelli, and Perotti (2018) and Nakata (2017).

Figure 2: Optimized response of government spending after a 5% negative capital quality shock and net effect on macroeconomic aggregates.



positive effects on output, consumption and investment. This holds true whether public and private goods are complements or substitutes. In the latter case, public spending rise less, around 2 pp of steady-state GDP, while the increase is quite larger, around 3 pp of GDP, when public and private goods are substitutes.

Table 3: Optimized policy rules.

	Low debt $\left(\frac{b^g}{4y}\right) = 0.6$						High debt $\left(\frac{b^g}{4y}\right) = 1.15$							
	$\epsilon^{c}$	$\epsilon^{c+g}$	$\Delta \epsilon$	$ ho_g$	$d_g$	2 years	5 years	$\epsilon^{c}$	$\epsilon^{c+g}$	$\Delta \epsilon$	$ ho_g$	$d_g$	2 years	5 years
$\nu = 0.45$	-3.37	-3.11	0.25	0.49	0.37	2.96	3.80	-3.49	-3.18	0.31	0.50	0.34	3.25	4.56
$\nu = 1$	-3.39	-3.18	0.21	0.49	0.53	1.82	2.27	-3.53	-3.25	0.28	0.48	0.50	2.10	2.93

Note:  $\epsilon^c$  denotes the welfare loss from the crisis with constant public spending, in percents of permanent consumption.  $\epsilon^{c+g}$  denotes the welfare loss from the crisis with an active optimized spending rule.  $\Delta \epsilon$  is the welfare gain from active spending policies:  $\Delta \epsilon = \epsilon^{c+g} - \epsilon^c$ .  $\rho_g$  and  $d_g$  are the optimized coefficients of the spending rule. Columns "2 years" and "5 years" respectively denote the present-value multipliers of output at the horizon of 8 quarters and 20 quarters.

In addition, Table 3 confirms the results given by the IRFs: high initial levels of debt and complementarity between public and private goods are associated with less aggressive spending policies, given that the latter are more effective at stabilizing output. Indeed, output multipliers are larger at the horizon of 4 or 20 quarters when debt levels are initially high or when public and private goods are complements in utility.<sup>11</sup>

<sup>&</sup>lt;sup>11</sup>Notice that the values of output multipliers differ quite substantially from those reported in the first sections of the paper. These differences are attributed to the fact that the persistence and size of increases in public spending both depend on the rule, and are no longer determined exogenously. Given this, one should not seek to compare directly the values reported in Table 3 with those reported in Table 2.

Closest to the above analysis are Bilbiie, Monacelli, and Perotti (2018) and Nakata (2017), who derive Ramsey policies subject to ZLB episodes. Some of our results are in perfect accordance with theirs. In particular, the fact that government interventions imply an increase in public spending. Further, the size of government interventions are broadly comparable, as well as the size of welfare gains from active policies at the ZLB. Our results differ however along crucial dimensions. First, Bilbiie, Monacelli, and Perotti (2018) assume lump-sum taxation. As such, the initial level of debt is irrelevant to the analysis. Second, Nakata (2017) finds that higher initial levels of debt should imply more aggressive spending policies while we find the opposite. In our view, this is due to the fact that the labor income tax follows a systematic feedback rule while this variable is an optimized policy instrument in Nakata (2017). In any case the design of optimal policies is not the main focus of our paper. We simply derive optimized rules to contrast the potential impact of the initial level of debt on the design of government interventions at the ZLB, and show that it potentially has non-trivial consequences.

## 6 Conclusion

This paper investigates the relation between the initial level of debt and the effectiveness of public spending shocks in a New-Keynesian model with capital accumulation, distortionary taxes and a lower bound constraint on the nominal interest rate. We find that countries with high debt are more fragile in the event of a crisis, as they experience larger economic downturns. In line with the literature, we also find that the spending multipliers are lower with a high initial debt-to-GDP ratio during normal times, and larger than during normal times when the ZLB is binding.

The novel result of the paper is that economies with a high initial debt-to-GDP ratio feature larger spending multipliers at the ZLB. The result is driven by the fact that fiscal policy becomes self-financing at the ZLB, allowing the debt-to-GDP ratio to fall after a spending shock, then producing a fall in distortionary taxes. Because the efficiency costs of taxation are convex, the subsequent fall in tax rates are larger when debt is initially higher, leading to larger positive effects on output. This raises the spending multipliers. Finally, this result implies that optimized spending policies at the ZLB are affected by the initial level of debt: a lower increase in public spending is required with high initial levels of public debt, as fiscal policy is more effective at stimulating output and provides larger reductions in the welfare losses from the crisis that pushed the economy at the ZLB.

## References

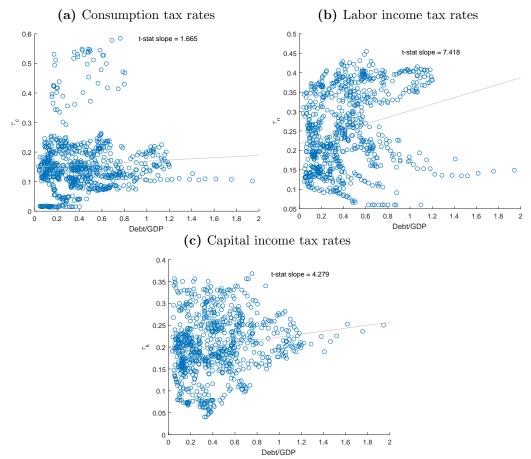
- Adjemian, Stéphane, Houtan Bastani, Michel Juillard, Frédéric Karamé, Ferhat Mihoubi, George Perendia, Johannes Pfeifer, Marco Ratto, and Sébastien Villemot. 2011. "Dynare: Reference Manual, Version 4." Dynare Working Paper 1, CEPREMAP.
- Auerbach, Alan J. and Yuriy Gorodnichenko. 2012. "Fiscal Multipliers in Recession and Expansion." In *Fiscal Policy after the Financial Crisis*, NBER Chapters. National Bureau of Economic Research, Inc, 63–98.
- Auray, Stéphane and Aurélien Eyquem. 2017. "Episodes of War and Peace in an Estimated Open Economy Model." Working paper, GATE L-SE.
- Bilbiie, Florin O., Tommaso Monacelli, and Roberto Perotti. 2018. "Is Government Spending at the Zero Lower Bound Desirable?" American Economic Journal: Macroeconomics :Forthcoming.
- Boitani, Andrea and Salvatore Perdichizzi. 2018. "Public Expenditure Multipliers in Recessions. Evidence from the Eurozone." DISCE - Working Papers del Dipartimento di Economia e Finanza def068, Università Cattolica del Sacro Cuore, Dipartimenti e Istituti di Scienze Economiche (DISCE).
- Bouakez, Hafedh and Nooman Rebei. 2007. "Why Does Private Consumption Rise after a Government Spending Shock?" *Canadian Journal of Economics* 40 (3):954–979.
- Christiano, Lawrence, Martin Eichenbaum, and Sergio Rebelo. 2011. "When Is the Government Spending Multiplier Large?" Journal of Political Economy 119 (1):78–121.
- Corsetti, Giancarlo, Keith Kuester, André Meier, and Gernot J. Müller. 2013. "Sovereign Risk, Fiscal Policy, and Macroeconomic Stability." *Economic Journal* 123:F99–F132.
- Corsetti, Giancarlo, André Meier, and Gernot J. Müller. 2012. "What Determines Government Spending Multipliers?" *Economic Policy* 72:521–564.
- Eggertsson, Gauti B. 2011. "What Fiscal Policy is Effective at Zero Interest Rates?" In NBER Macroeconomics Annual 2010, Volume 25, NBER Chapters. National Bureau of Economic Research, Inc, 59–112.
- Erceg, Christopher and Jesper Lindé. 2014. "Is There a Fiscal Free Lunch in a Liquidity Trap?" Journal of the European Economic Association 12 (1):73–107.
- Galí, Jordi, J. David López-Salido, and Javier Vallés. 2007. "Understanding the Effects of Government Spending on Consumption." Journal of the European Economic Association 5 (1):227– 270.

- Gertler, Mark and Peter Karadi. 2011. "A Model of Unconventional Monetary Policy." *Journal* of Monetary Economics 58 (1):17–34.
- Ilzetzki, Ethan, Enrique G. Mendoza, and Carlos A. Végh. 2013. "How Big (Small?) are Fiscal Multipliers?" Journal of Monetary Economics 60 (2):239–254.
- Juillard, Michel. 1996. "Dynare : A Program for the Resolution and Simulation of Dynamic Models with Forward Variables through the Use of a Relaxation Algorithm." CEPREMAP Working Paper 9602, CEPREMAP.
- Leeper, Eric M. 1991. "Equilibria under 'Active' and 'Passive' Monetary and Fiscal Policies." Journal of Monetary Economics 27 (1):129–147.
- Leeper, Eric M., Nora Traum, and Todd B. Walker. 2015. "Clearing Up the Fiscal Multiplier Morass: Prior and Posterior Analysis." NBER Working Papers 21433, National Bureau of Economic Research, Inc.
- McDaniel, Cara. 2007. "Average Tax Rates on Consumption, Investment, Labor and Capital in the OECD 1950-2003." Manuscript, Arizona State University 19602004.
- Mendoza, Enrique G., Assaf Razin, and Linda L. Tesar. 1994. "Effective Tax Rates in Macroeconomics: Cross-country Estimates of Tax Rates on Factor Incomes and Consumption." Journal of Monetary Economics 34 (3):297–323.
- Nakata, Taisuke. 2017. "Optimal Government Spending at the Zero Lower Bound: A Non-Ricardian Analysis." Review of Economic Dynamics 23:150–169.
- Perotti, Roberto. 1999. "Fiscal Policy in Good Times and Bad." *Quarterly Journal of Economics* 114 (4):1399–1436.
- Reinhart, Carmen M. and Kenneth S. Rogoff. 2011. "From Financial Crash to Debt Crisis." American Economic Review 101 (5):1676–1706.

## A Debt-to-GDP and tax rates in the data

We take a quick look at the relation between debt-to-GDP ratios and tax rates using various data sources. First, we take tax data from the dataset compiled by McDaniel (2007). Following the method of Mendoza, Razin, and Tesar (1994), she computes the consumption, labor income and capital income tax rates for 15 advanced countries from 1950 to 2014.<sup>12</sup> We relate each of these tax rates with debt-to-GDP ratios taken from the updated Reinhart and Rogoff (2011) dataset for the same countries and the same time span in the following scatter plots.



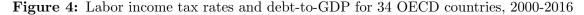


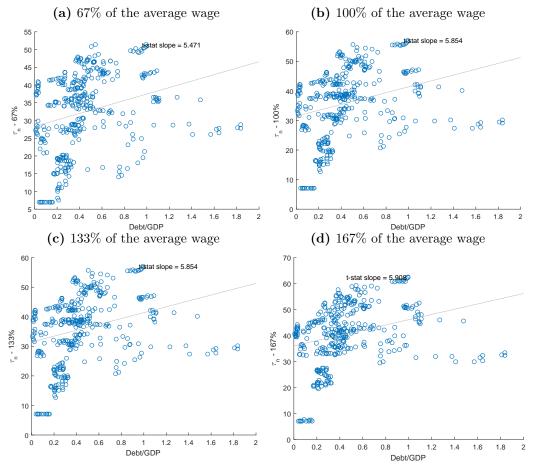
<u>Notes</u>: Tax rates are taken from the updated dataset of McDaniel (2007). Debt-to-GDP ratios are taken from the updated dataset of Reinhart and Rogoff (2011).

The above graphs are not a thorough empirical analysis but clearly suggest that higher levels of debt-to-debt are associated with larger tax rates on average over time. They are consistent with the idea of long-run fiscal sustainability. In addition, they suggest that labor income tax rates are more significantly and positively related to debt-to-GDP ratios. To confirm this first-pass analysis, we also plot various measures of labor income tax rates using OECD data. We take

<sup>&</sup>lt;sup>12</sup>The following countries are considered: Australia, Austria, Belgium, Finland, France, Germany, Italy, Netherlands, Spain, Sweden, Switzerland, United Kingdom, United States.

the OECD measures of total labor wedges at for different levels of wages (67%, 100%, 133% and 167% of the average real wage) from the OECD Tax Database for 34 OECD countries between 2000 and 2016, and relate those labor income tax measures to the debt-to-GDP levels reported in the Central Government Debt OECD dataset for the same countries over the same period.<sup>13</sup> Again, we pool all data together to get an idea of the average relation between debt-to-GDP and labor income tax rates. The second set of graphs confirms the positive relation between





<u>Note</u>: Labor income tax rates are taken from the OECD tax database. They are computed using personal income taxes and social security contribution rates on gross labor income. Debt-to-GDP ratios are taken OECD Central Government Debt dataset.

debt-to-GDP ratios and labor income tax rates. Overall, this simple descriptive analysis shows that our assumption that consists in adjusting either the labor or the capital tax rate in the steady state when we vary the steady-state debt-to-GDP ratio is broadly consistent with the data.

<sup>&</sup>lt;sup>13</sup>The following countries are considered: Australia, Austria, Belgium, Canada, Chile, Czech Republic, Denmark, Estonia, Finland, France, Germany, Greece, Hungary, Iceland, Ireland, Israel, Italy, Japan, Korea, Luxembourg, Mexico, Netherlands, New Zealand, Norway, Poland, Portugal, Slovak Republic, Slovenia, Spain, Sweden, Switzerland, Turkey, United Kingdom, United States.

## **B** Additional figures

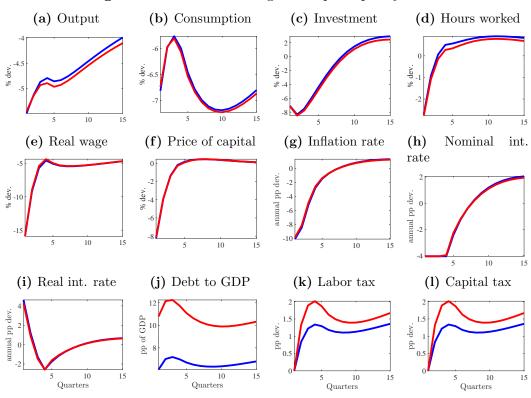


Figure 5: IRFs to a 5% negative capital quality shock.

Black:  $b^{g}/(4y) = 0.6$  and  $\tau = 0.2050$ . Red:  $b^{g}/(4y) = 1.15$  and  $\tau = 0.2481$ .